

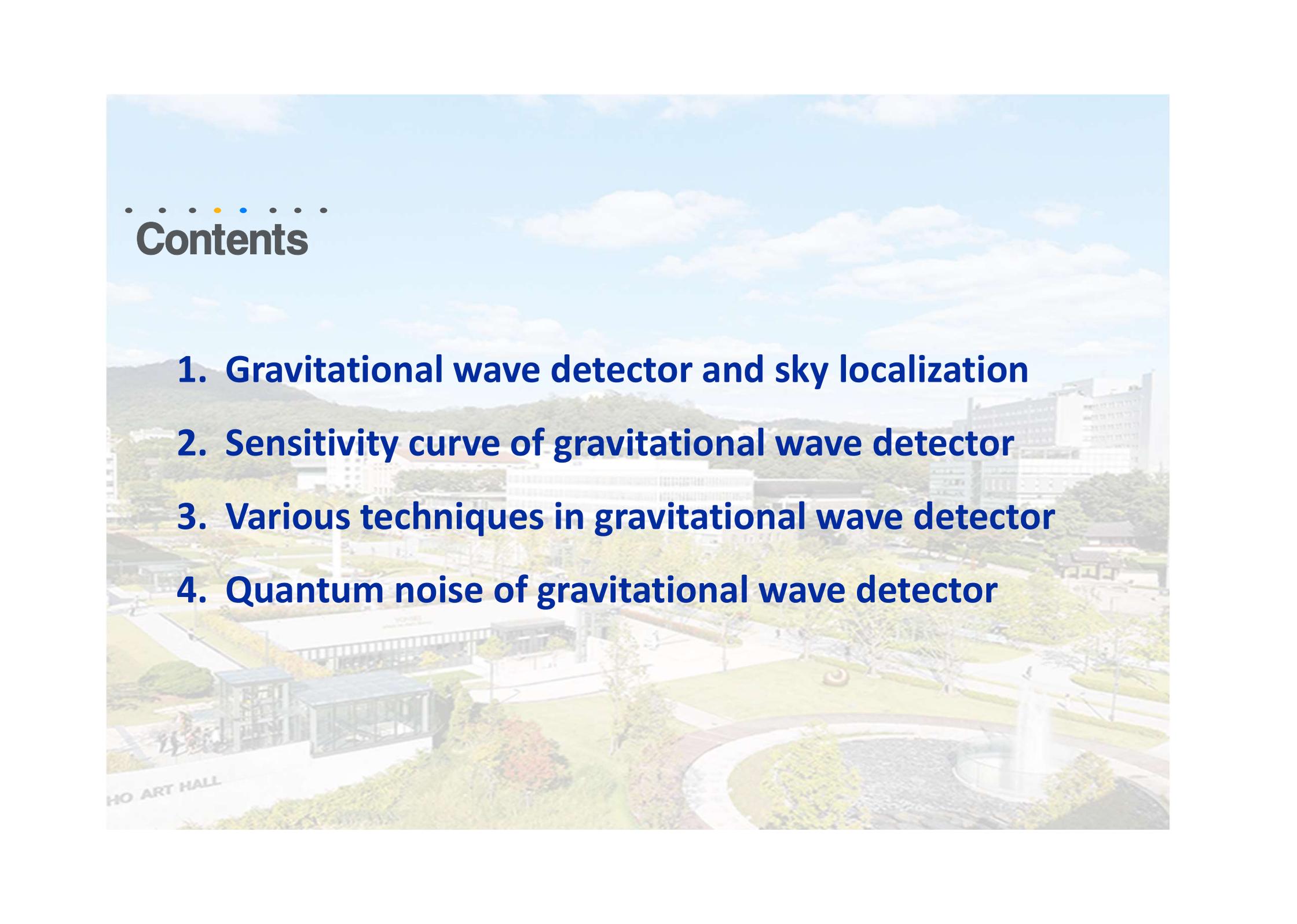
# Ground Base Laser Interferometer Gravitational Wave Detector

Department of Astronomy  
June Gyu Park

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연세대학교  
YONSEI UNIVERSITY



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**Contents**

- 1. Gravitational wave detector and sky localization**
- 2. Sensitivity curve of gravitational wave detector**
- 3. Various techniques in gravitational wave detector**
- 4. Quantum noise of gravitational wave detector**

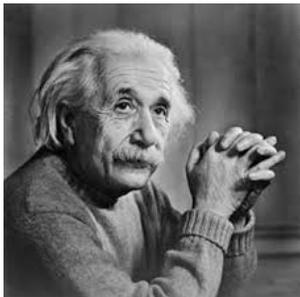
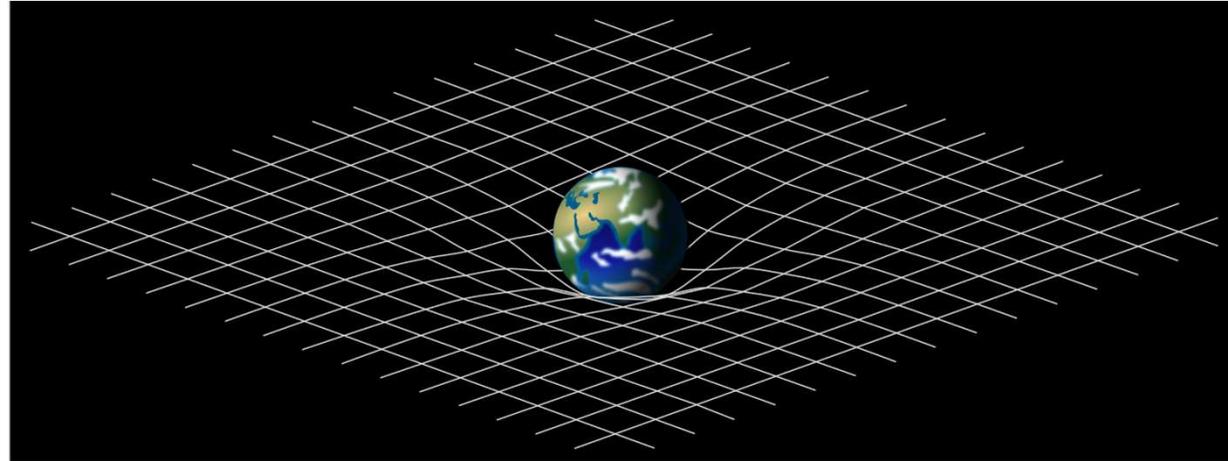


# 1. Gravitational wave detector and sky localization



# Gravity and general relativity

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$$G_{\mu\nu} + \Lambda g_{\mu\nu} = \kappa T_{\mu\nu}$$

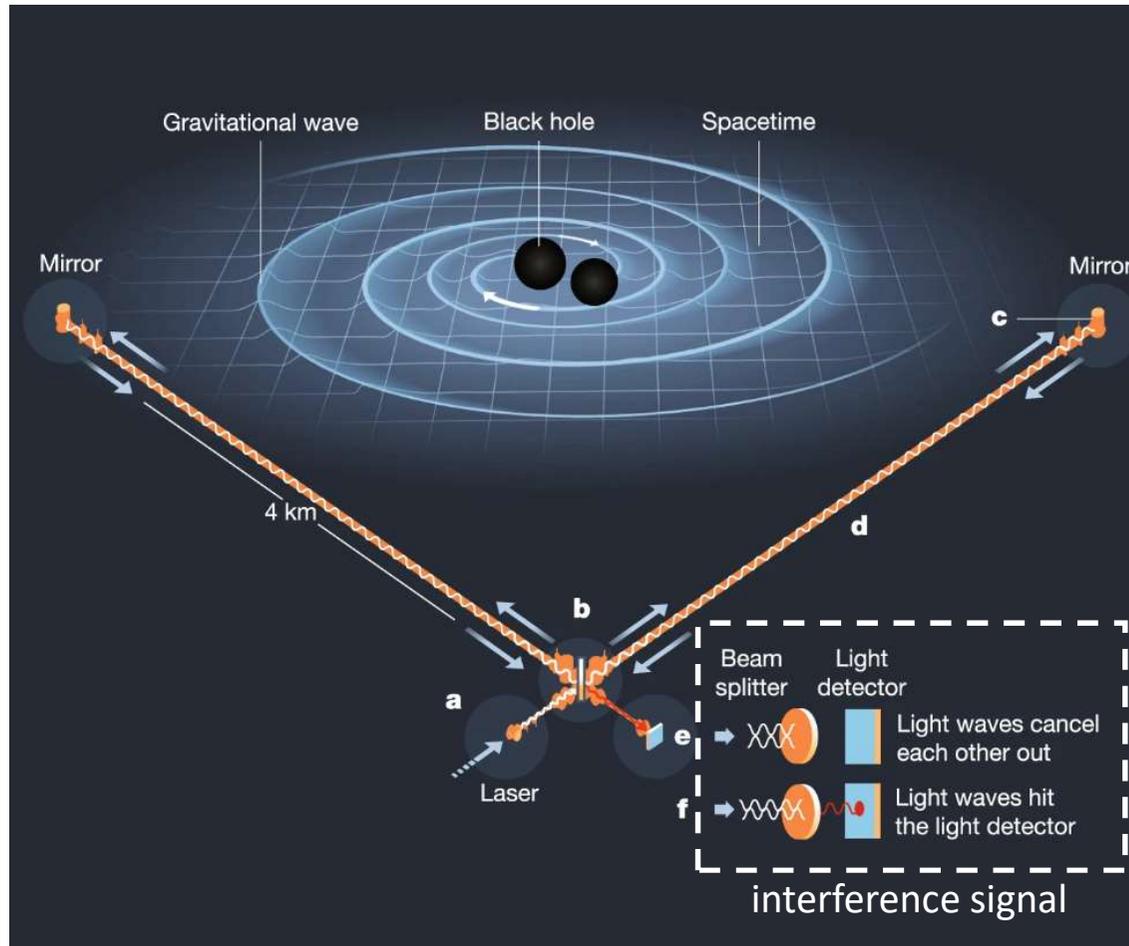
Local space time curvature

Local energy, momentum stress

Mass of object

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# Gravitational wave detector

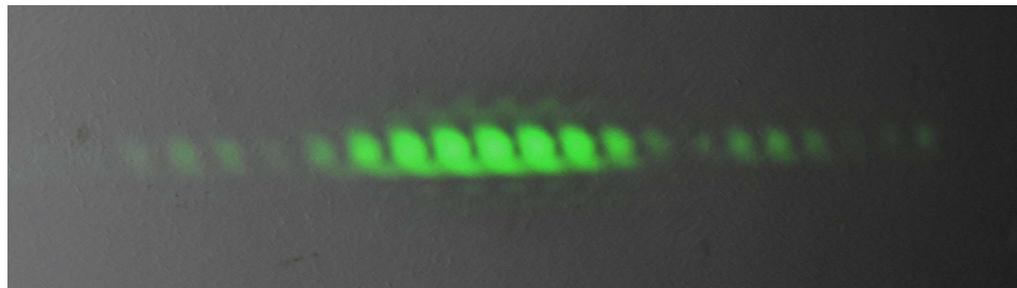
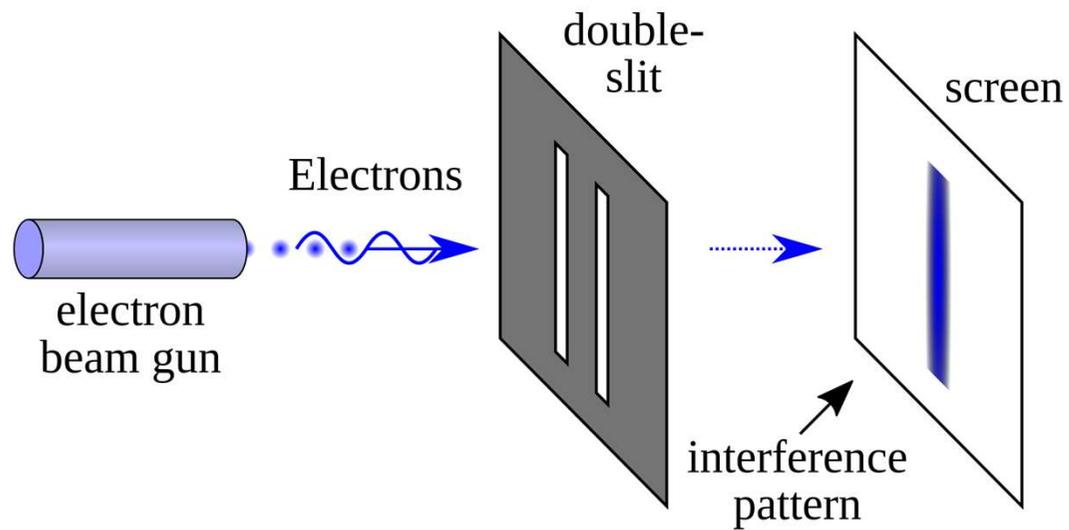


- Ground scale Michelson interferometer
- 4 km vacuum tunnel arm
- Over 1000 km interaction length

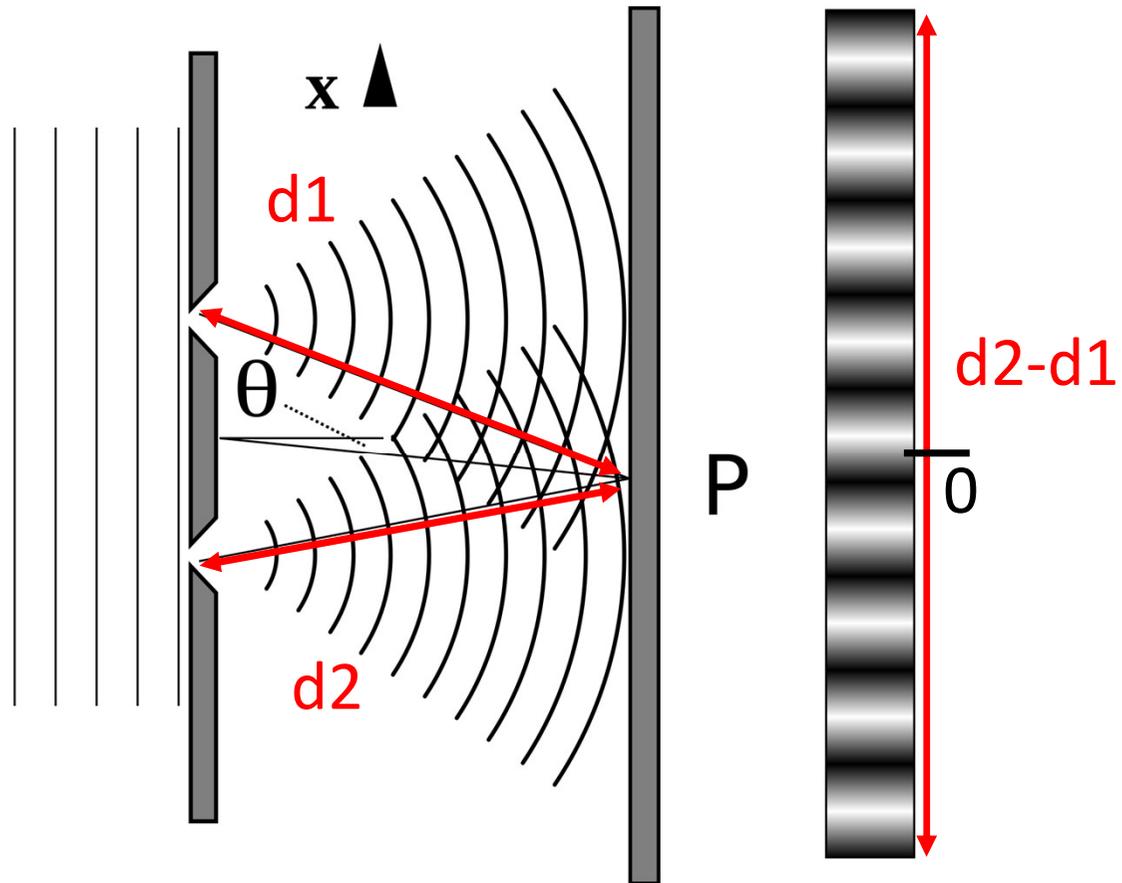
Miller, M.C., Yunes, N. The new frontier of gravitational waves. *Nature* **568**, 469–476 (2019)

# Double slit experiment

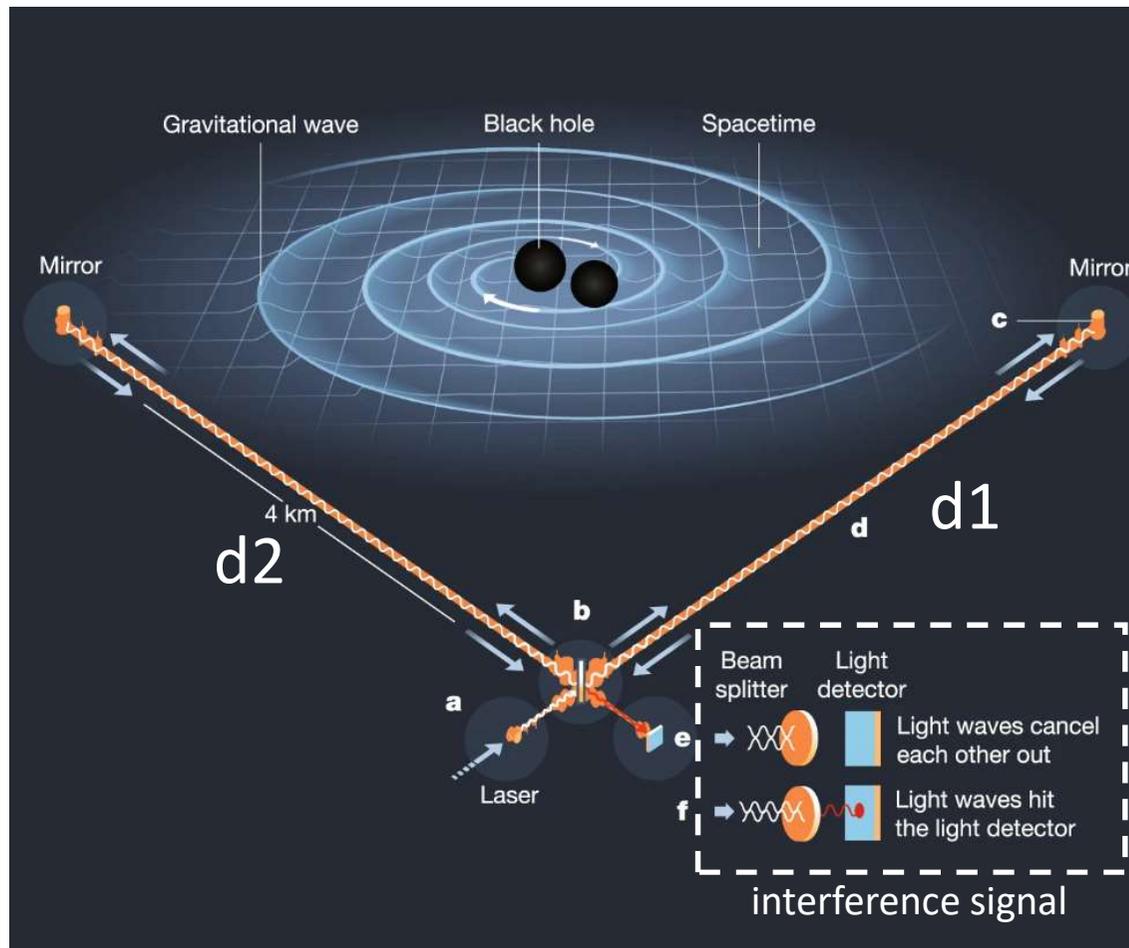
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# Interference



# Gravitational wave detector

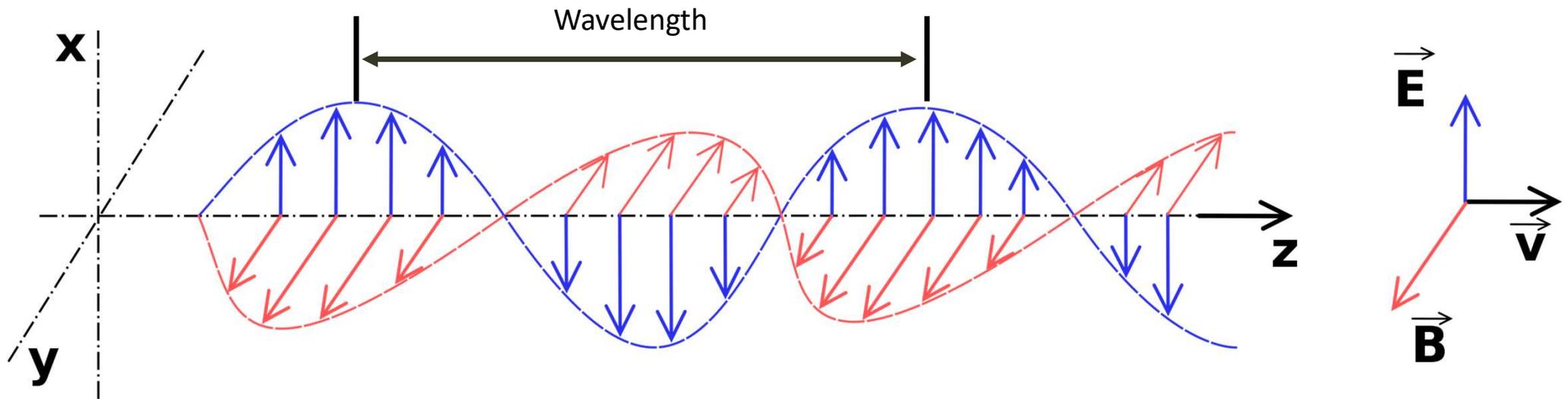


- Ground scale Michelson interferometer
- 4 km vacuum tunnel arm
- Over 1000 km interaction length

Miller, M.C., Yunes, N. The new frontier of gravitational waves. *Nature* **568**, 469–476 (2019)

# Light (Electromagnetic wave)

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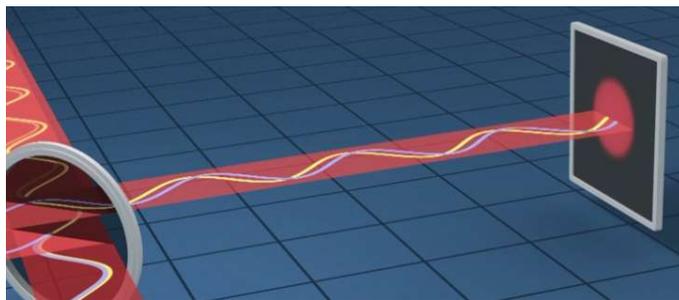
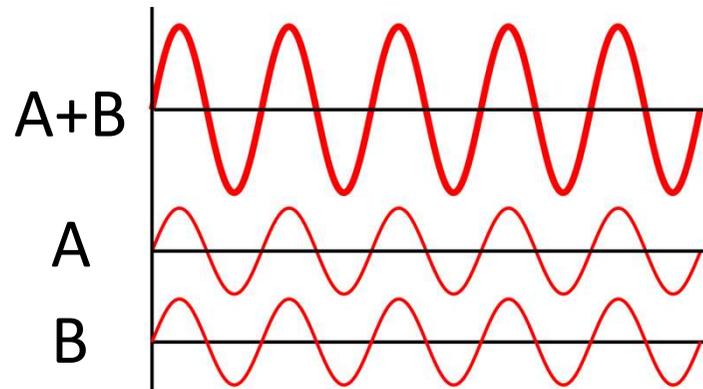


$$|\vec{E}| \propto \text{Intensity of Light}$$

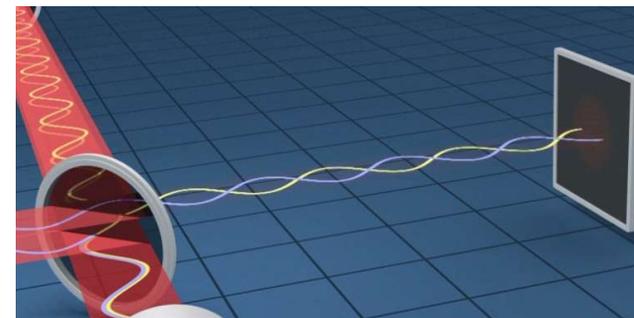
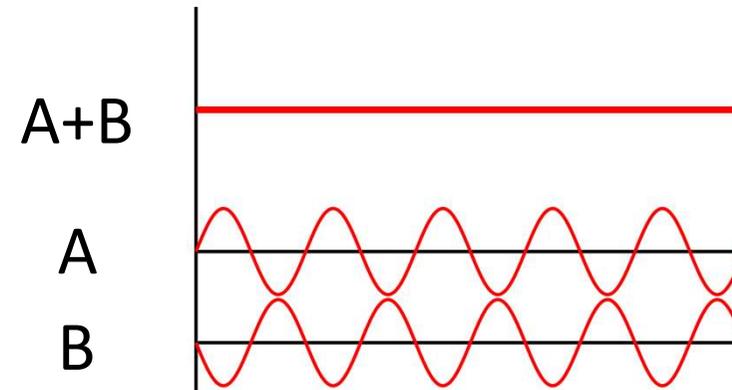
---

# Interference

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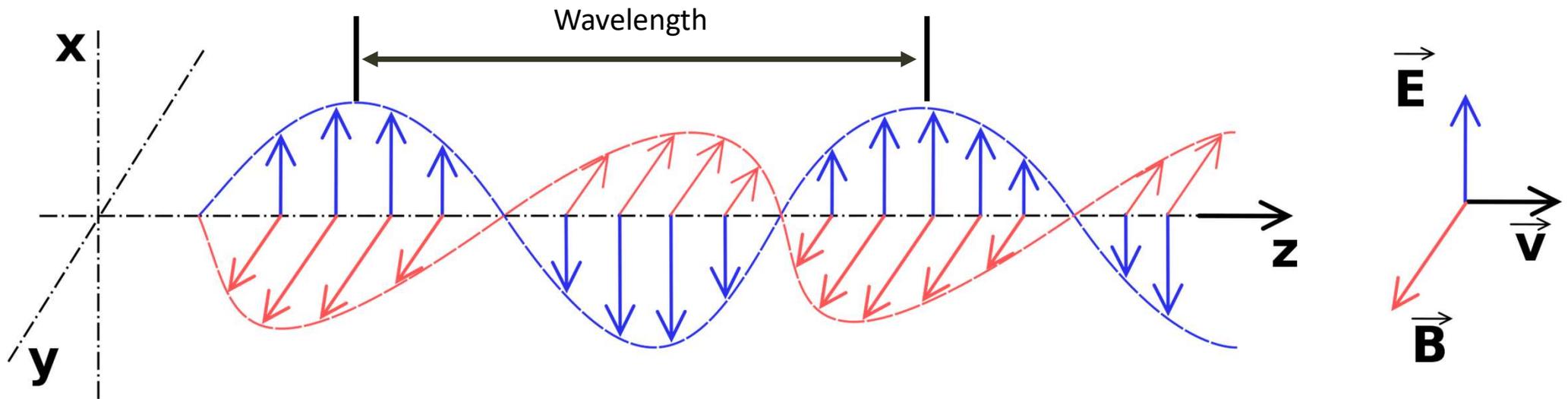
Constructive



Destructive

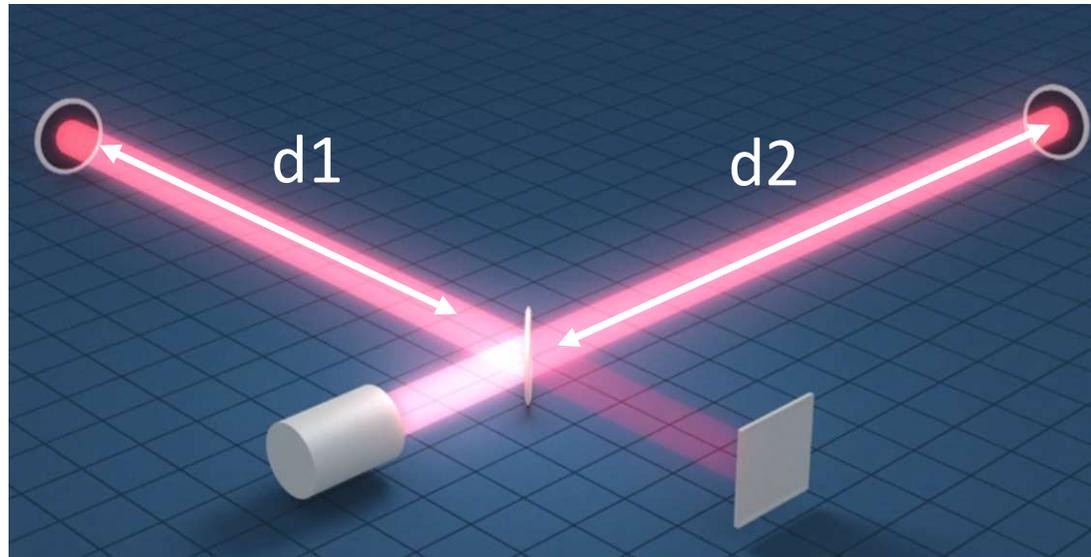
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# Light (Electromagnetic wave)



$$\vec{E} = E_0 \cos(kx - \omega t + \varphi)$$

# Interference signal

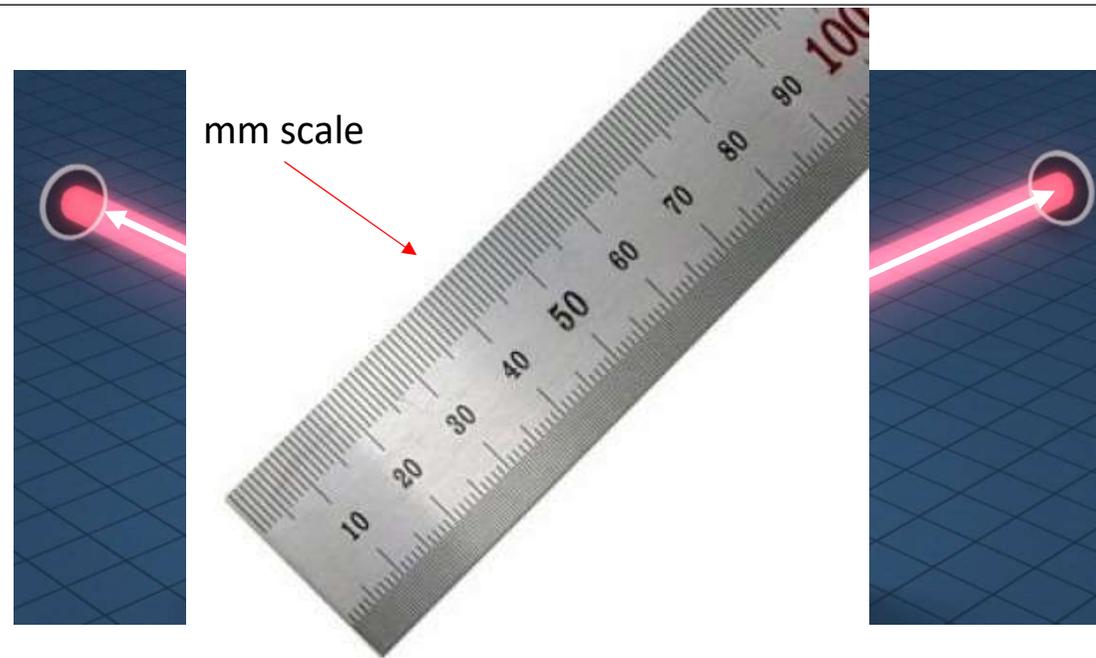


$$\vec{E} = E_0 \cos(kx - \omega t + \varphi) \quad \varphi \propto d1 - d2 \text{ (in some condition)}$$

$$k = \frac{2\pi}{\lambda} \quad \lambda : \text{wavelength}$$

$0.1\mu m \sim 10\mu m$

# Interference signal



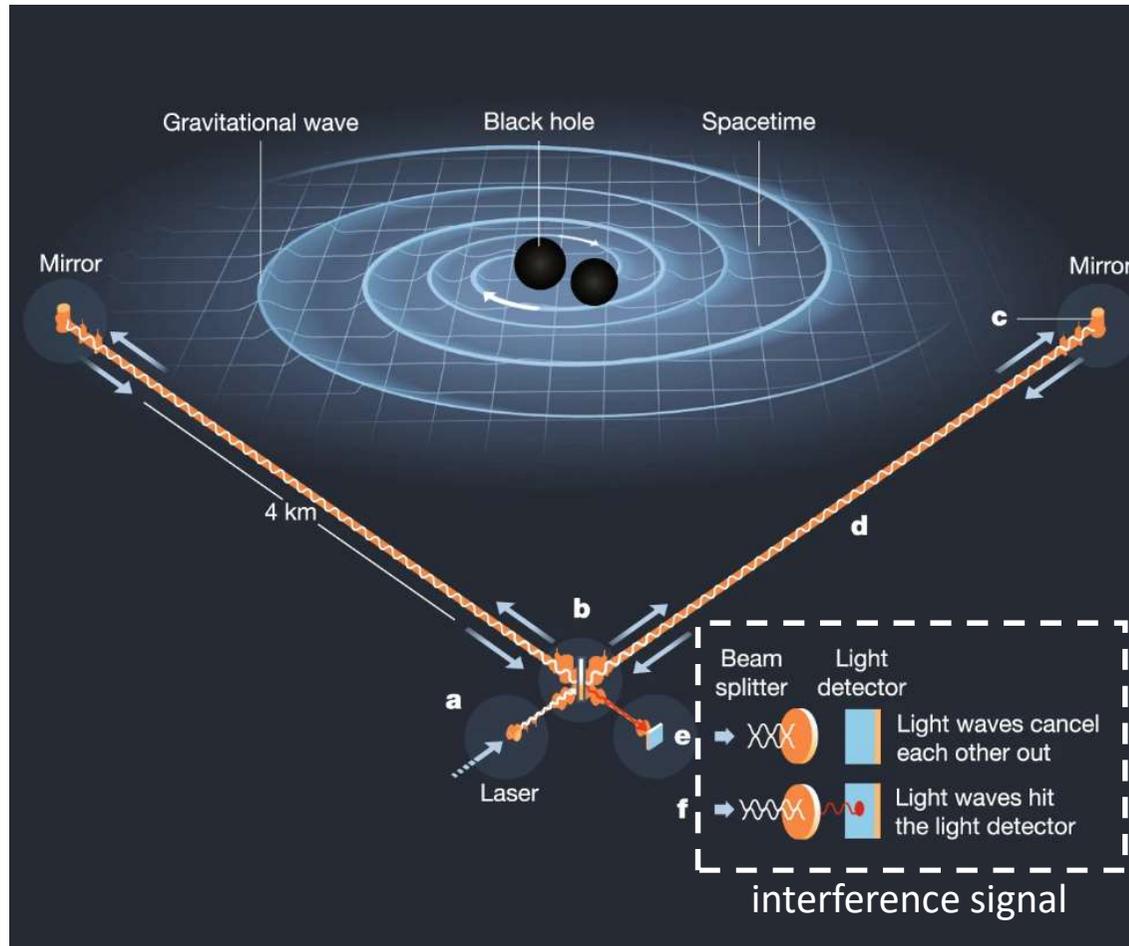
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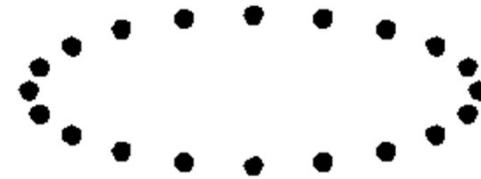
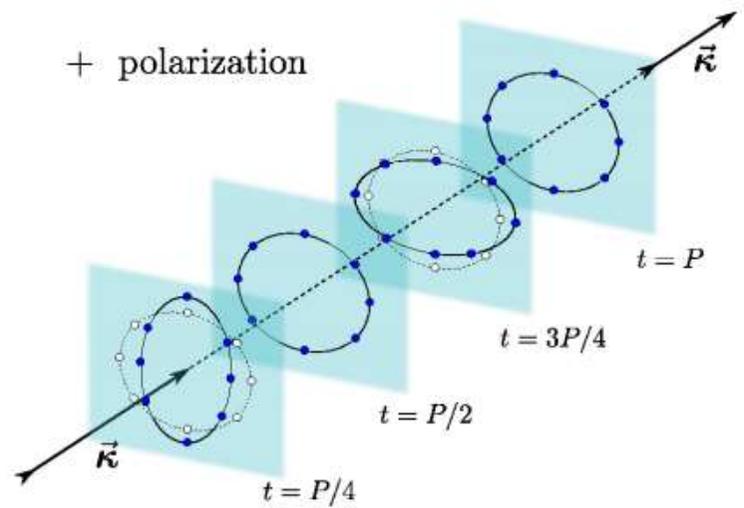
# Gravitational wave detector



- Ground scale Michelson interferometer
- 4 km vacuum tunnel arm
- Over 1000 km interaction length

Build most sensitive system  
using most simple arrangement

# Gravitational wave



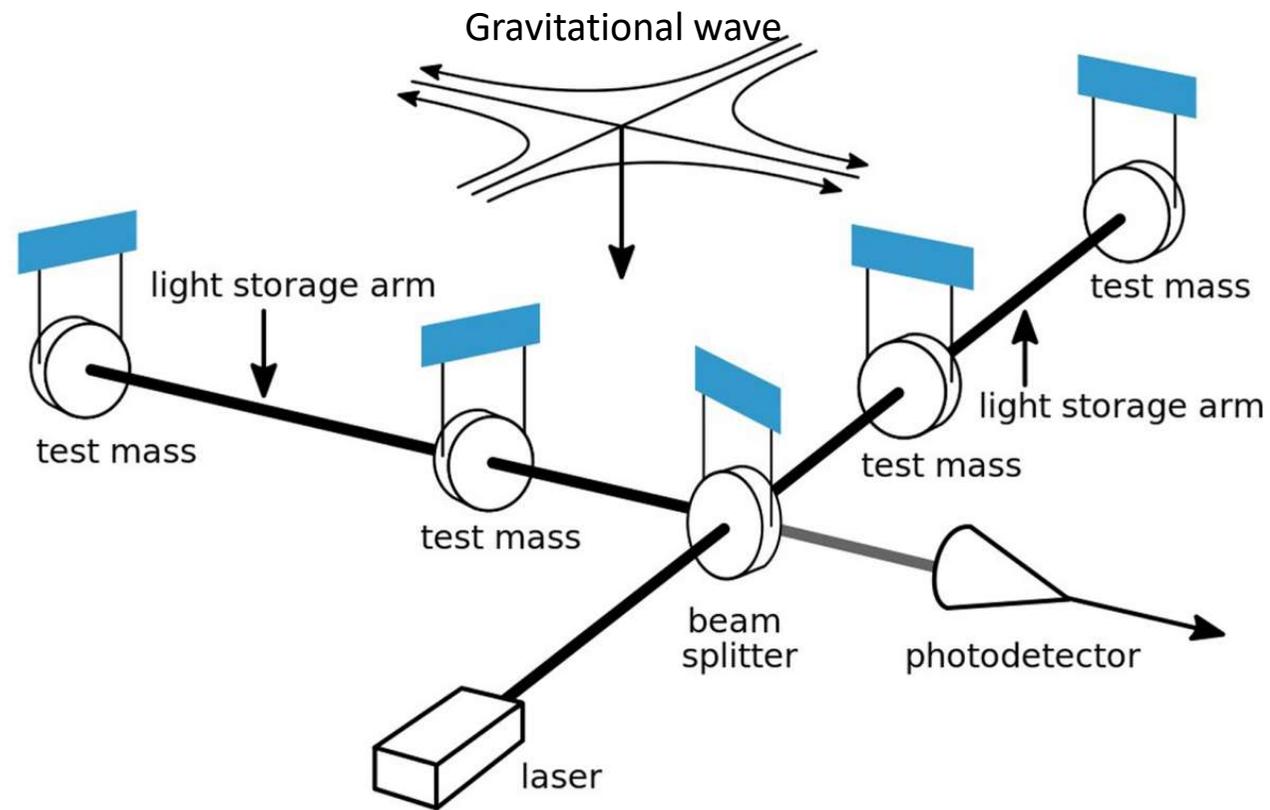
MPA Lectures on Gravitational Waves in Cosmology  
Azadeh Maleknejad  
Max-Planck-Institute for Astrophysics

# Effect of gravitational wave

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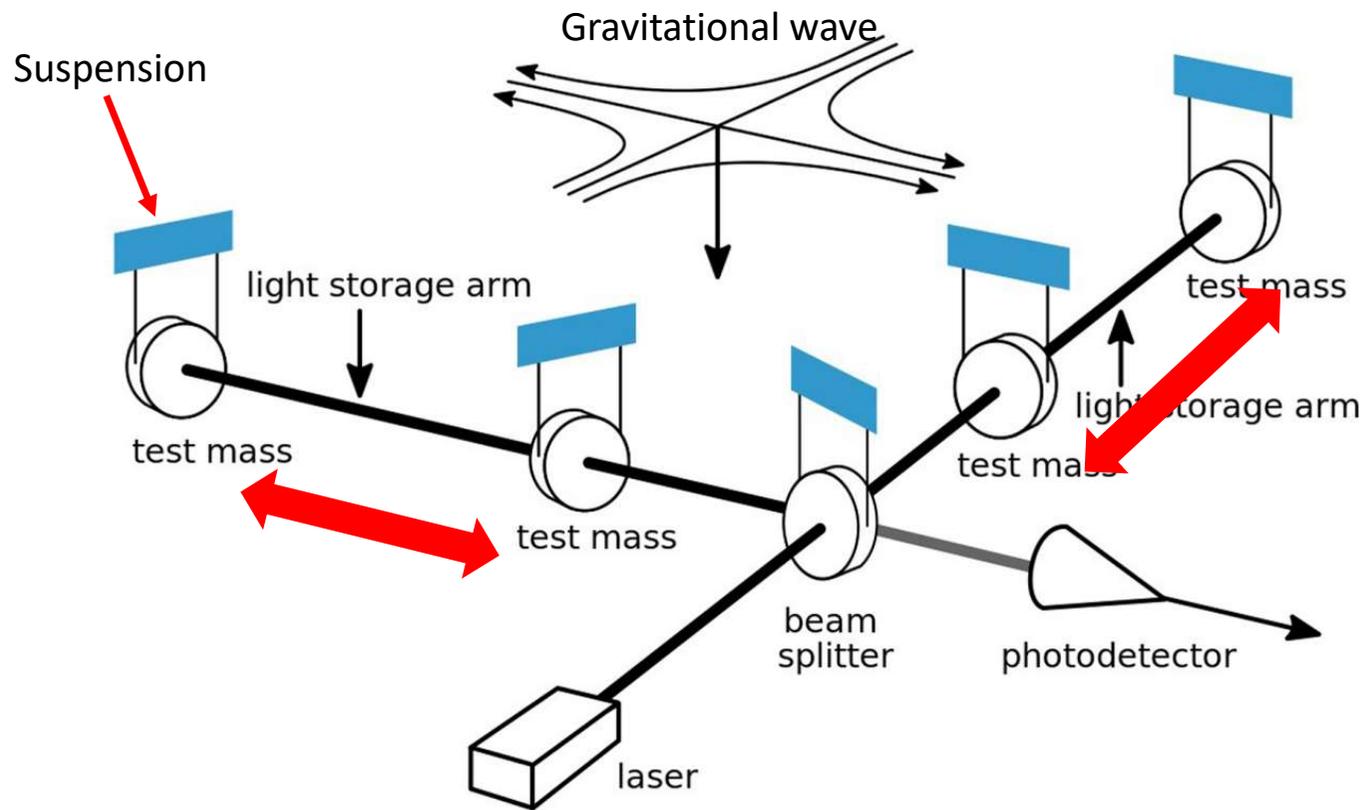


# Gravitational wave and GW detector



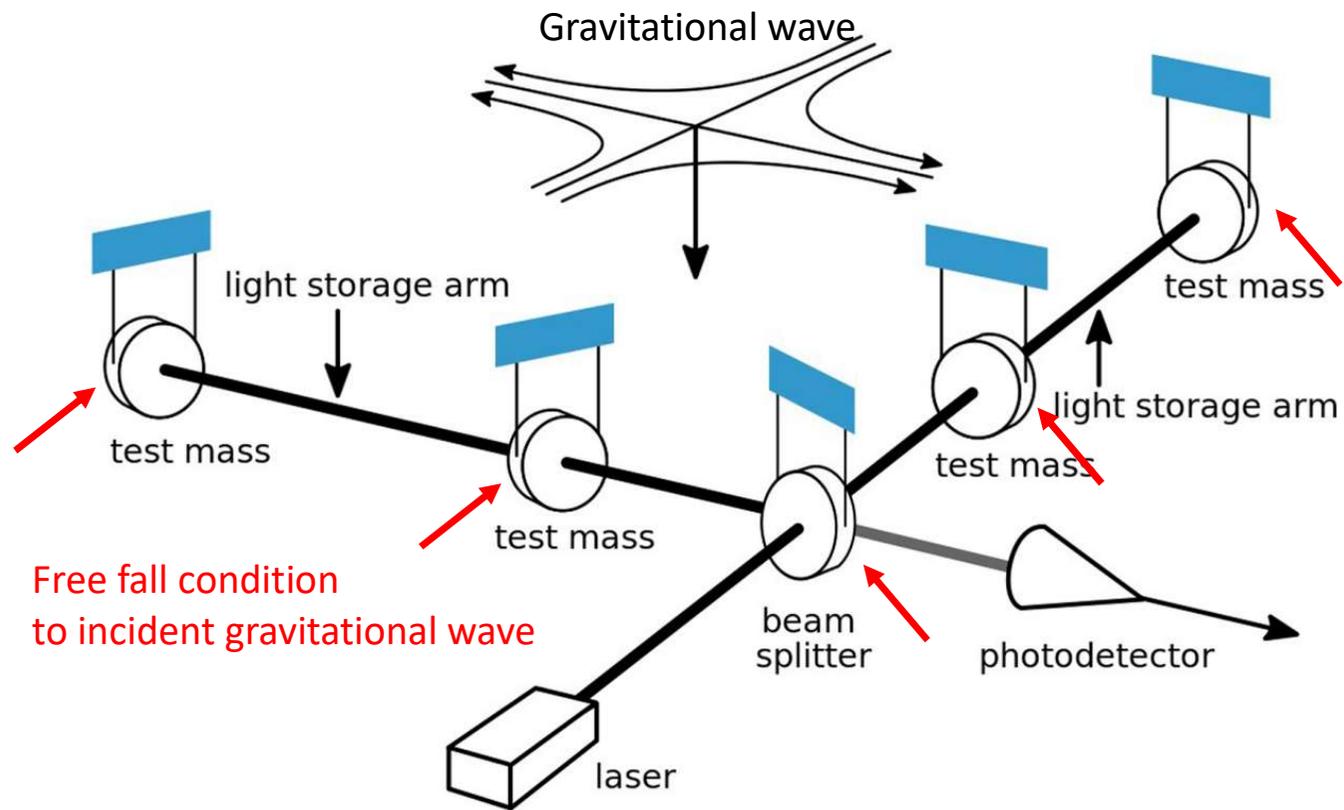
<https://www.ligo.caltech.edu/>

# Gravitational wave and GW detector

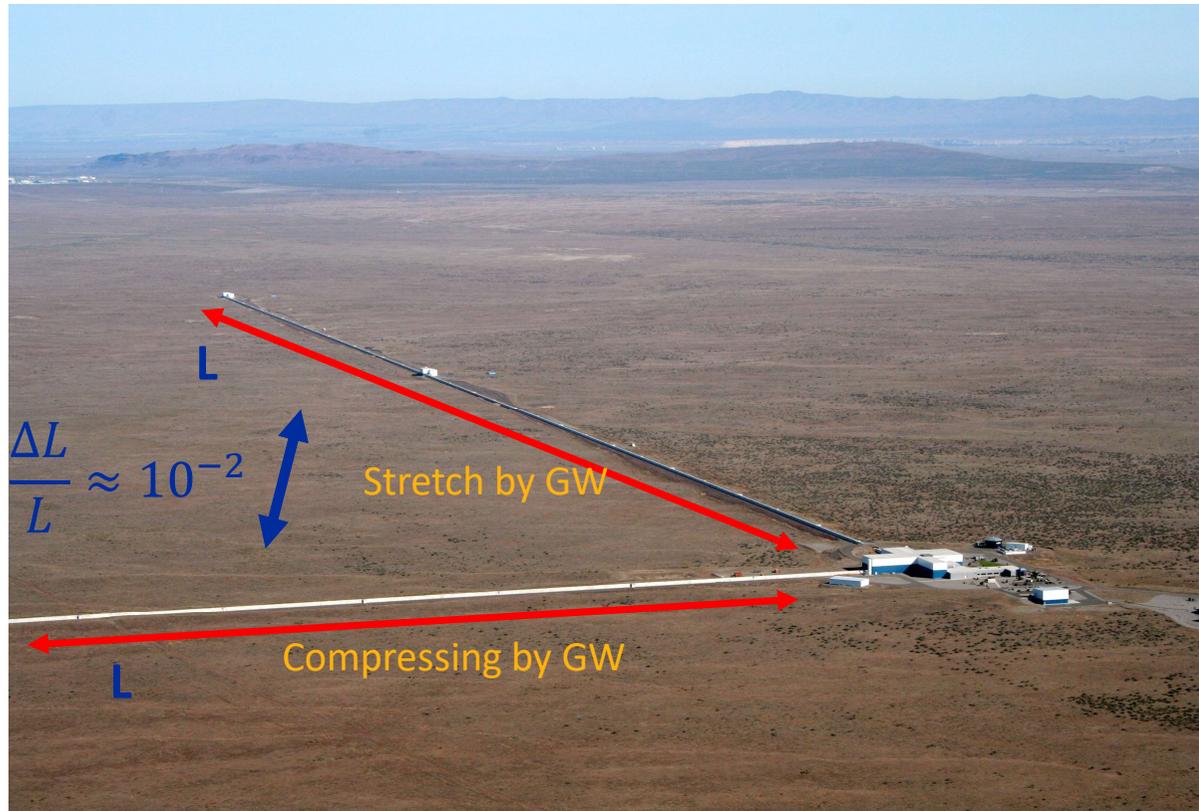


<https://www.ligo.caltech.edu/>

# Gravitational wave and GW detector



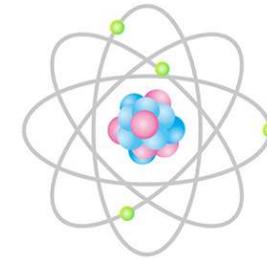
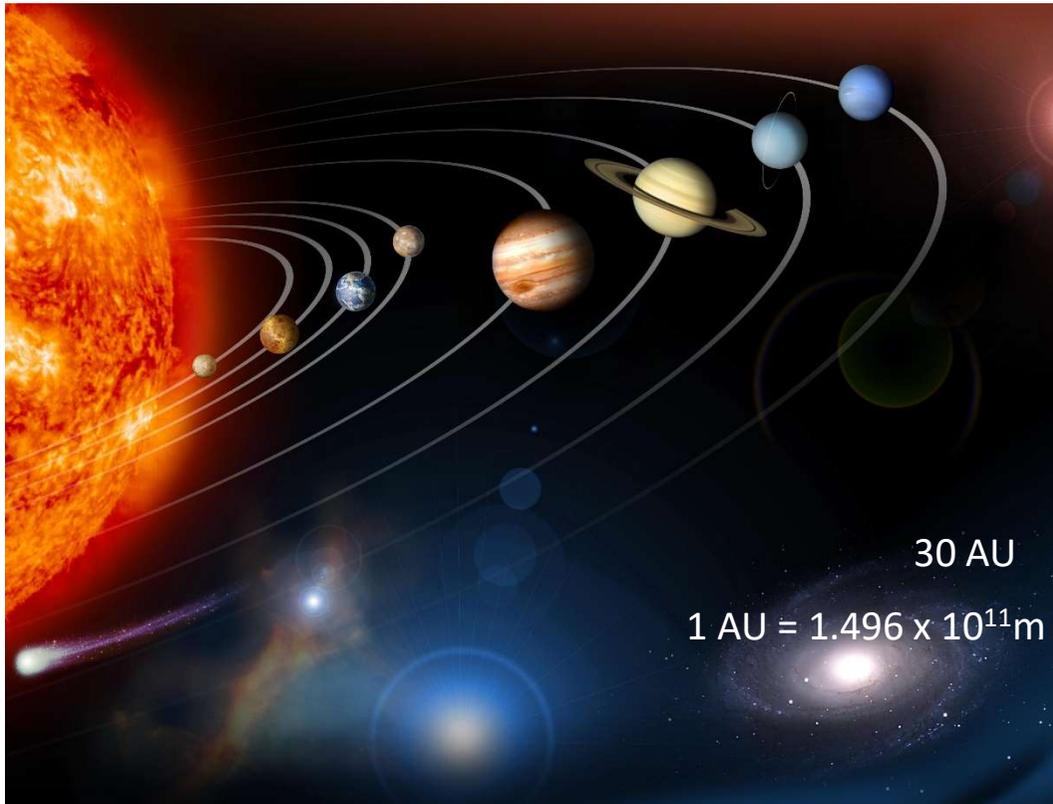
# Strain sensitivity



Minimum sensitivity

$$\frac{\Delta L}{L} \approx 10^{-21}$$

# Strain due to gravitational wave

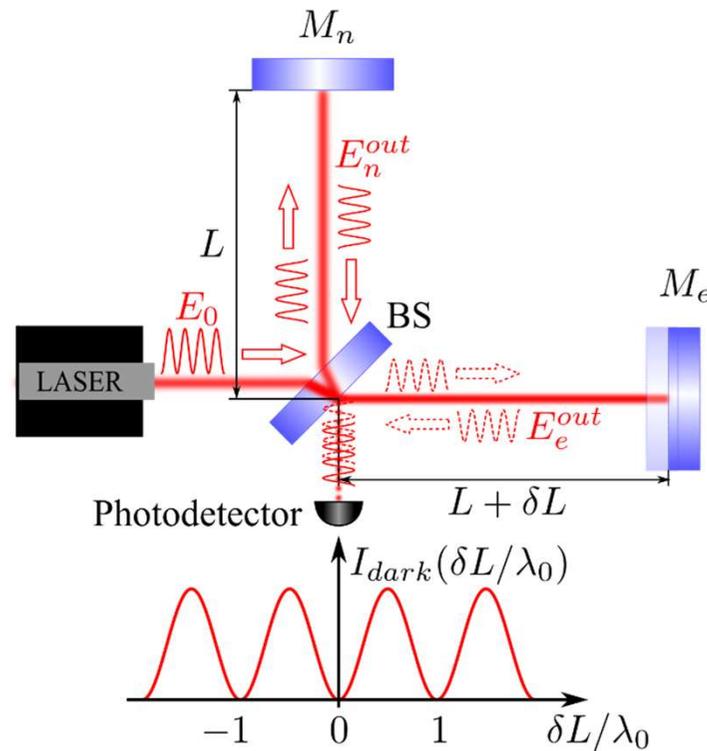


Size of atom =  $1 \times 10^{-10}$  m

$$\frac{\Delta L}{L} \approx 10^{-21}$$

Detect existence of a single atom

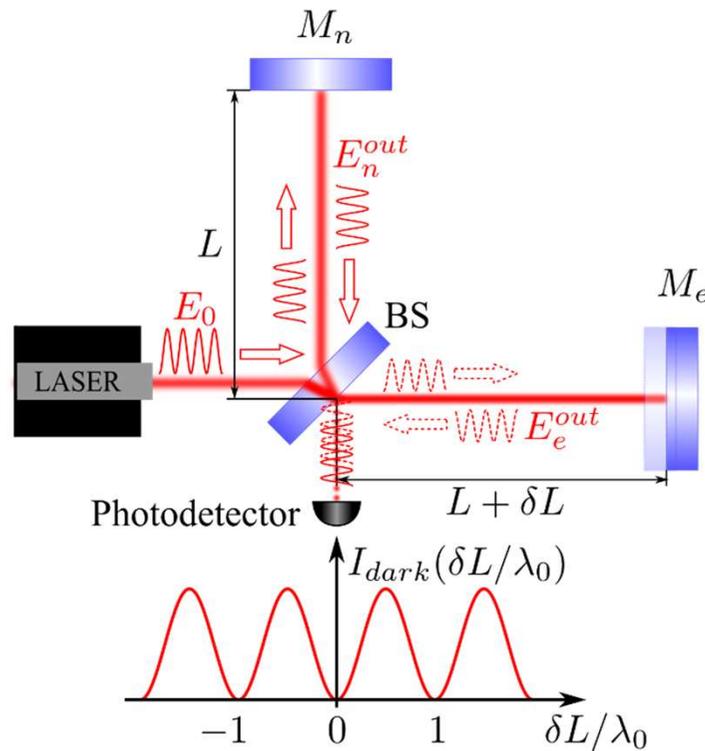
# Sensitivity of michelson interferometer



When  $L = 1 \text{ m}$

$$\frac{\Delta L}{L} \approx 10^{-1}$$

# Sensitivity of michelson interferometer



When  $L = 1 \text{ m}$

$$\frac{\Delta L}{L} \approx 10^{-16}$$

IF  $L = 1000 \text{ km}$

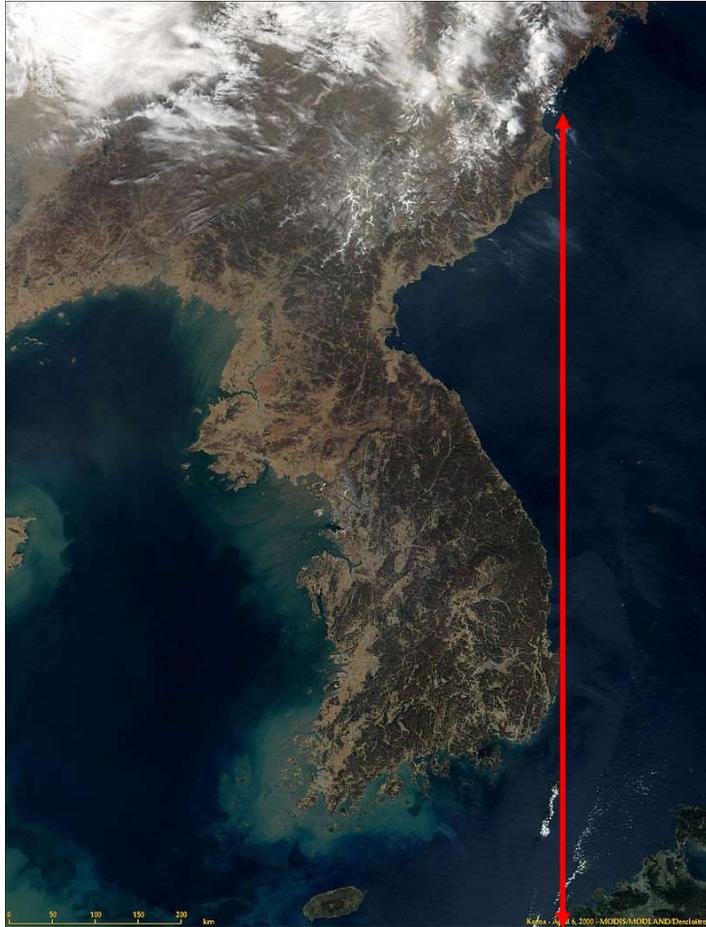
$$\frac{\Delta L}{L} \approx 10^{-2}$$

오 1000 km 간섭계를 만들면 되겠다!

Danilishin, Stefan L. et al. Living Rev.Rel. 15 (2012) 5 arXiv:1203.1706



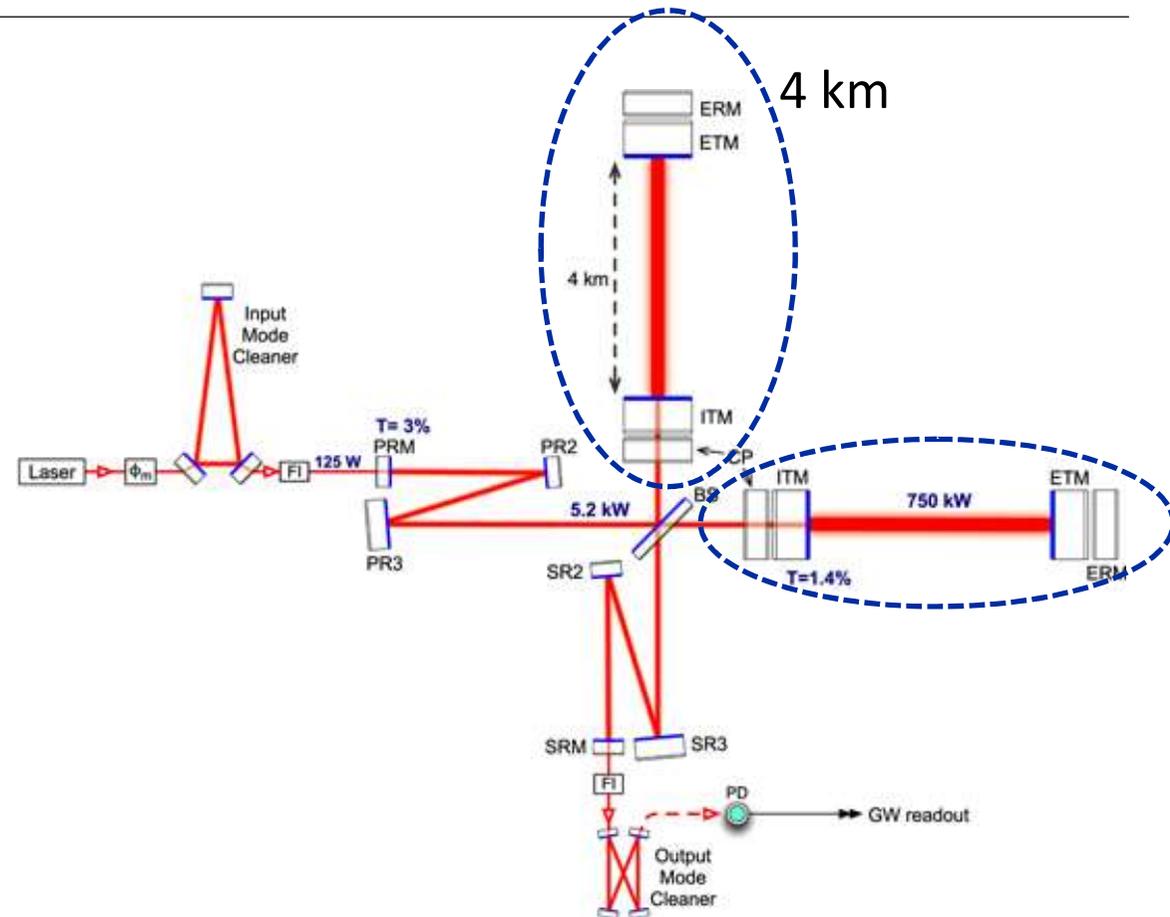
# 1000 km interferometer



~1100km



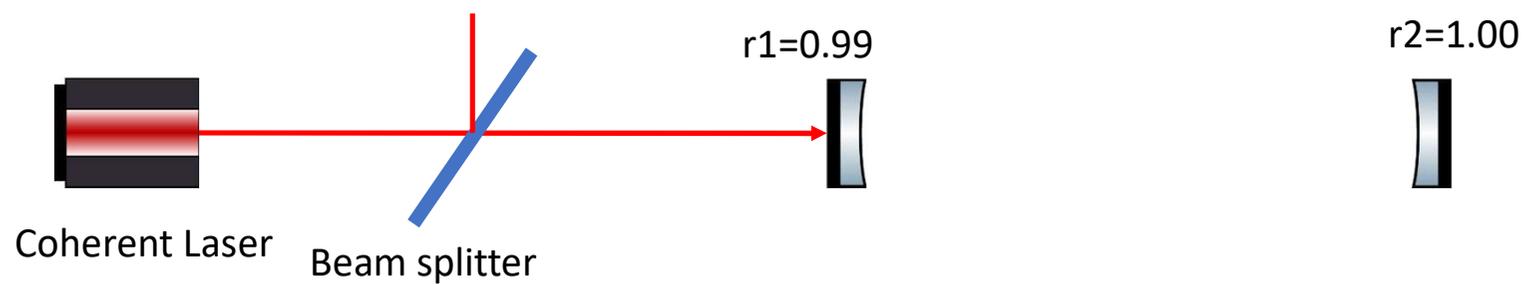
# LIGO interferometer



LIGO interferometer / Livingston

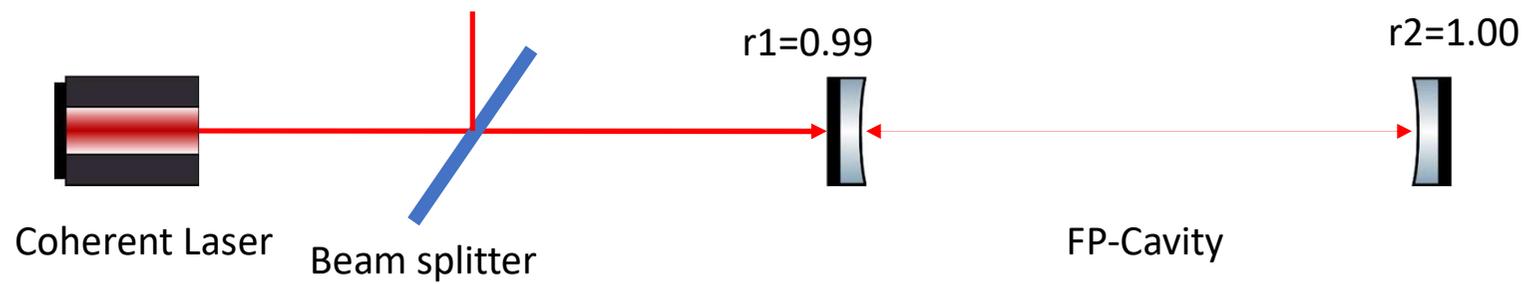
# Fabry-perot cavity

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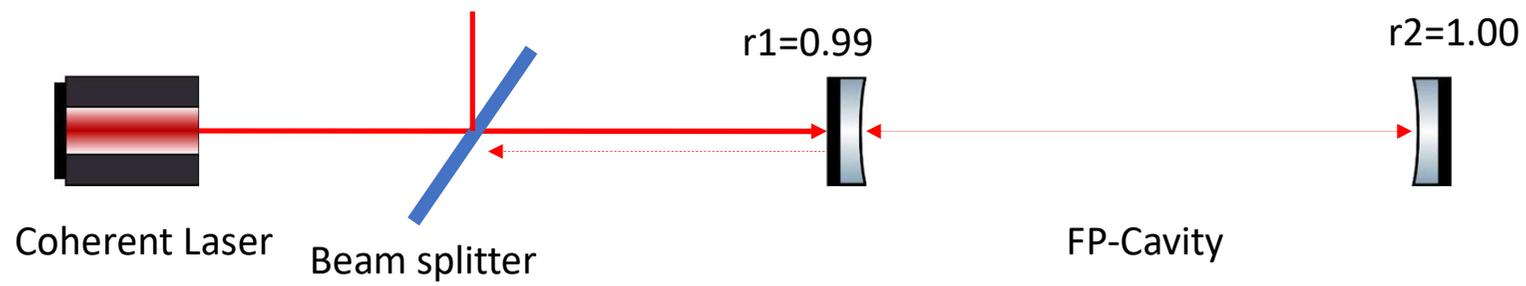
# Fabry-perot cavity

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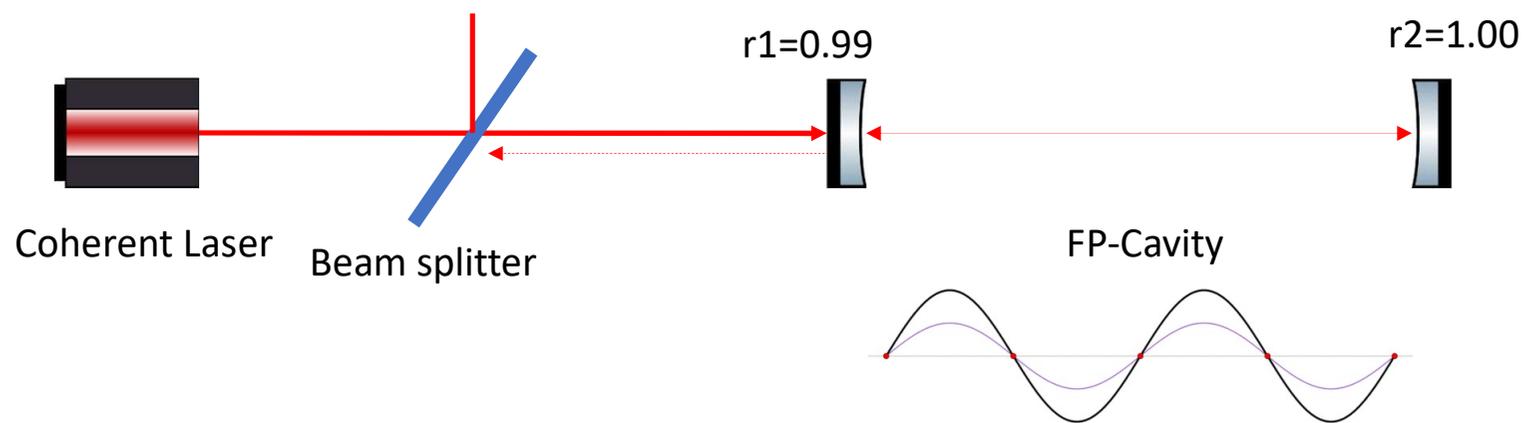
# Fabry-perot cavity

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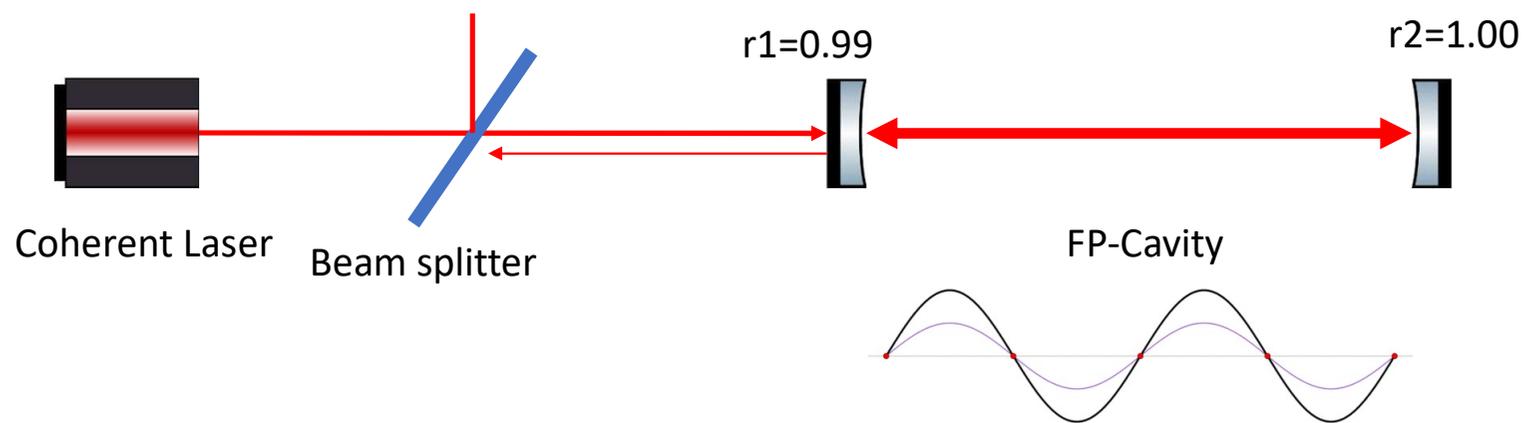
# Fabry-perot cavity

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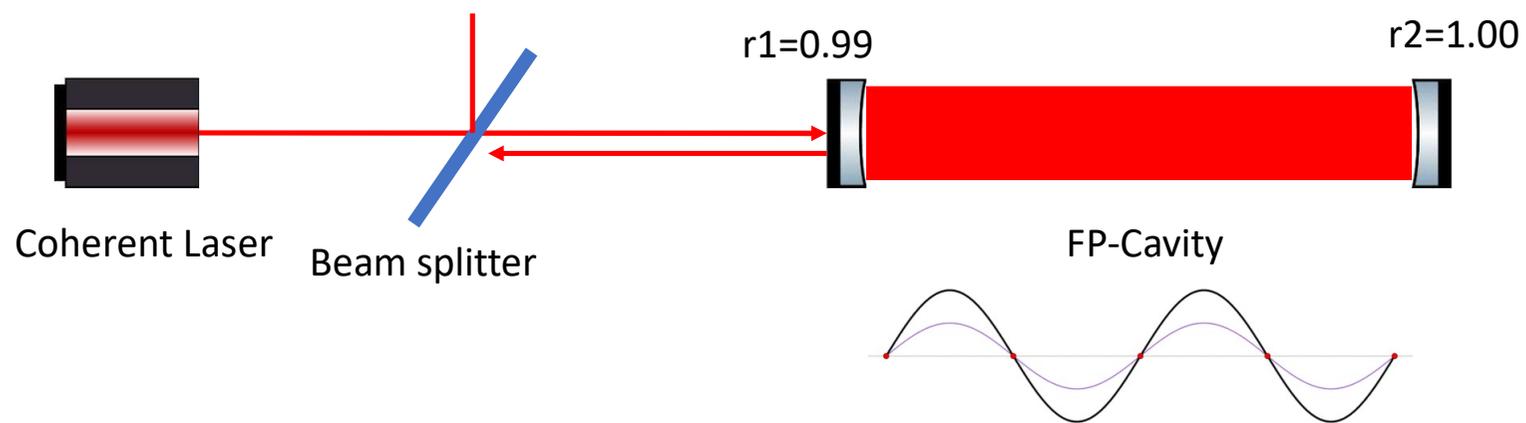
# Fabry-perot cavity

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# Fabry-perot cavity

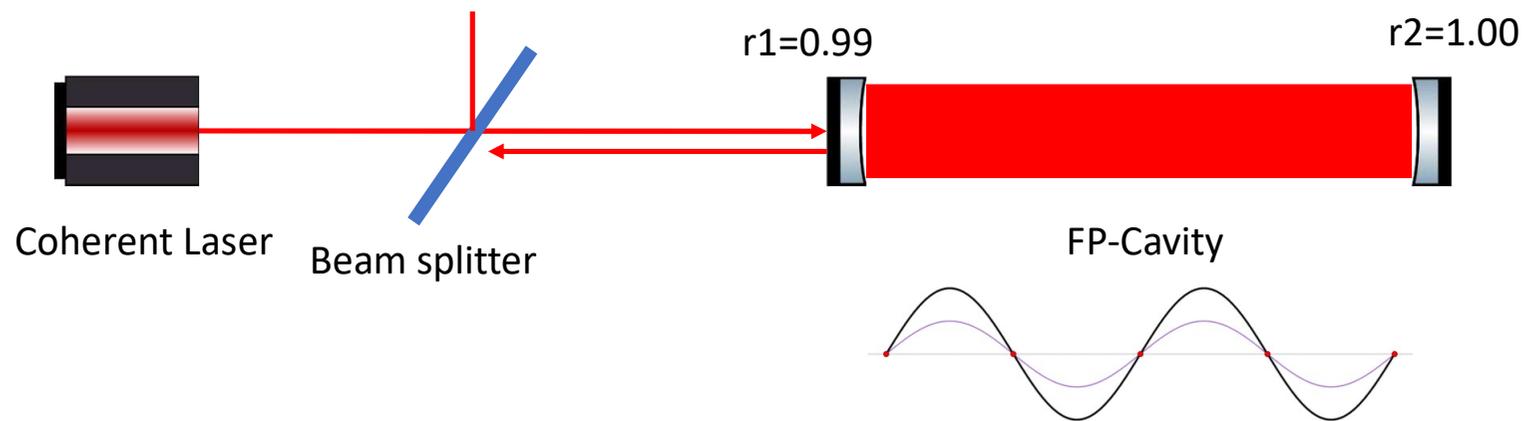
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# Fabry-perot cavity

---

Number of round trip  $> 250$

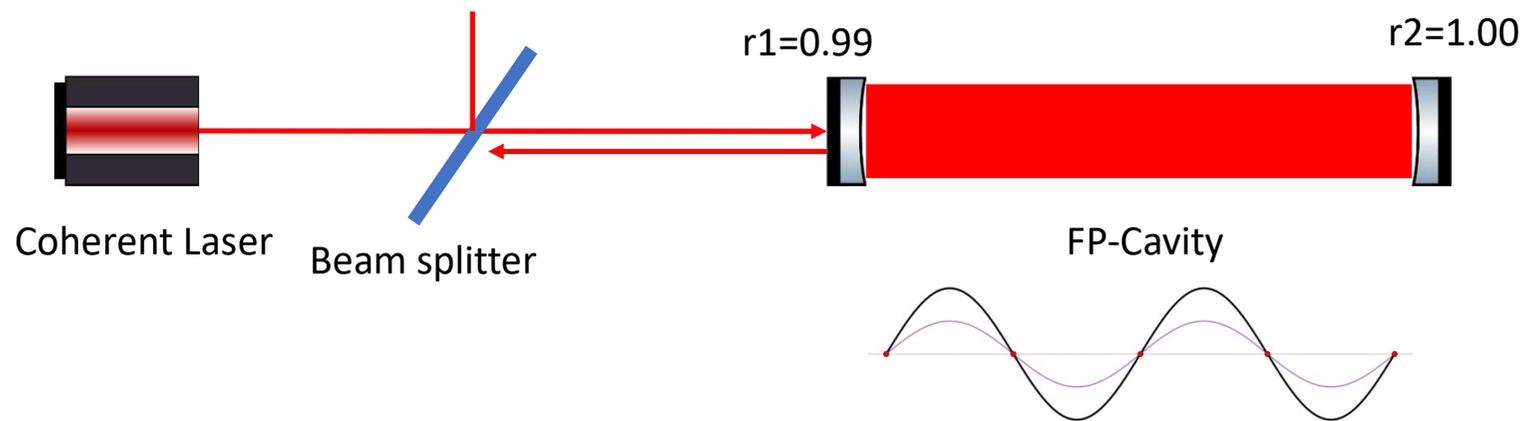


# Fabry-perot cavity

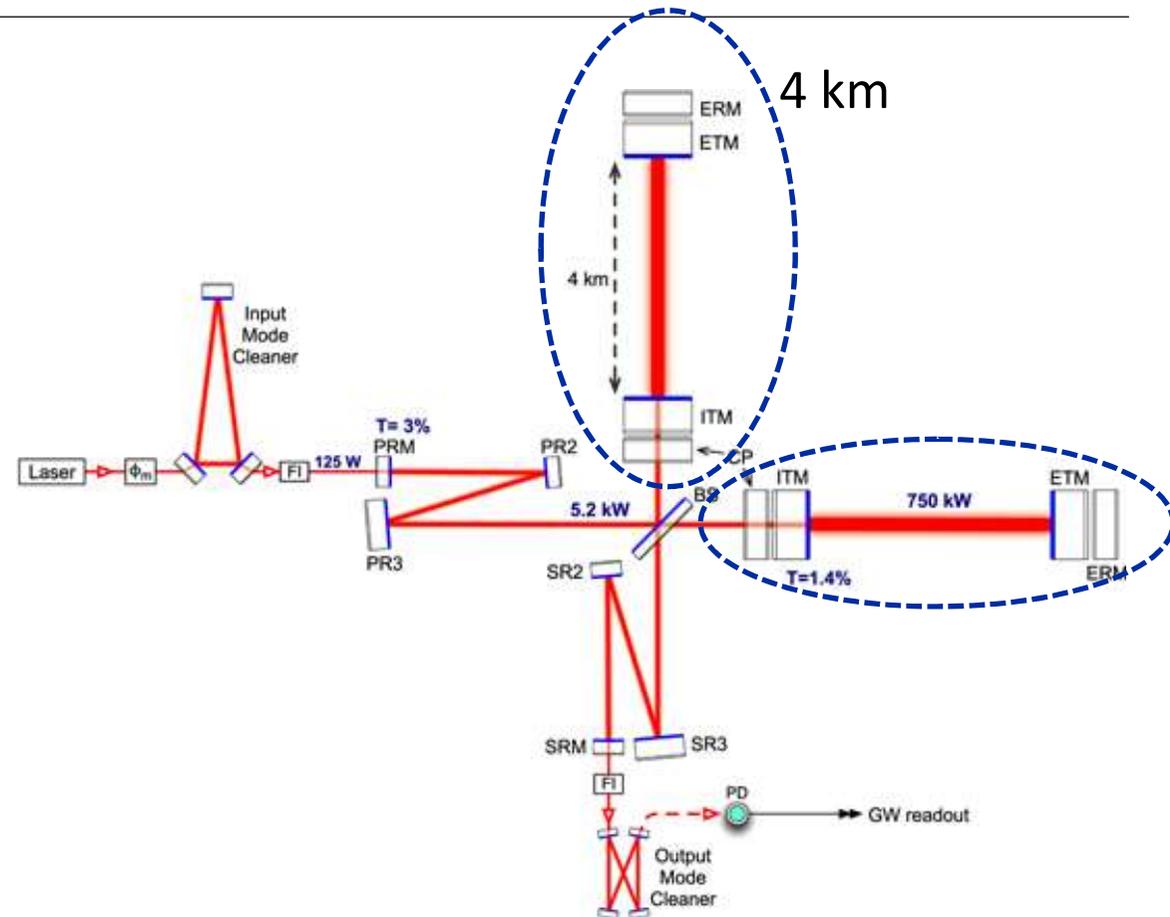
---

Number of round trip  $> 250$

4 km x 250  $\sim$  1000 km

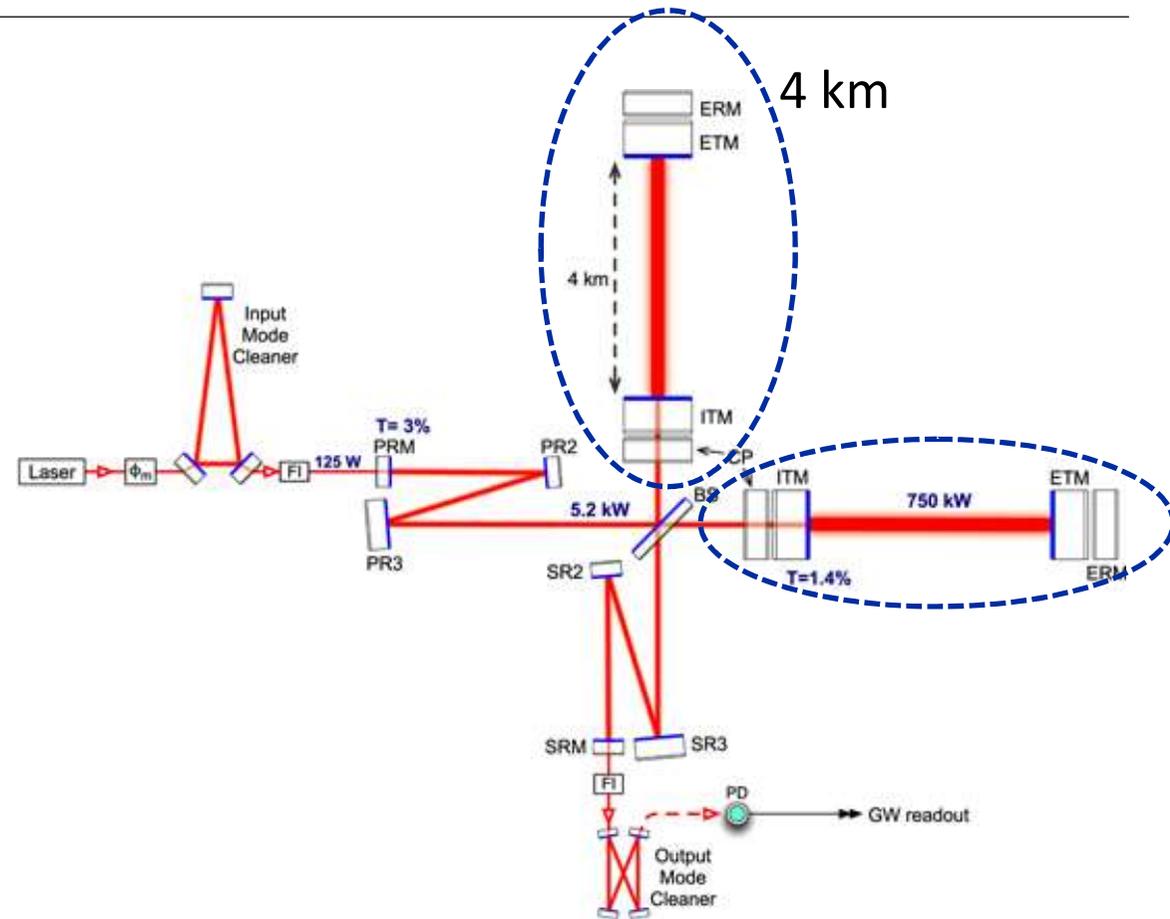


# LIGO interferometer



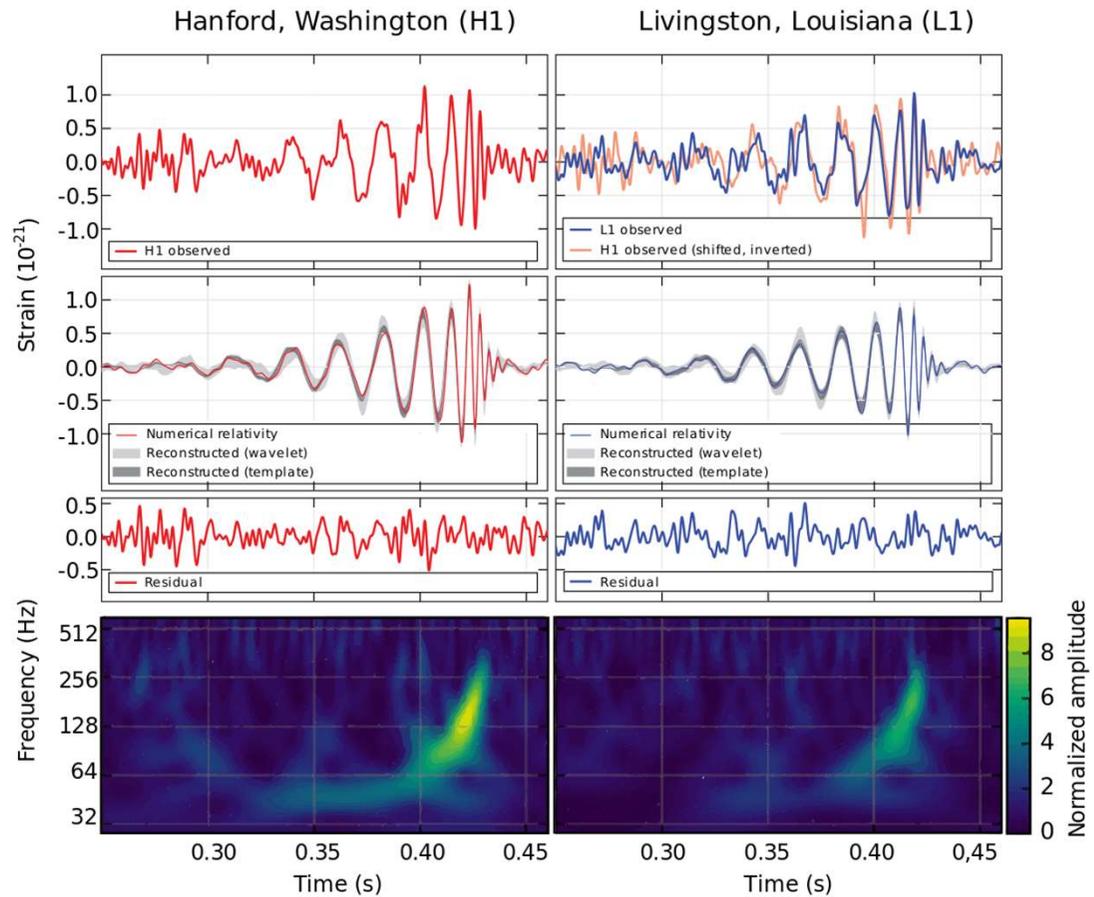
LIGO interferometer / Livingston

# LIGO interferometer



LIGO interferometer / Livingston

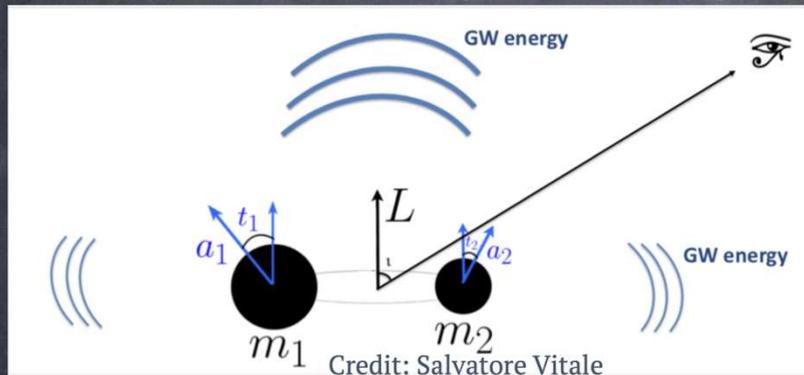
# First detection of gravitational wave



# Parameter estimation

## Compact Binary Coalescences (CBCs) parameters

- For CBCs, the astrophysical contribution is a waveform that depends on 17 parameters

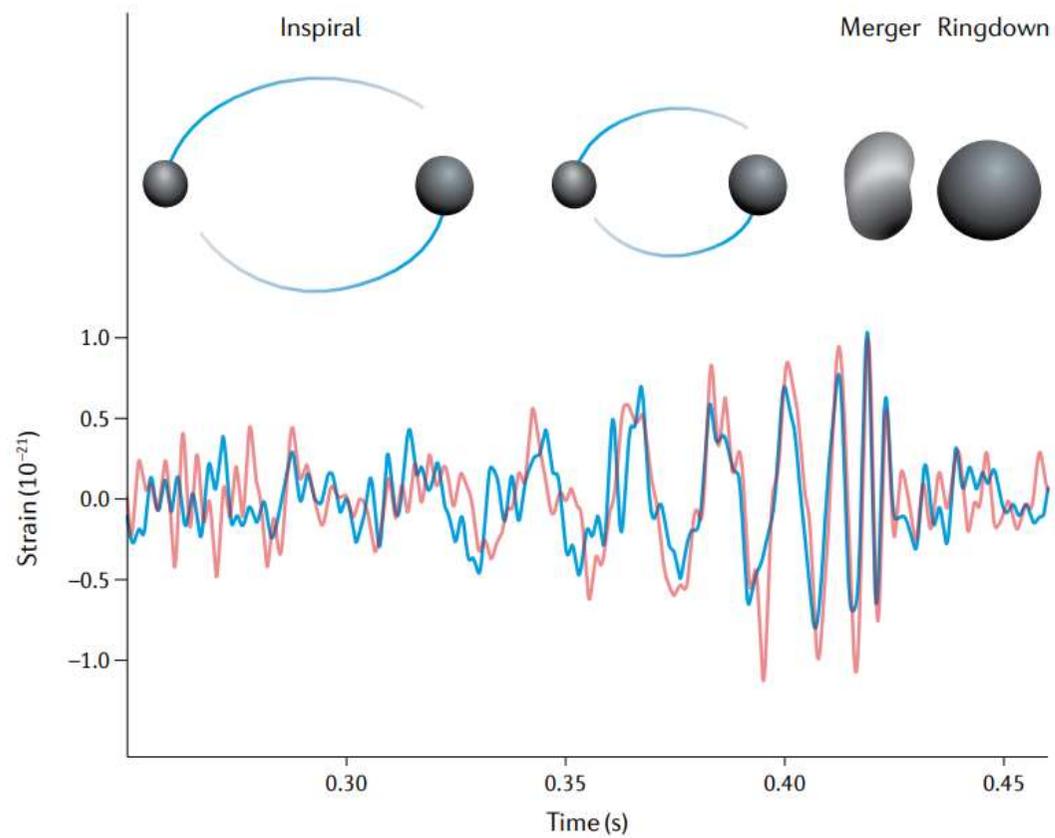


- **Intrinsic:** Component masses, Component spins
- **Extrinsic:** Sky-location, Distance, Inclination, Polarization, Reference phase, Time at coalescence

## Black Hole

- High mass
- High density(point source)
- No hair

# Inspiral–Merger–Ringdown

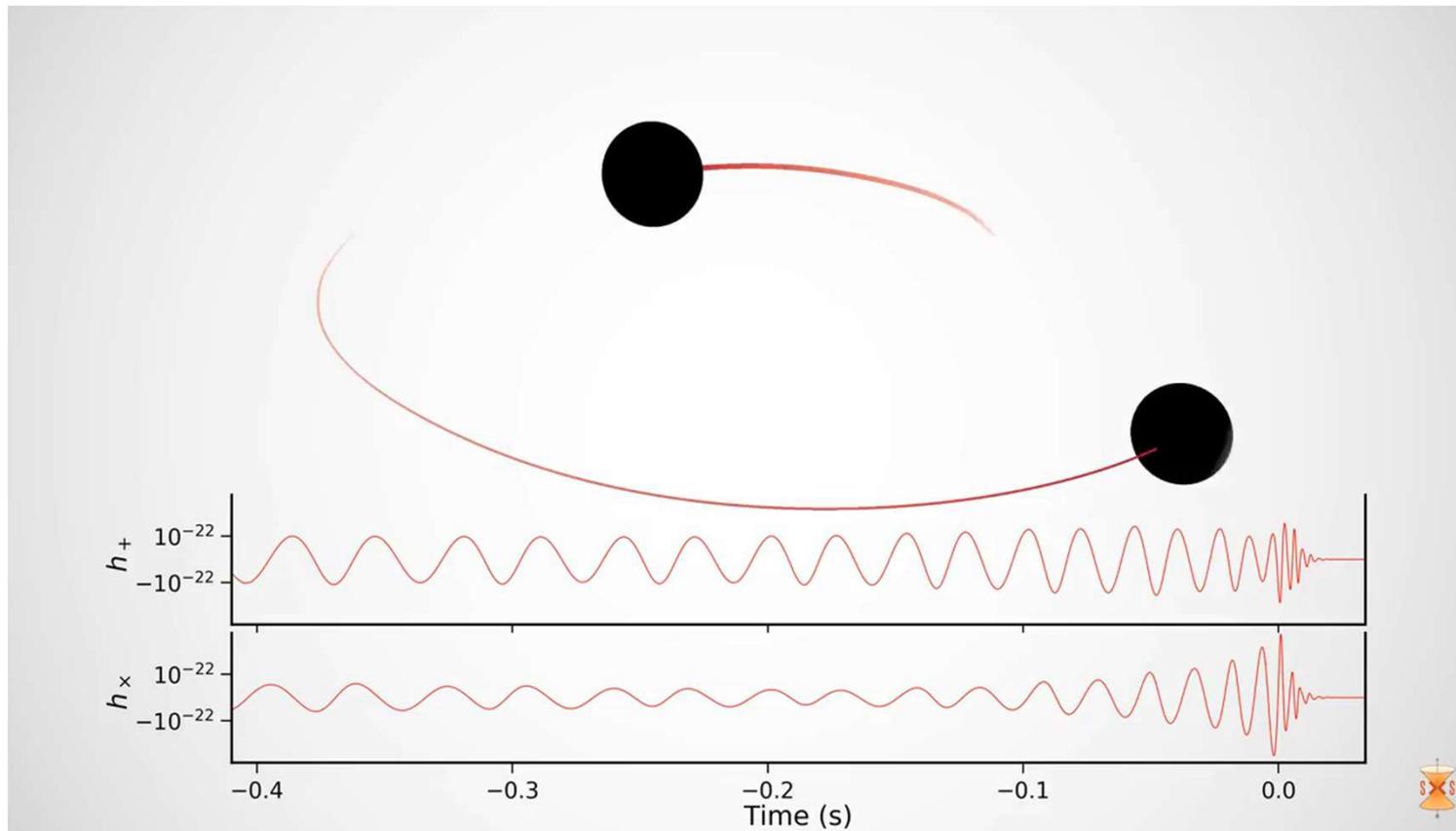


*Nature Reviews Physics* volume 3, pages344–366 (2021)

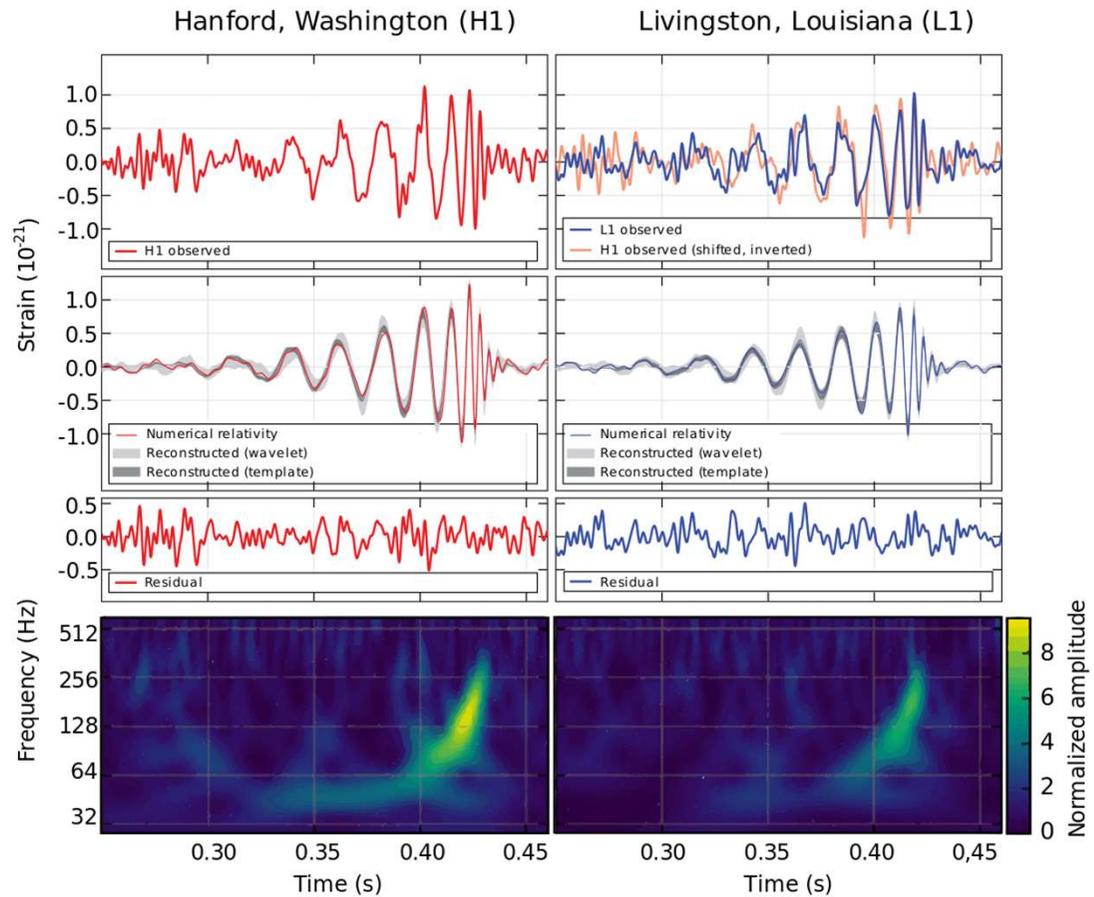
# GW170104

+ pol

x pol



# First detection of gravitational wave



# First detection of gravitational wave

Gravitational Waves Detected 100 Years After Prediction

News Release • February 11, 2016

The Nobel Prize in Physics 2017

Press Release

“for decisive contributi

Kip Thorne share the 2017 prize for their work at LIGO to



health

Life, But Better

Fitness

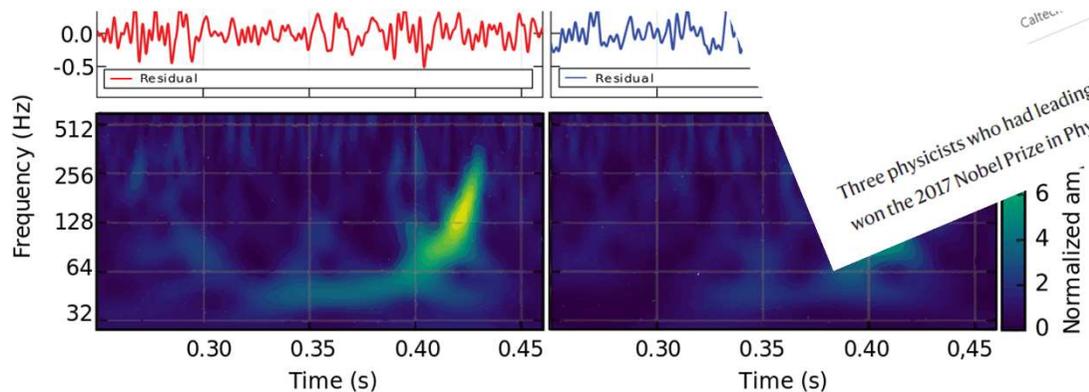
Food

Sleep

Mindfulness

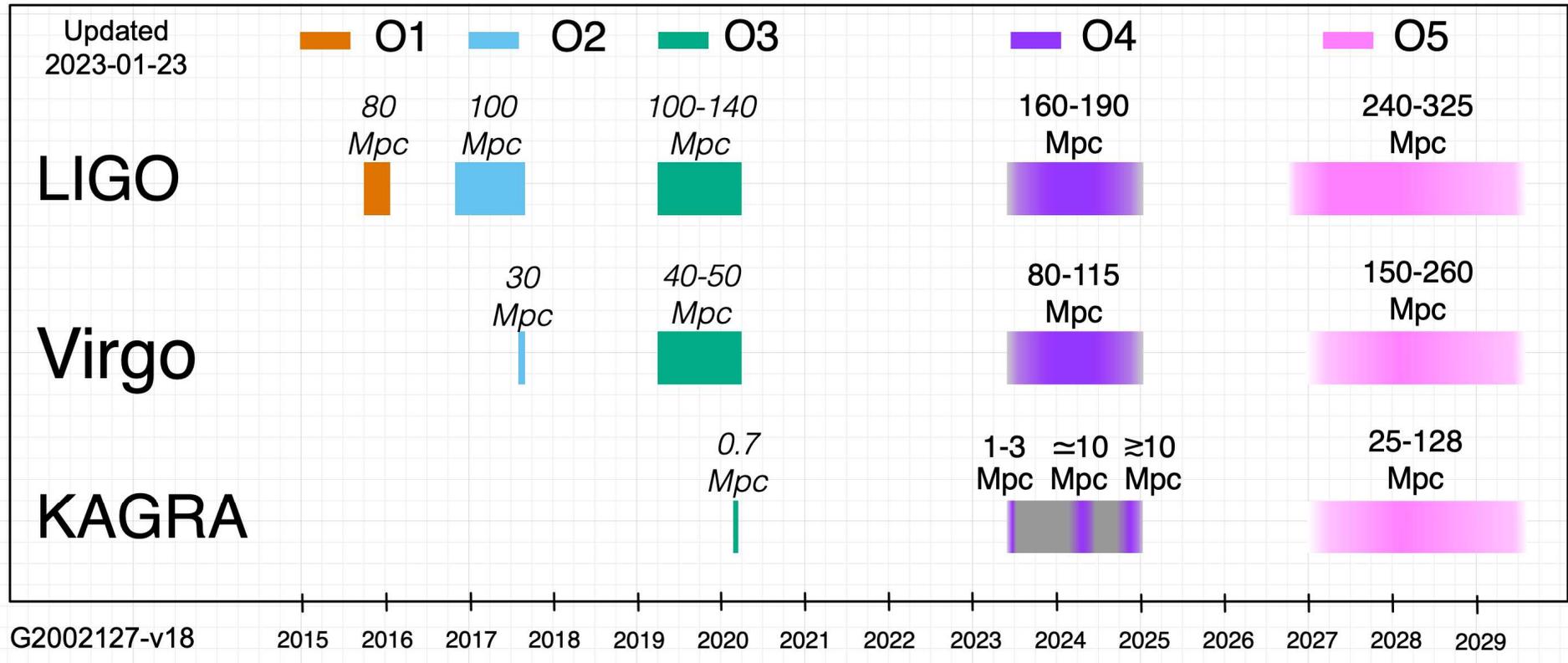
Relationships

## Nobel Prize in Physics goes to ‘black hole telescope’ trio



Three physicists who had leading roles in the first direct observation of gravitational waves won the 2017 Nobel Prize in Physics.

# LVK Observation plan



# BNS range

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- Binary-neutron-star range
- Common benchmark of sensitivity
- Made up of two 1.4 solar mass neutron stars
- Signal-to-noise ratio of 8

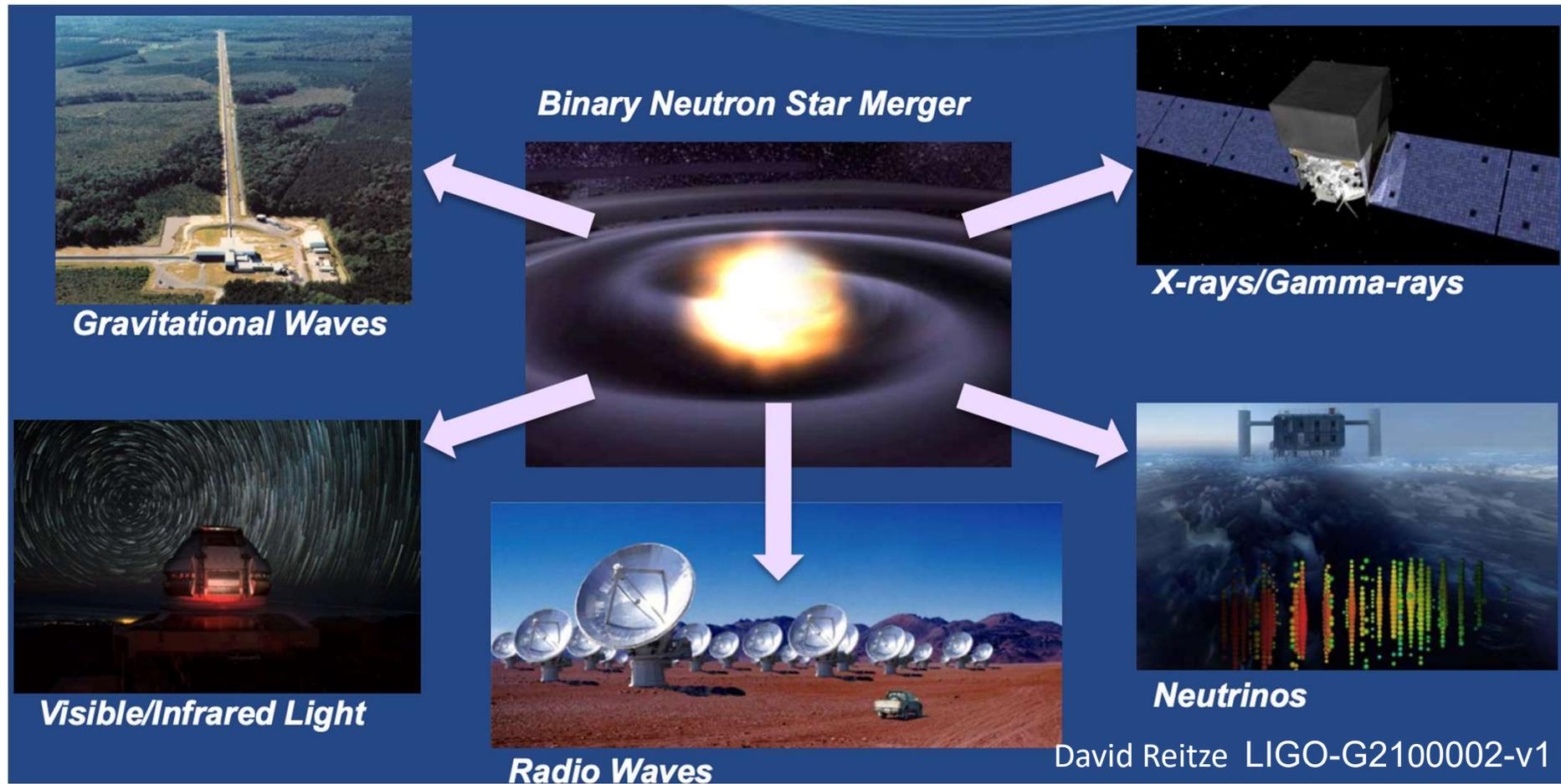


<https://svs.gsfc.nasa.gov/10543>

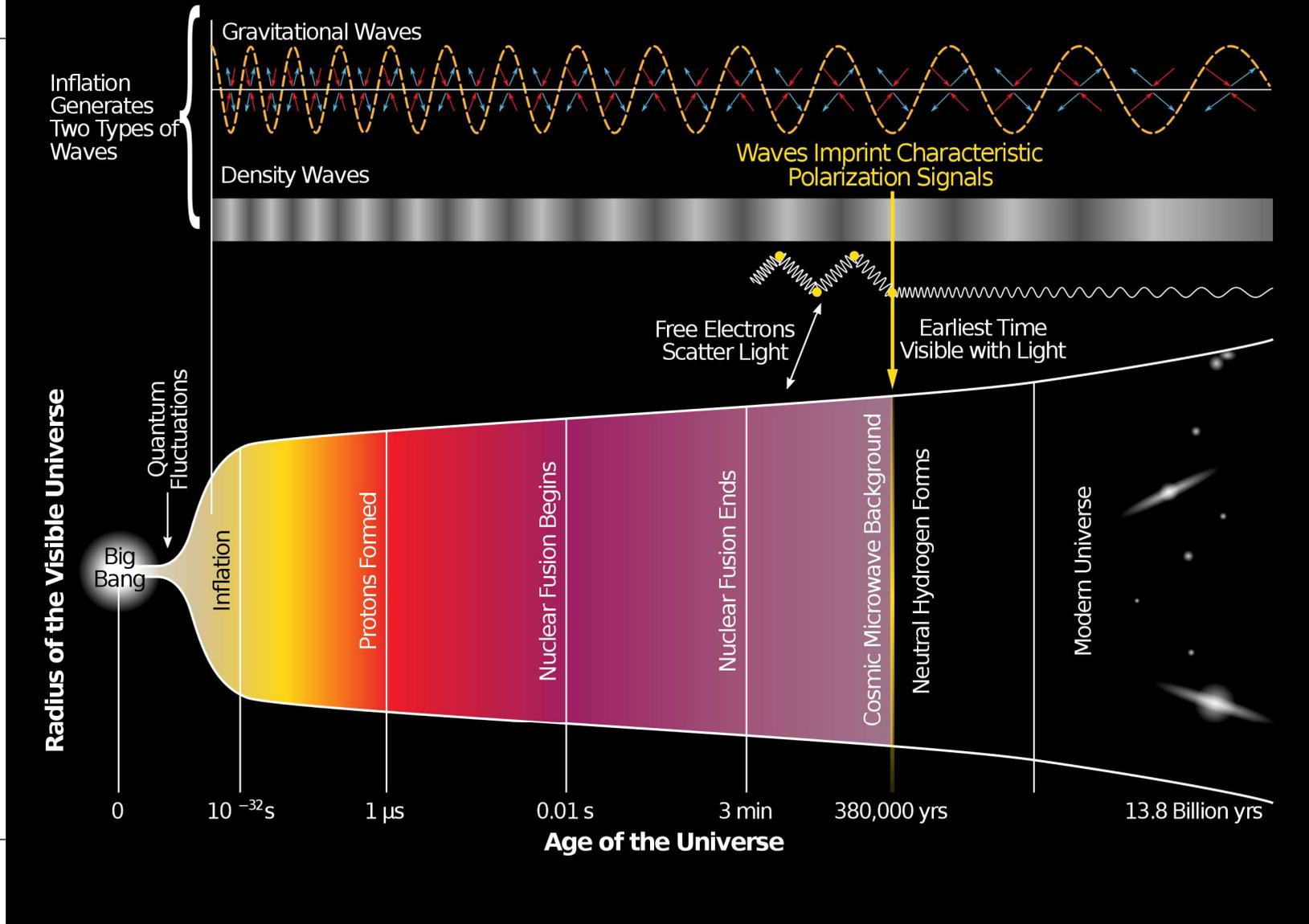
Maximum distance at which an event can be detected

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# Multi-messenger astronomy with gravitational waves

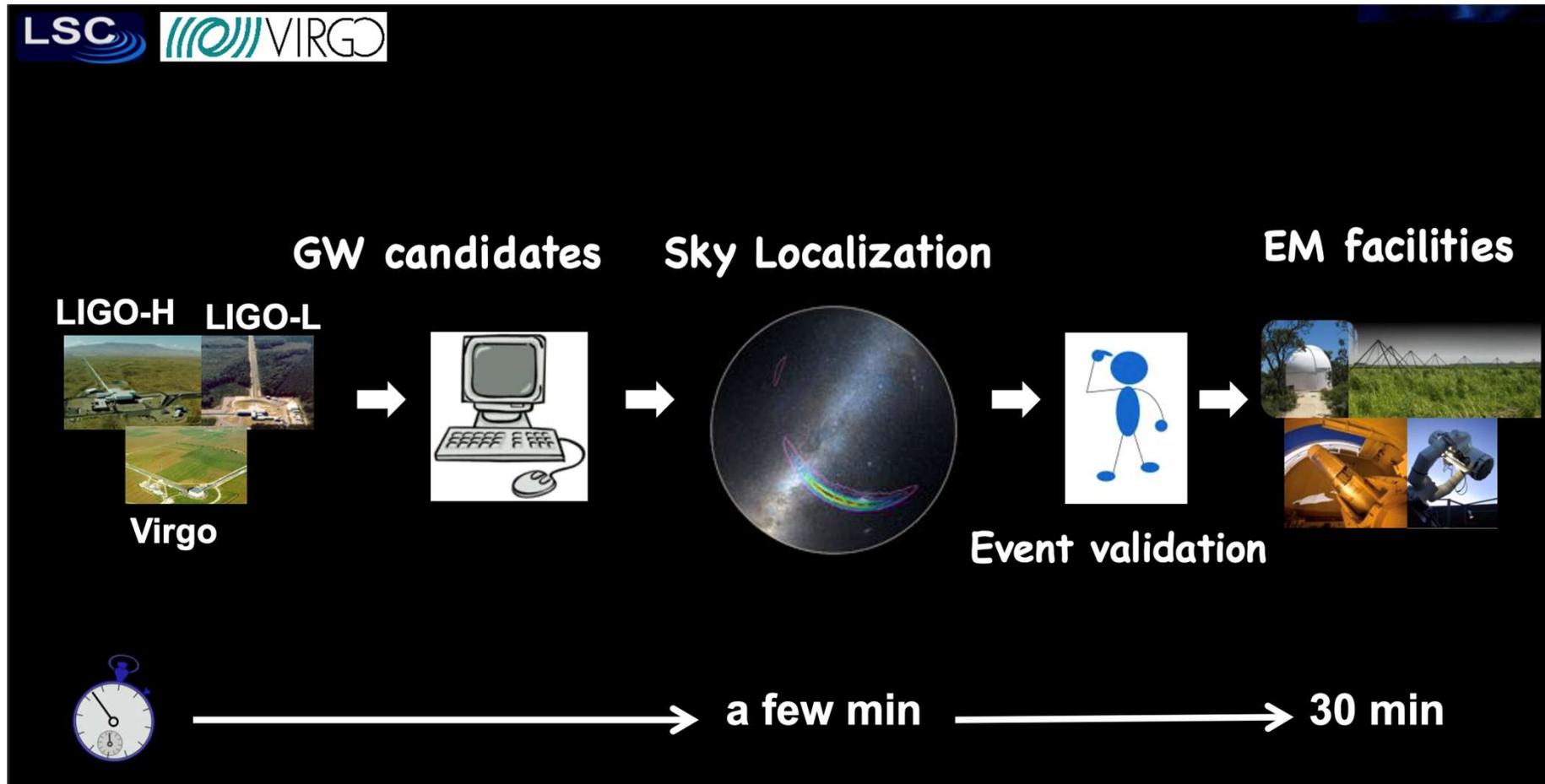


# History of the Universe

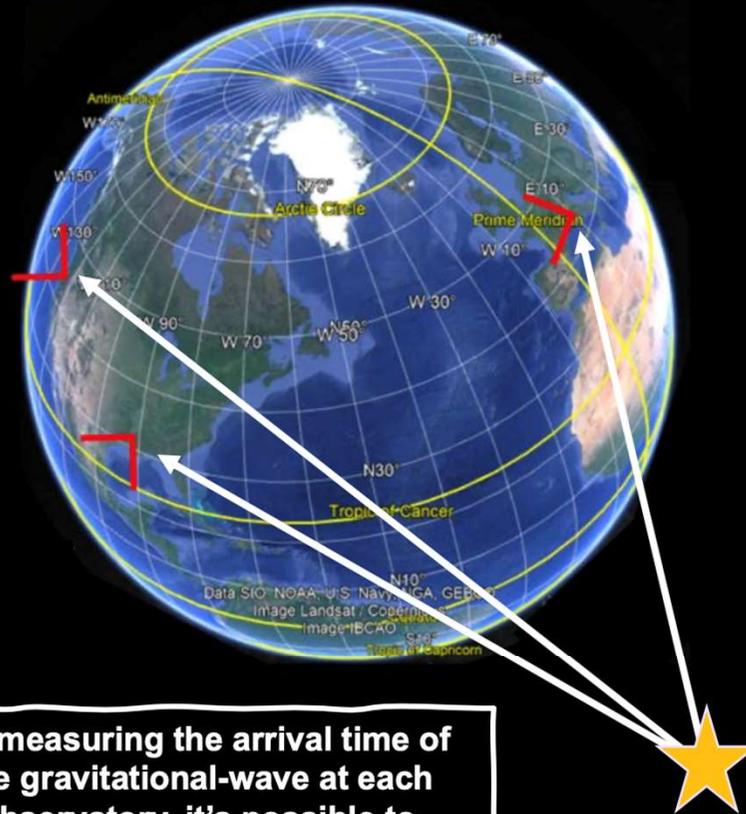


credit : BICEP2

# GW alert procedure



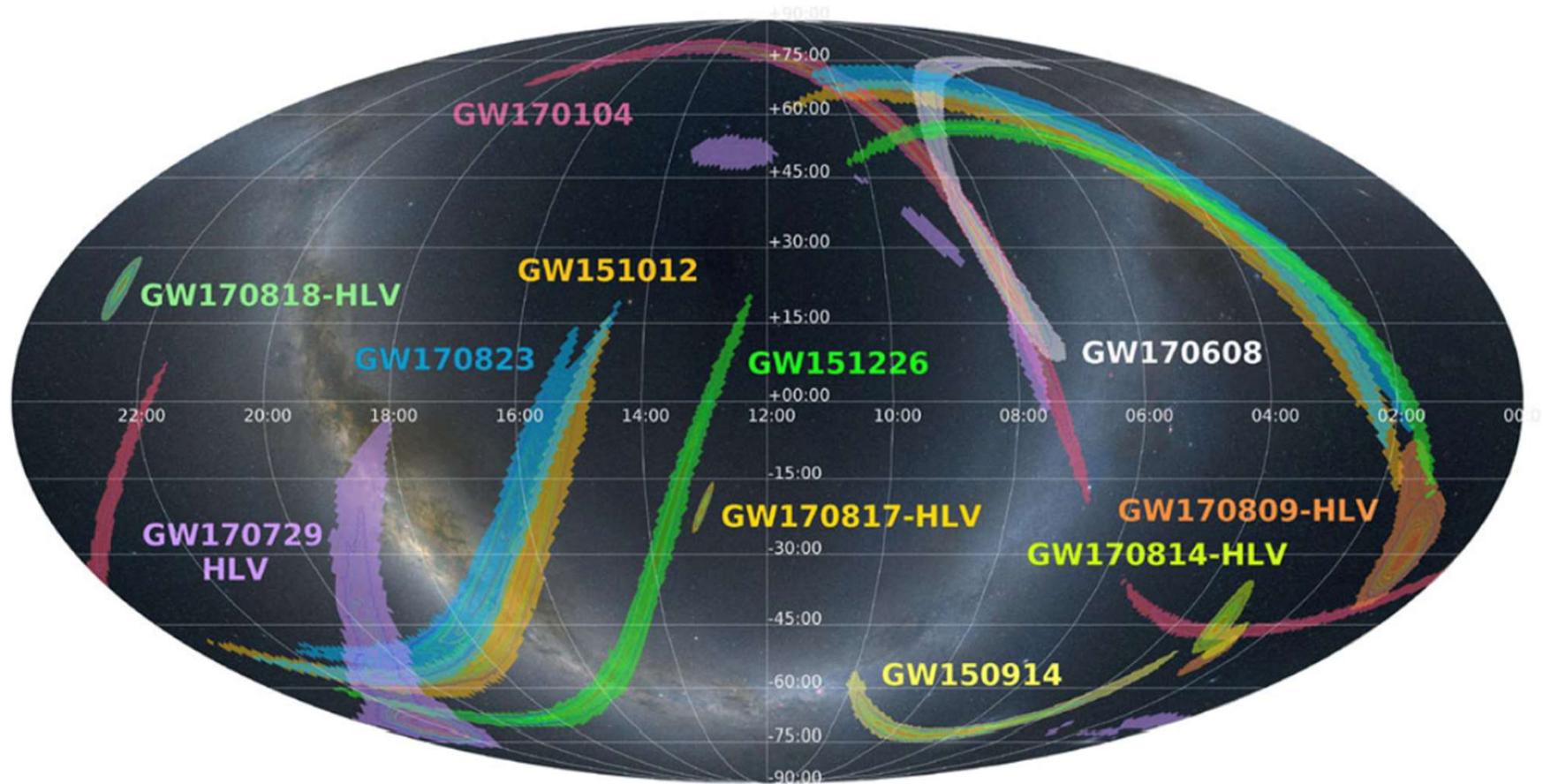
# Localizing Gravitational-wave Events



By measuring the arrival time of the gravitational-wave at each observatory, it's possible to identify its location on the sky

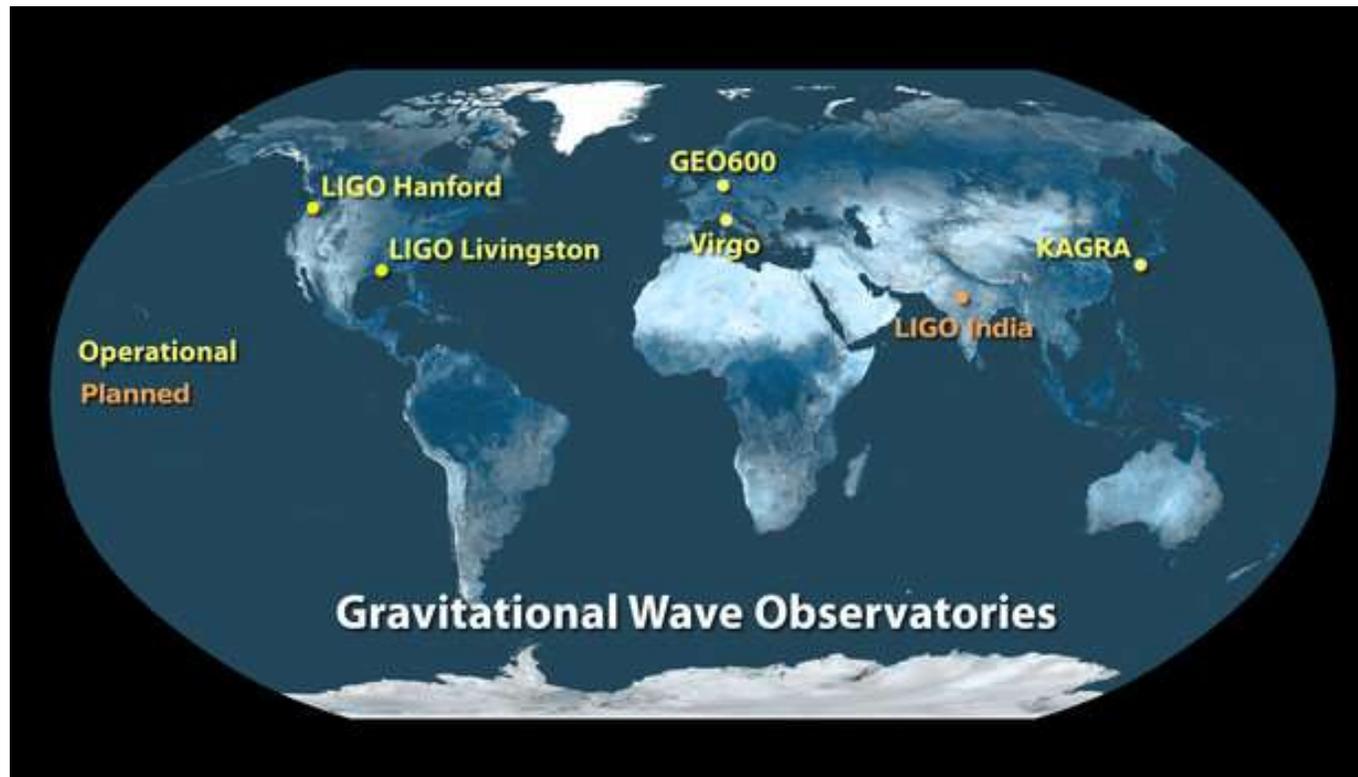
A single GW observatory is mostly insensitive to the sky location; we want two and preferably three or more observatories

# Sky localization



# Gravitational wave observatories

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# First multi-messenger detection

Binary neutron star merger

Gamma ray burst detection with Fermi-detector

Kilonova detection using telescope

## GW170817

### Binary neutron star merger

A LIGO / Virgo gravitational wave detection with associated electromagnetic events observed by over 70 observatories.



Distance  
130 million light years

Discovered  
17 August 2017

Type  
Neutron star merger



12:41:04 UTC

A gravitational wave from a binary neutron star merger is detected.

#### gravitational wave signal

Two neutron stars, each the size of a city but with at least the mass of the sun, collided with each other.

#### gamma ray burst

A short gamma ray burst is an intense beam of gamma ray radiation which is produced just after the merger.

+ 2 seconds

A gamma ray burst is detected.



GW170817 allows us to measure the expansion rate of the universe directly using gravitational waves for the first time.



Detecting gravitational waves from a neutron star merger allows us to find out more about the structure of these unusual objects.



This multimessenger event provides confirmation that neutron star mergers can produce short gamma ray bursts

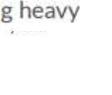


The observation of a kilonova allowed us to show that neutron star mergers could be responsible for the production of most of the heavy elements, like gold, in the universe.

neutron-rich ejecta creates a glowing kilonova producing heavy



Observing both electromagnetic and gravitational waves from the event provides compelling evidence that gravitational waves travel at the same speed as light.



+10 hours 52 minutes

A new bright source of optical light is detected in a galaxy called NGC 4993, in the constellation of Hydra.



+100 days  
Radio emission detected.

# Radioactively powered transients

Relativistic astrophysics

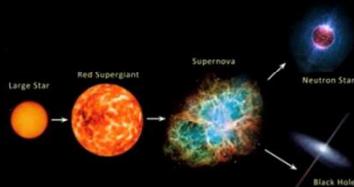


Nucleosynthesis and enrichment of the Universe

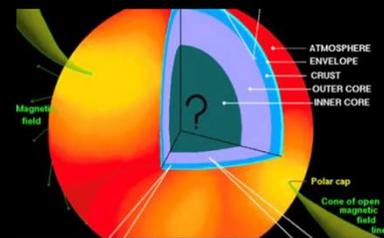


GW170817

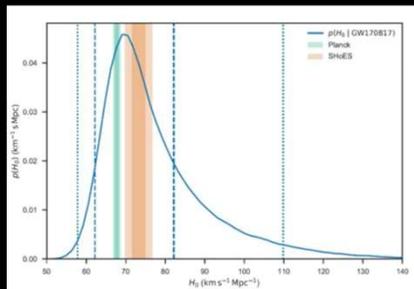
Compact object formation and evolution



Nuclear matter physics

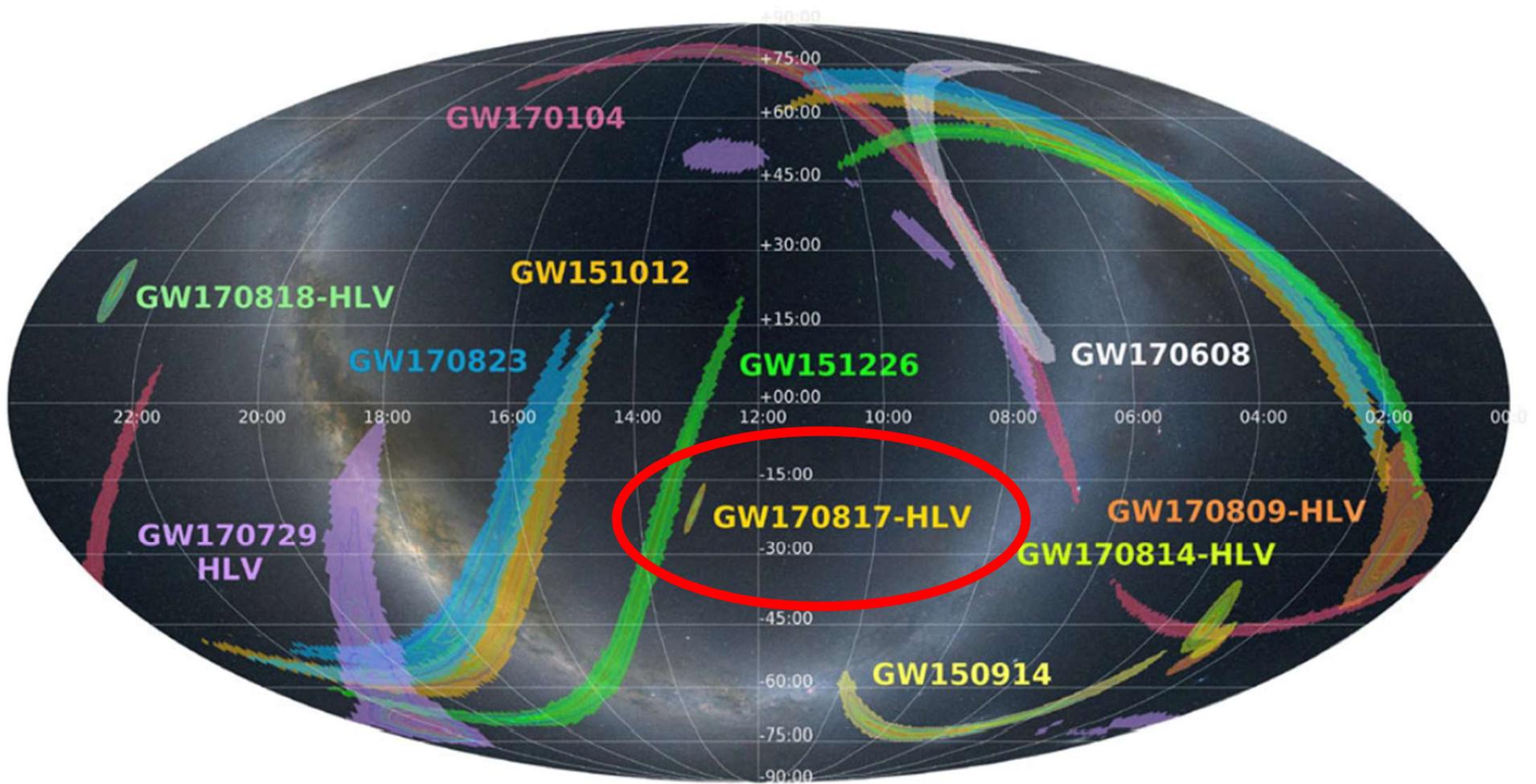


Cosmology

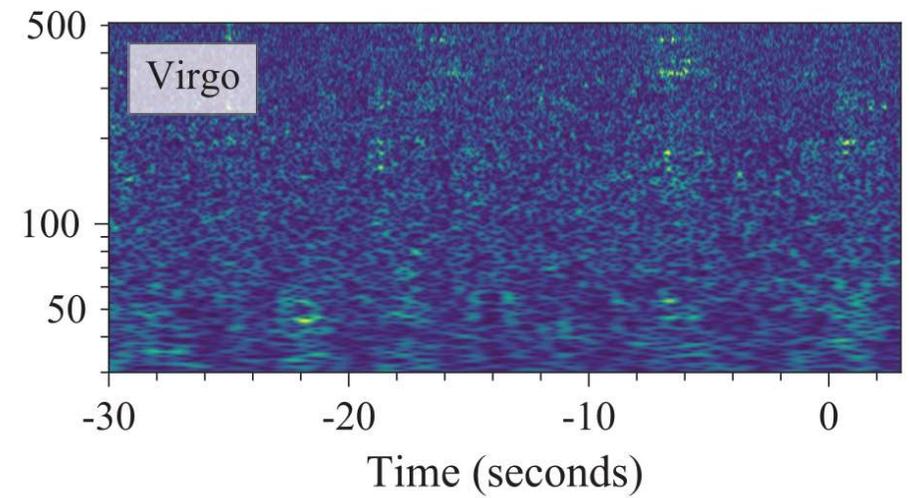
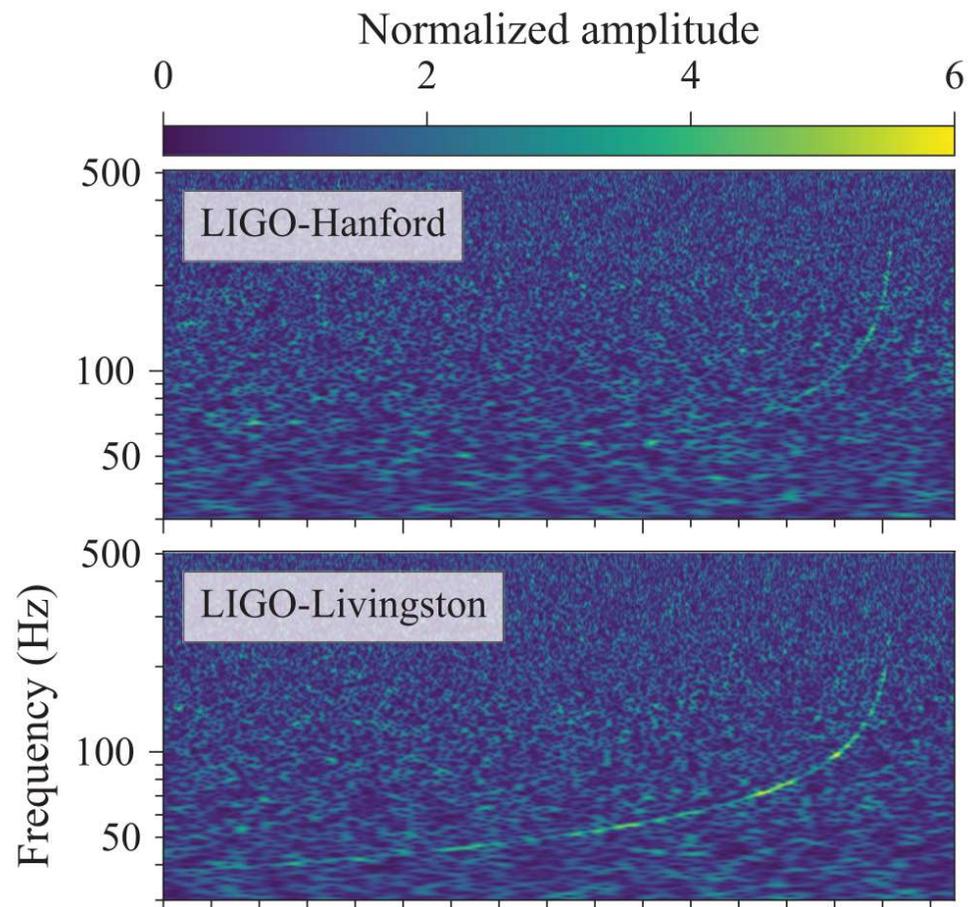


Yokohama GRB 2019  
Marci Branchesi

# Sky localization

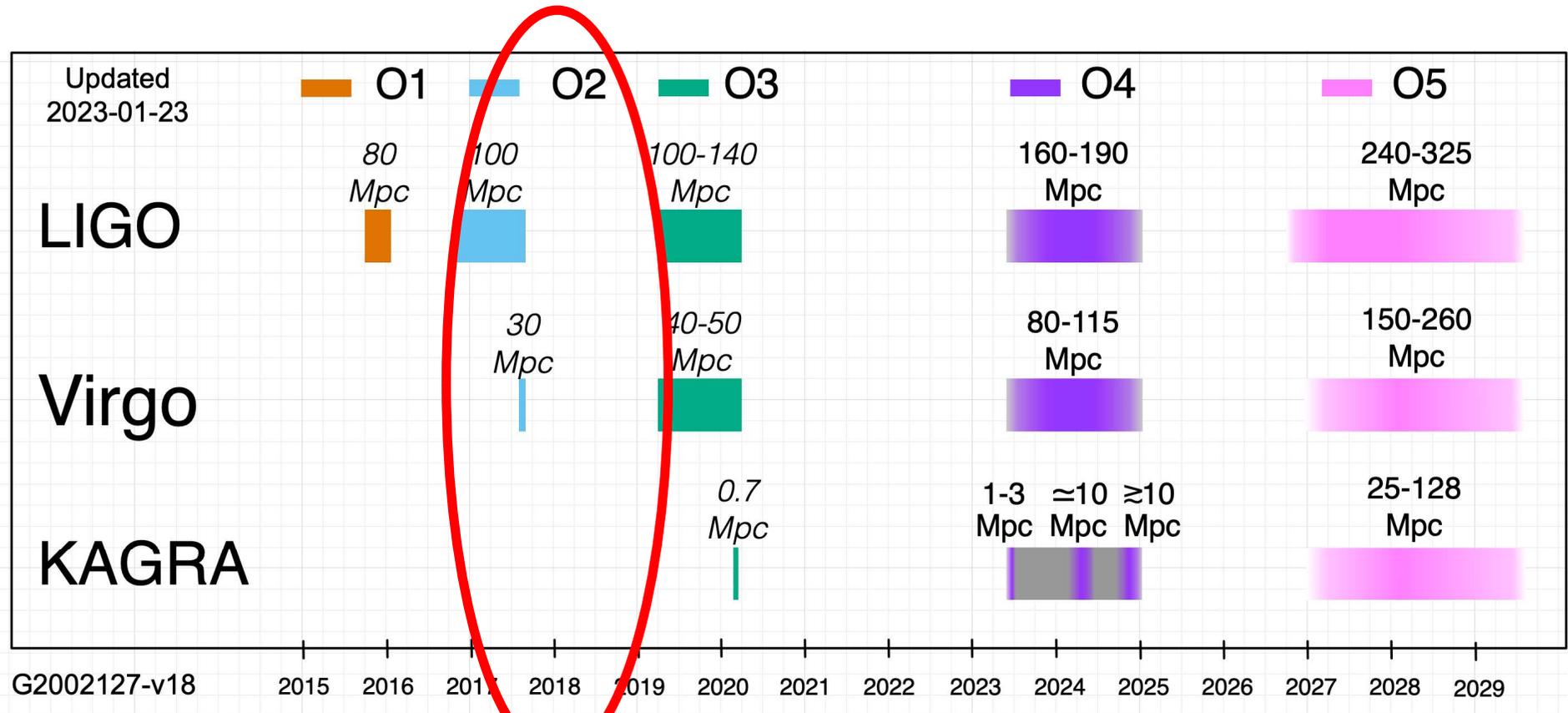


# GW170817



No Signal at VIRGO ???

# LVK Observation plan



# LIGO-VIRGO joint observation

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## VIRGO JOINS LIGO FOR THE O2 DATA-TAKING PERIOD

Warning: Use of undefined constant multiple - assumed 'multiple' (this will throw an error in a future version of PHP) [content/themes/](#)

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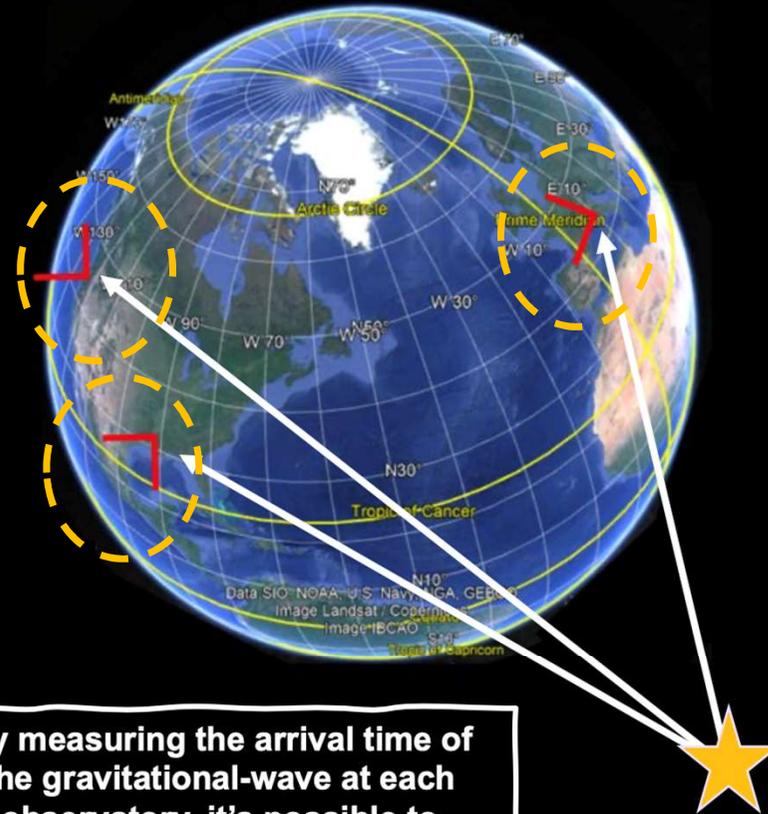
 By Massimiliano Razzano  August 1, 2017  News, Press Releases

### VIRGO joins LIGO for the “Observation Run 2” (O2) data-taking period

Today, **Tuesday August 1st 2017**, the VIRGO detector based in Europe has officially joined “Observation Run 2” (O2) alongside the two LIGO detectors based in the United States.

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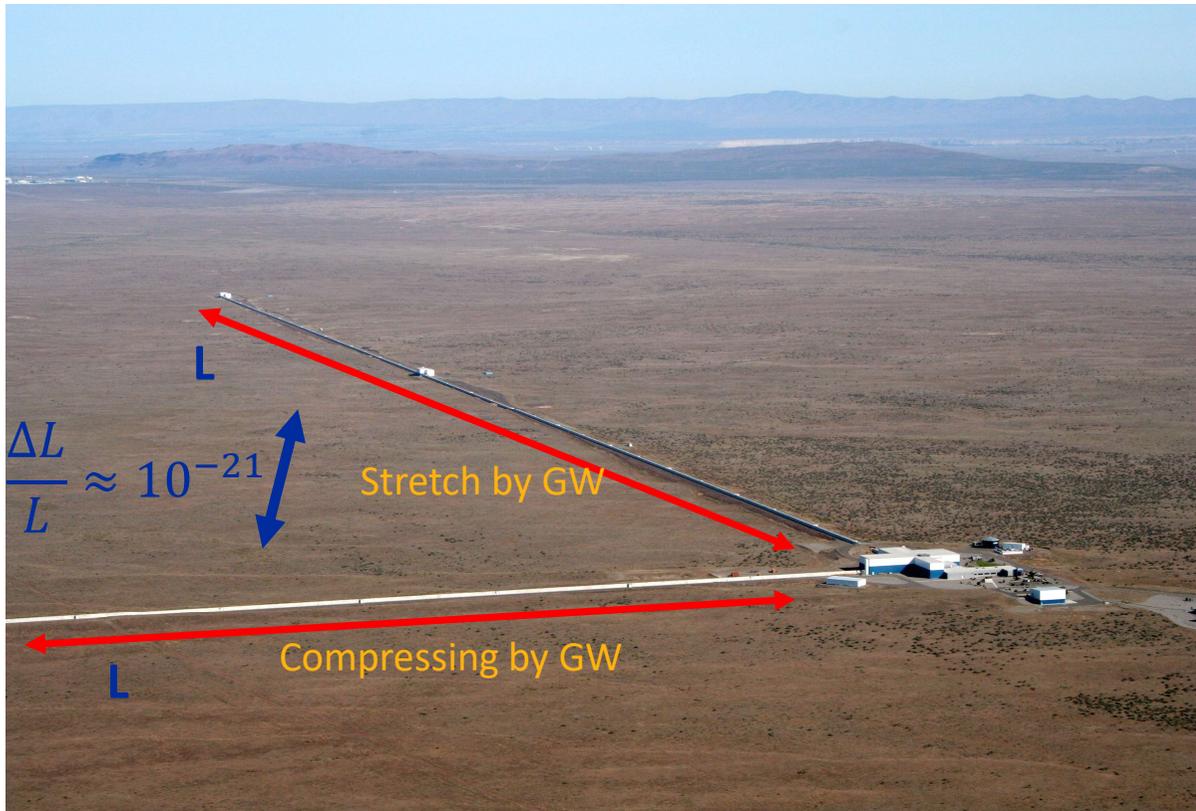
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# Strain sensitivity

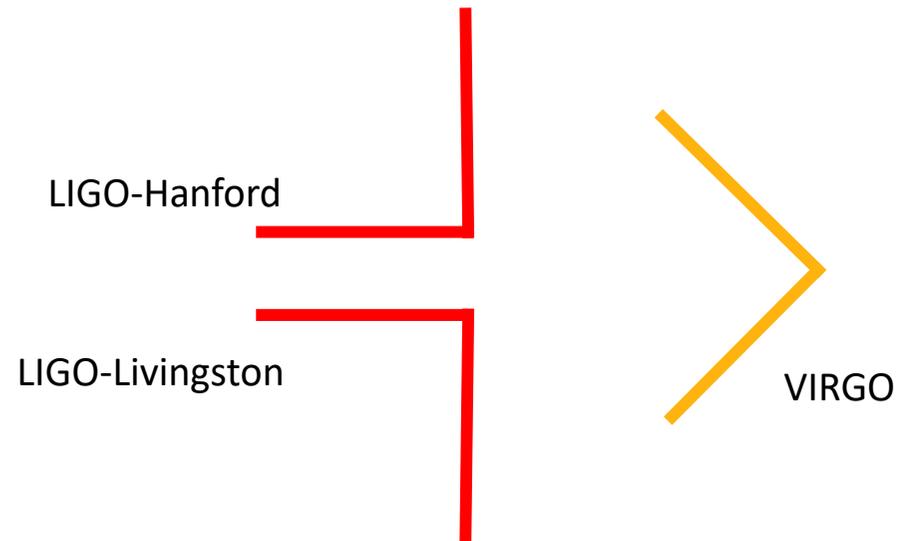


Minimum sensitivity

$$\frac{\Delta L}{L} \approx 10^{-21}$$

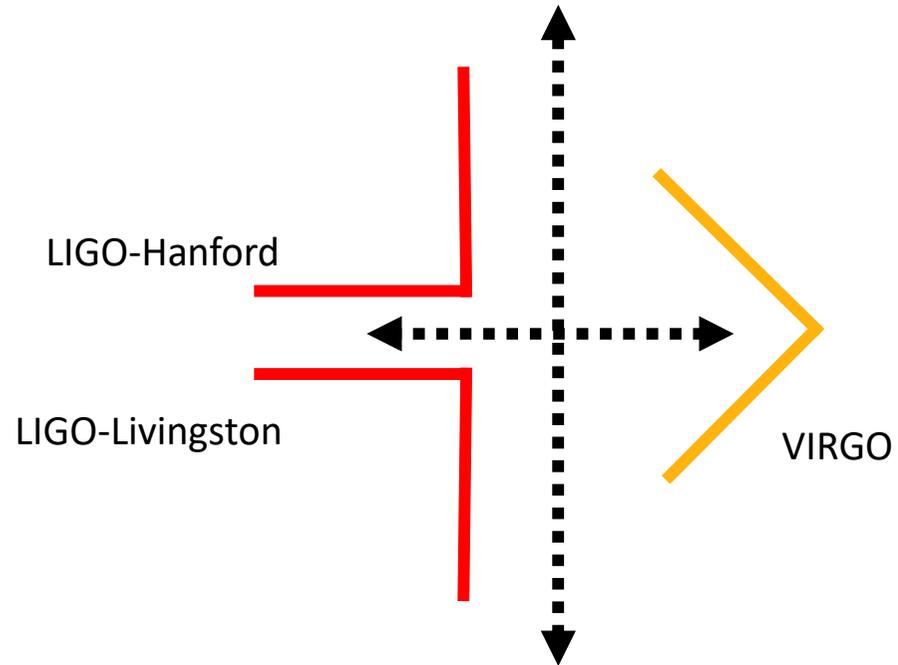
# Polarization of gravitational wave

---



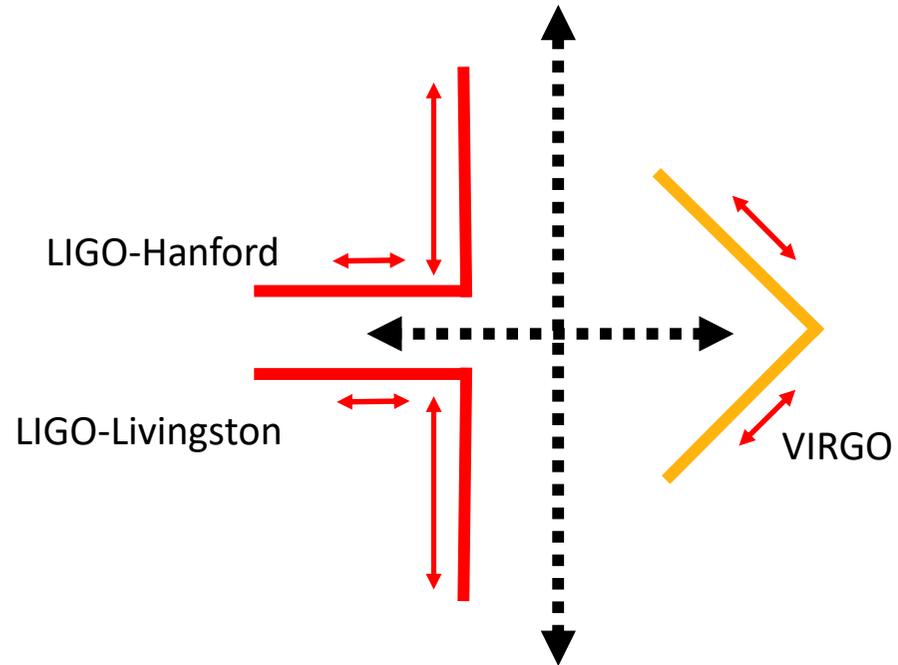
# Polarization of gravitational wave

---



# Polarization of gravitational wave

---



# Localizing Gravitational-wave Events



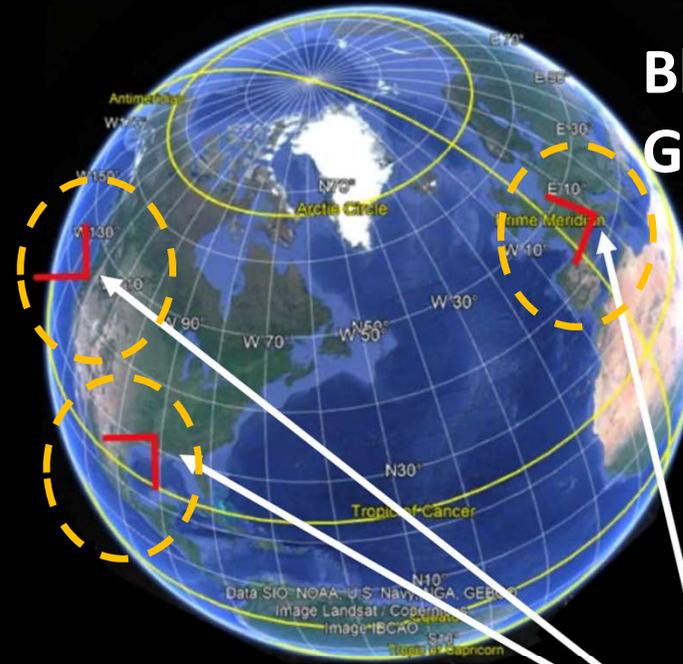
Virgo, Cascina, Italy



LIGO, Livingston, LA



LIGO, Hanford, WA



Blind spot of  
GW170817

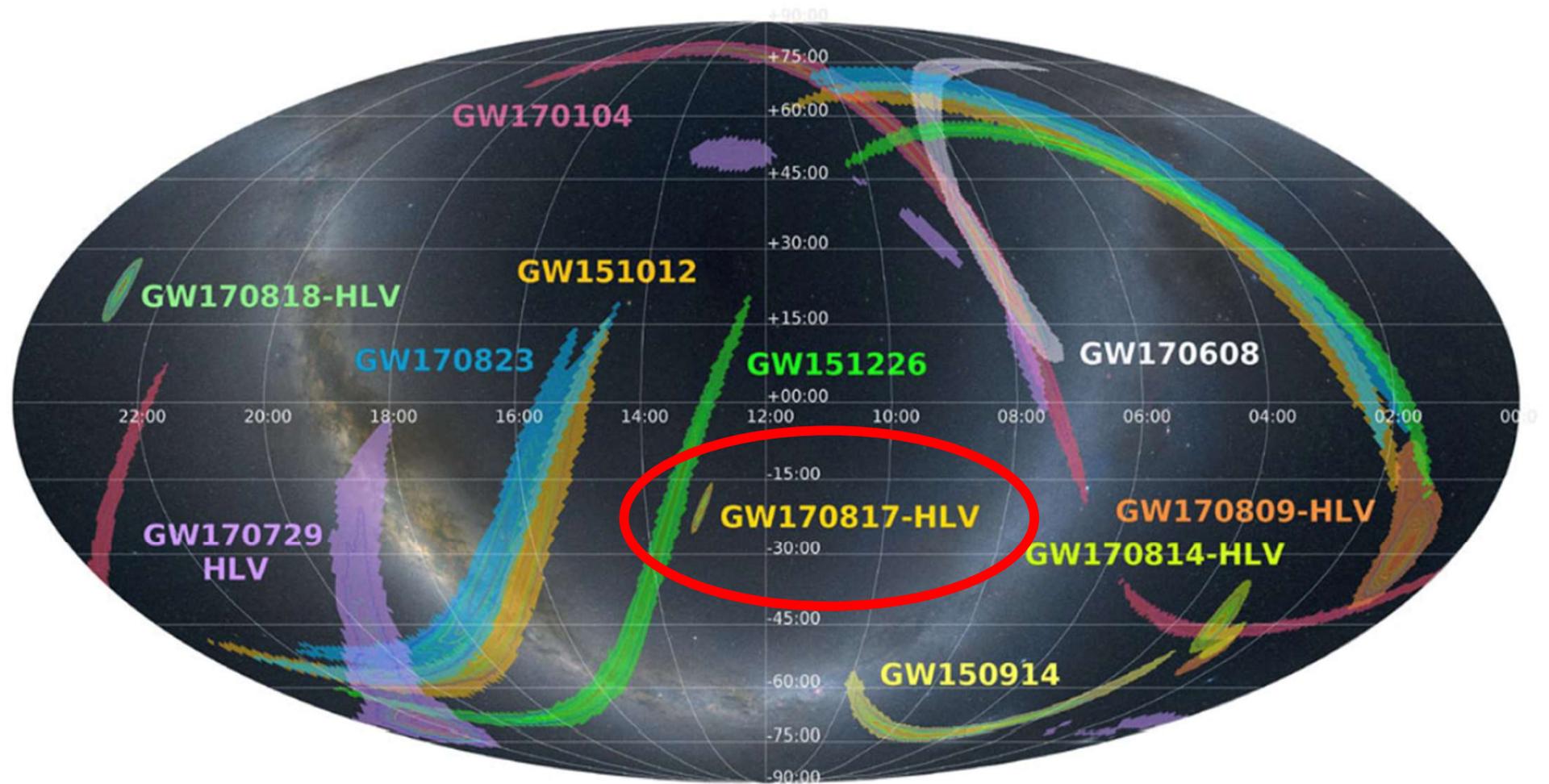
By measuring the arrival time of the gravitational-wave at each observatory, it's possible to identify its location on the sky

A single GW observatory is mostly insensitive to the sky location; we want two and preferably three or more observatories



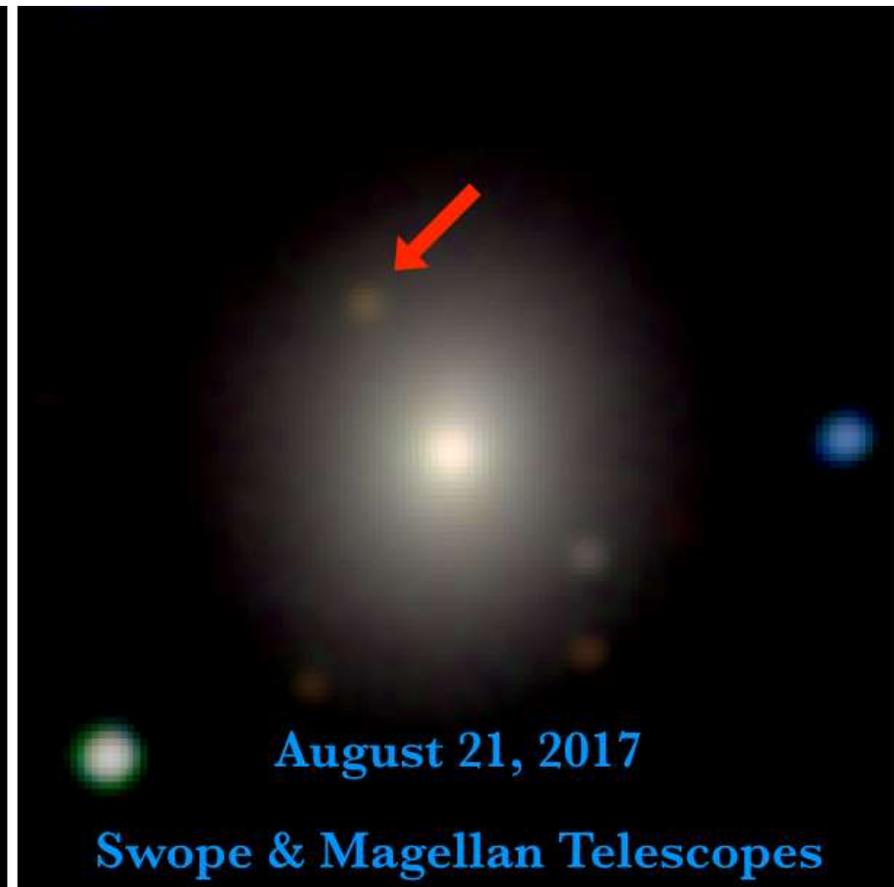
Tokushima GRB 2019  
Marci Branchesi

# Sky localization

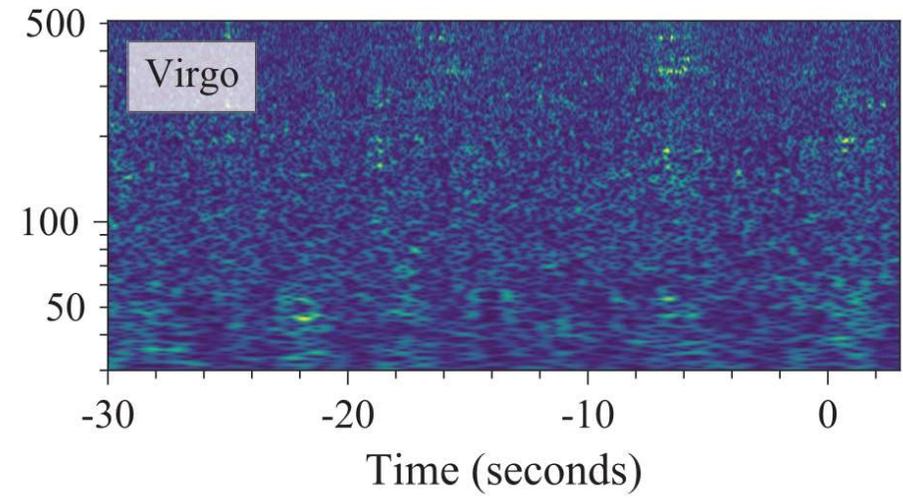
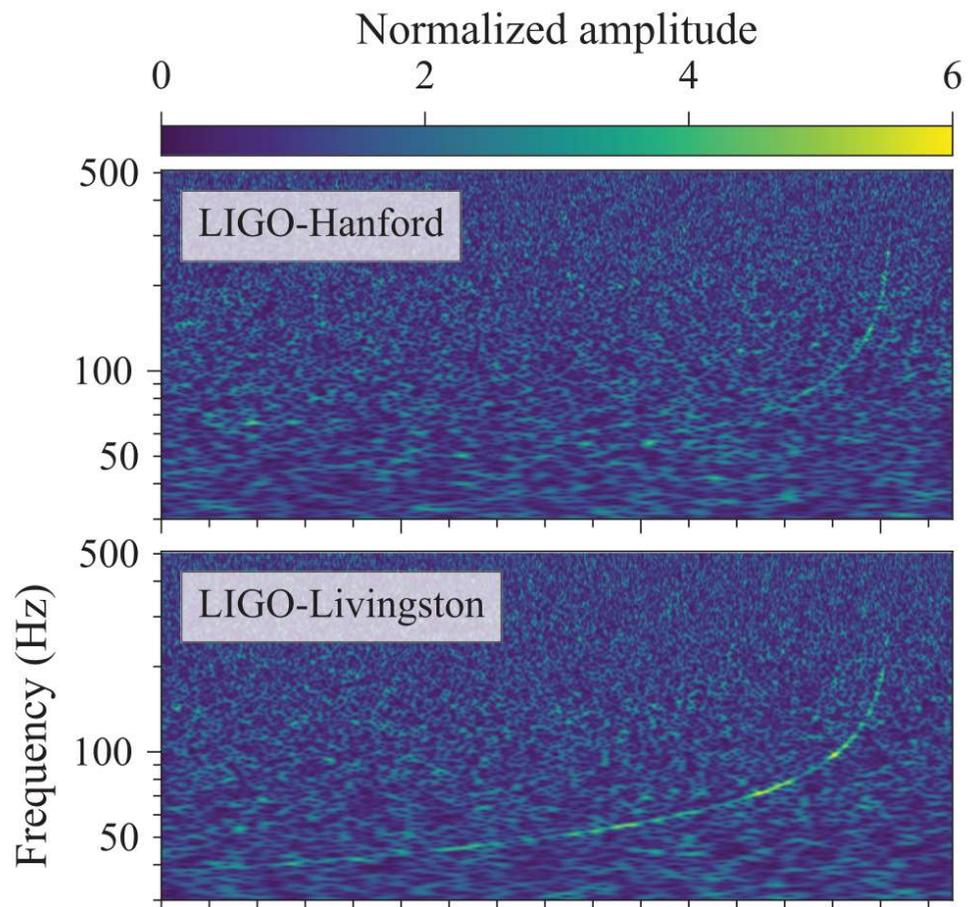


# GW170817

---



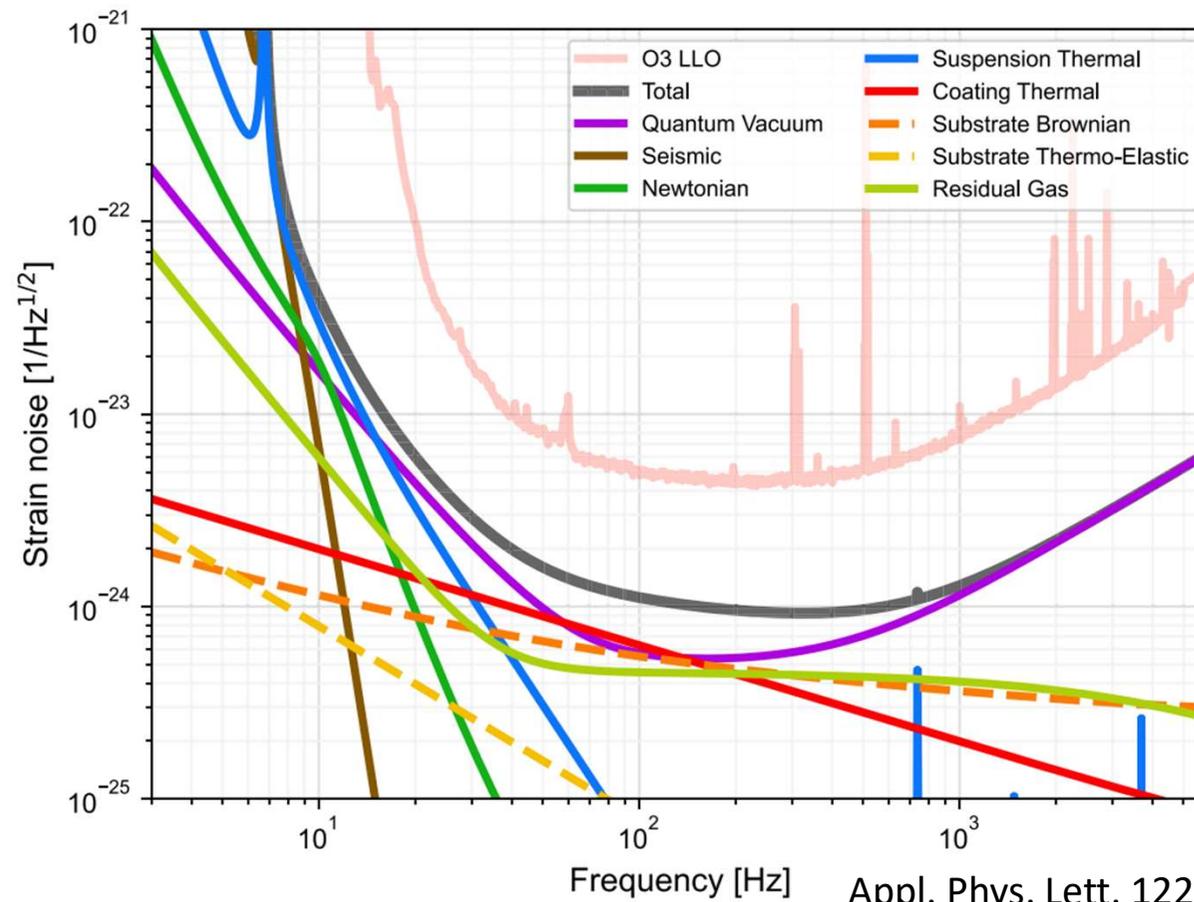
# GW170817



## 2. Sensitivity curve of gravitational wave detector



# LIGO sensitivity



Appl. Phys. Lett. 122, 110502 (2023)

# Signal and noise

---

Signal : 전달하고 자 하는 것

Noise : 시그널을 제외한 나머지

---

Google

뉴진스 직캠



전체 이미지 동영상 지도 뉴스 더보기 도구



YouTube  
입덕직캠 4K 뉴진스 민지 'Hype Boy' (NewJe...  
입덕직캠 뉴진스 하니 직캠 4K 'Attention' (NewJean...  
입덕직캠 뉴진스 민지 직캠 4K 'Attention' (...  
입덕직캠 뉴진스 해린 직캠 4K 'Attention' (...



YouTube  
입덕직캠 뉴진스 하니 직캠 4K 'Hype Boy...  
입덕직캠 4K 뉴진스 민지 'Hype Boy' (NewJ...  
입덕직캠 뉴진스 해린 직캠 4K 'Hype Boy' (NewJean...  
입덕직캠 뉴진스 다니엘 직캠 4K 'Hype Bo...  
네 영상



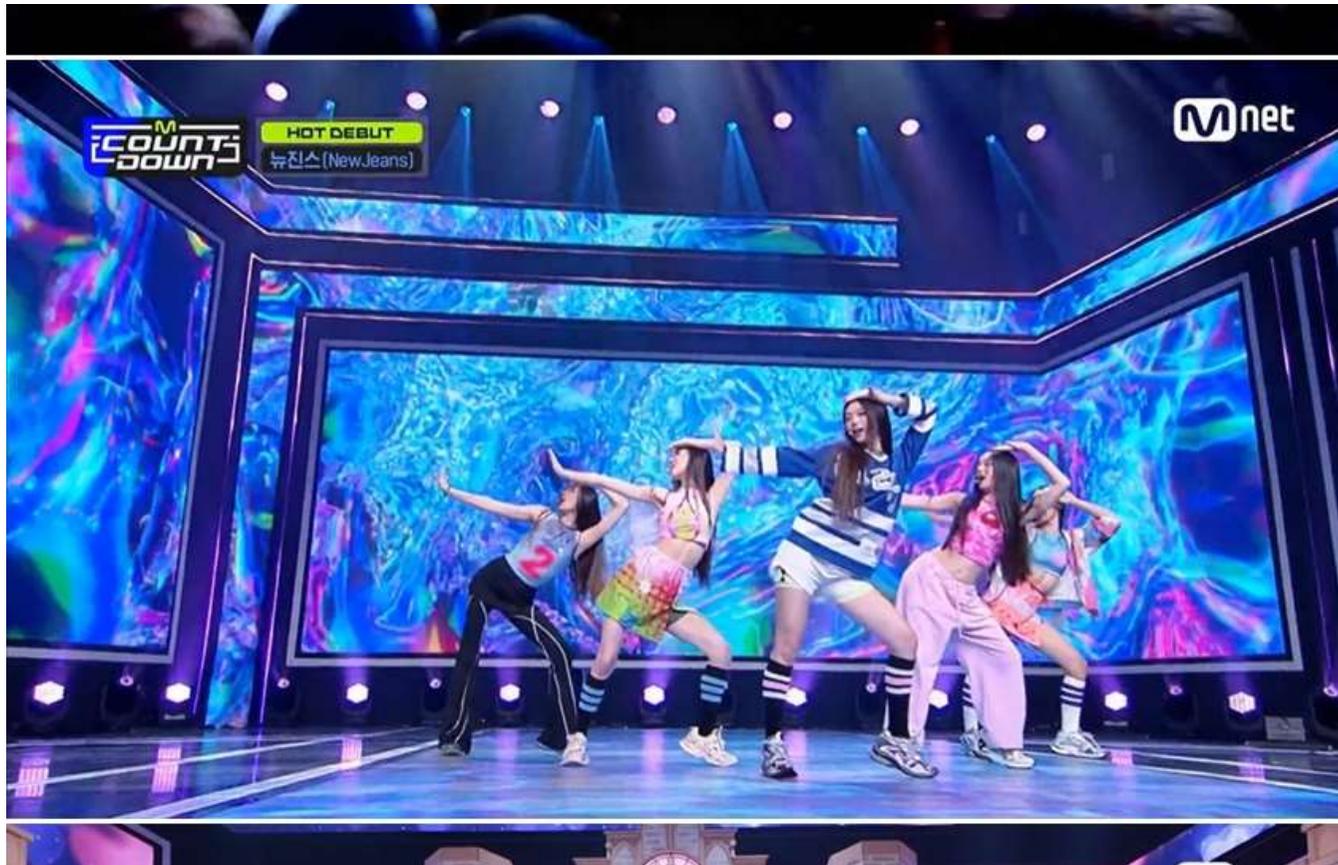
YouTube  
입덕직캠 4K 뉴진스 민지 'Attention' (NewJe...  
입덕직캠 뉴진스 하니 직캠 4K 'Cookie' (New...  
K-Fancam 뉴진스 민지 직캠 'Hype boy' (NewJe...  
안방1열 직캠4K 뉴진스 해린 'Cookie' (NewJe...

아이돌 직캠?

왜??

# Signal and noise

---

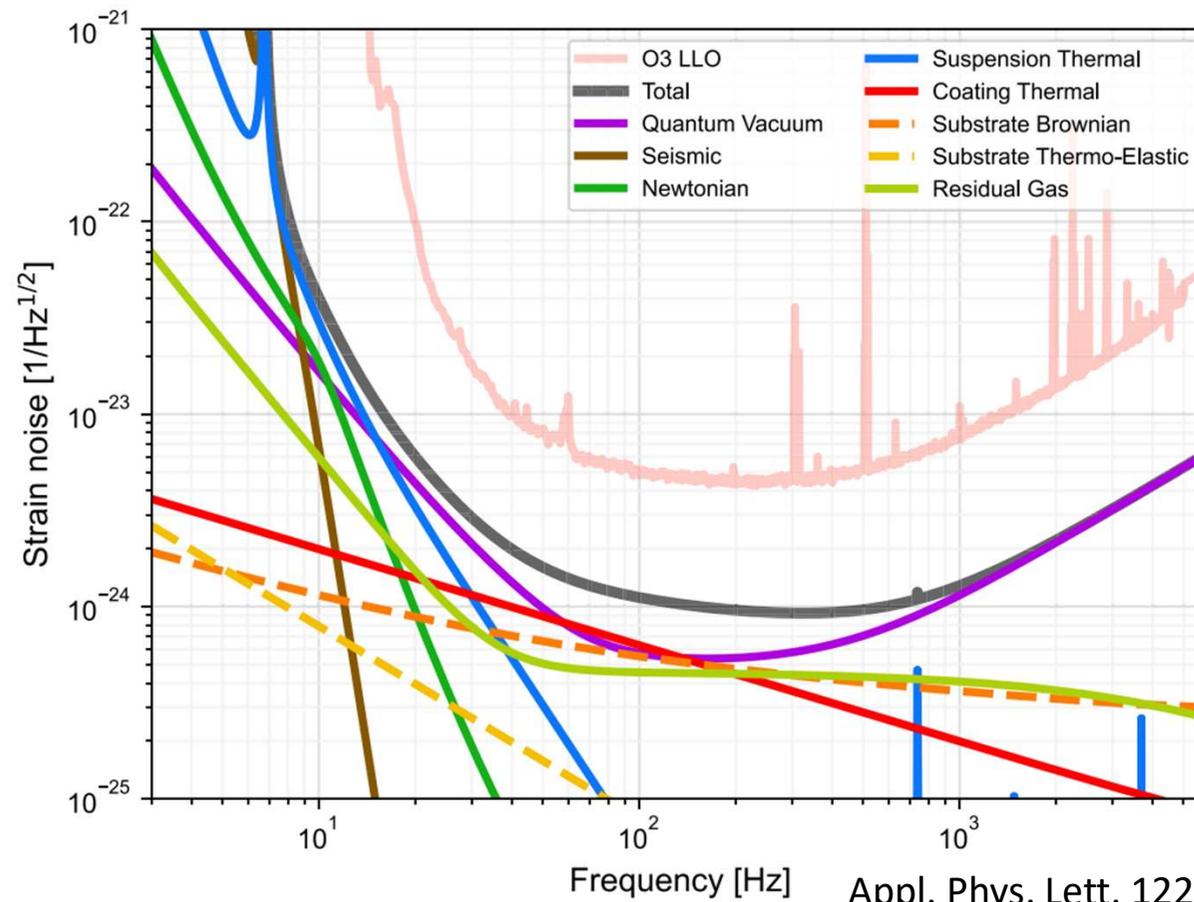


Signal : 내가보고 싶은 멤버

Noise : 내가 보고싶은 멤버  
뺀 나머지

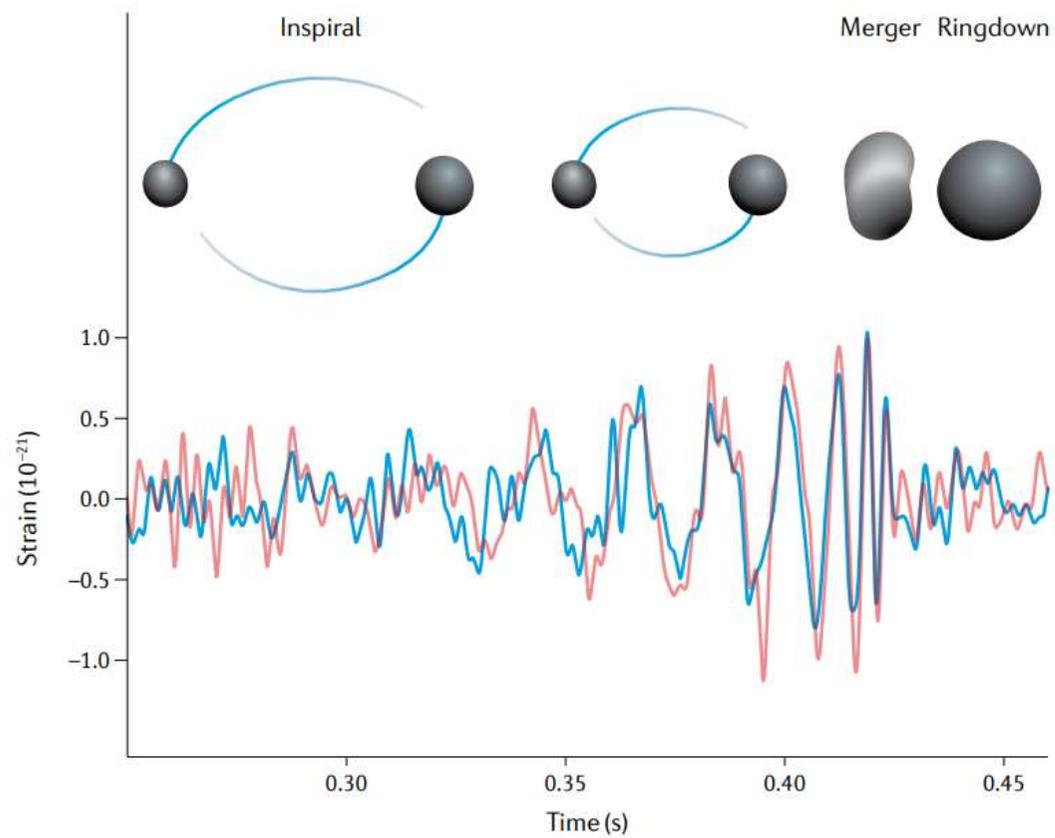
---

# LIGO sensitivity



Appl. Phys. Lett. 122, 110502 (2023)

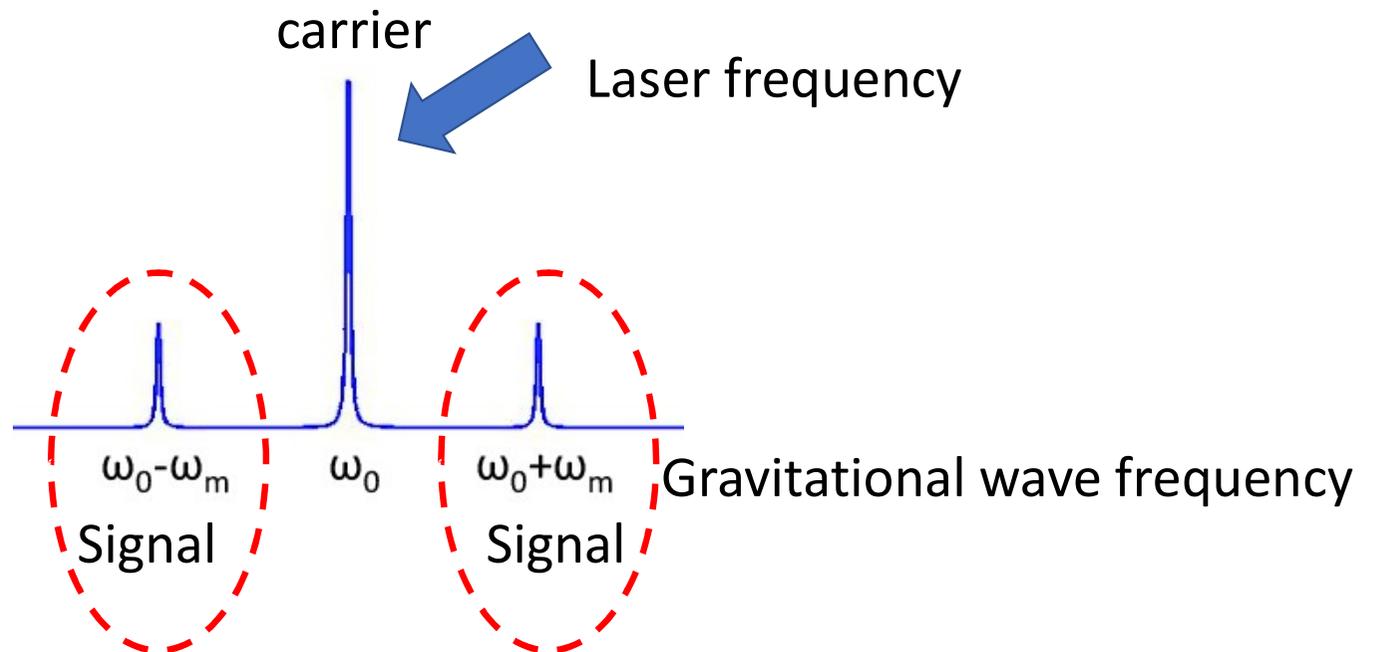
# Inspiral–Merger–Ringdown



*Nature Reviews Physics* volume 3, pages344–366 (2021)

# Side band figure

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## Side band figure

---

We can illustrate the creation of sidebands with one trigonometric identity:

$$\cos(A) \cdot \cos(B) \equiv \frac{1}{2} \cos(A + B) + \frac{1}{2} \cos(A - B)$$

Adding  $\cos(A)$  to both sides:

$$\cos(A) \cdot [1 + \cos(B)] = \frac{1}{2} \cos(A + B) + \cos(A) + \frac{1}{2} \cos(A - B)$$

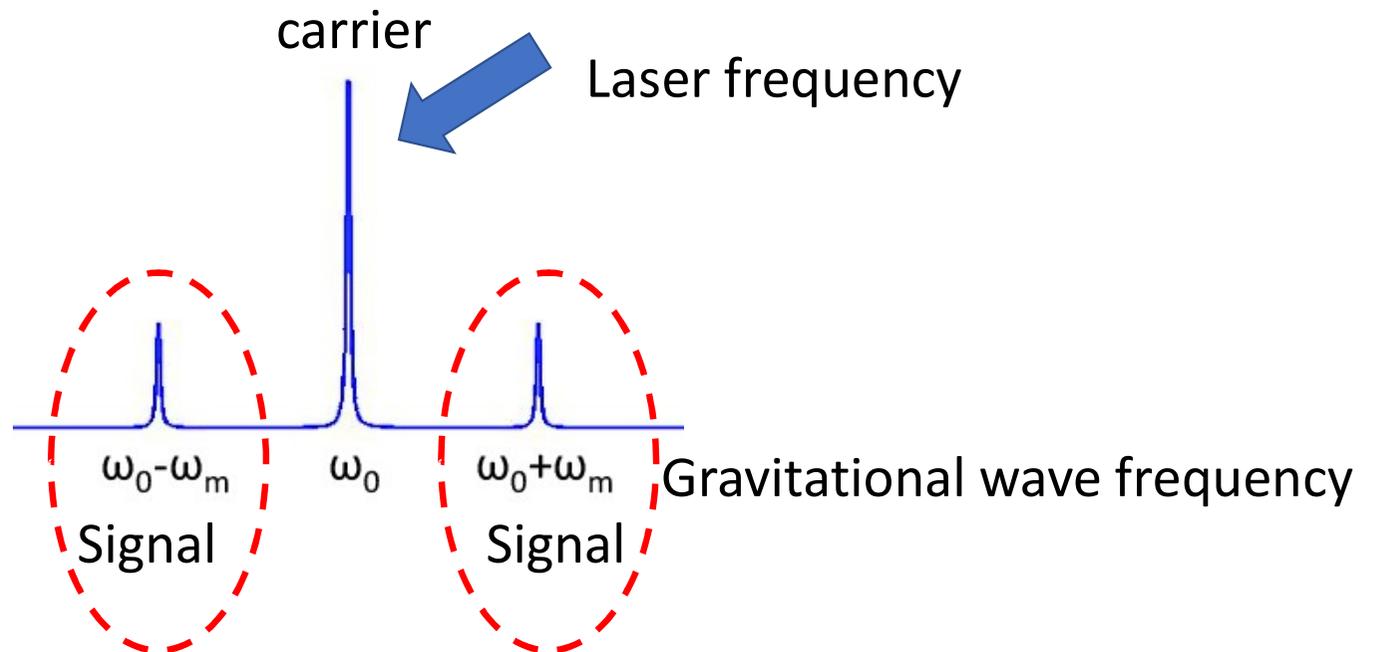
Substituting (for instance)  $A \triangleq 1000 \cdot t$  and  $B \triangleq 100 \cdot t$ , where  $t$  represents time:

$$\underbrace{\cos(1000 t)}_{\text{carrier wave}} \cdot \underbrace{[1 + \cos(100 t)]}_{\text{amplitude modulation}} = \underbrace{\frac{1}{2} \cos(1100 t)}_{\text{upper sideband}} + \underbrace{\cos(1000 t)}_{\text{carrier wave}} + \underbrace{\frac{1}{2} \cos(900 t)}_{\text{lower sideband}}.$$

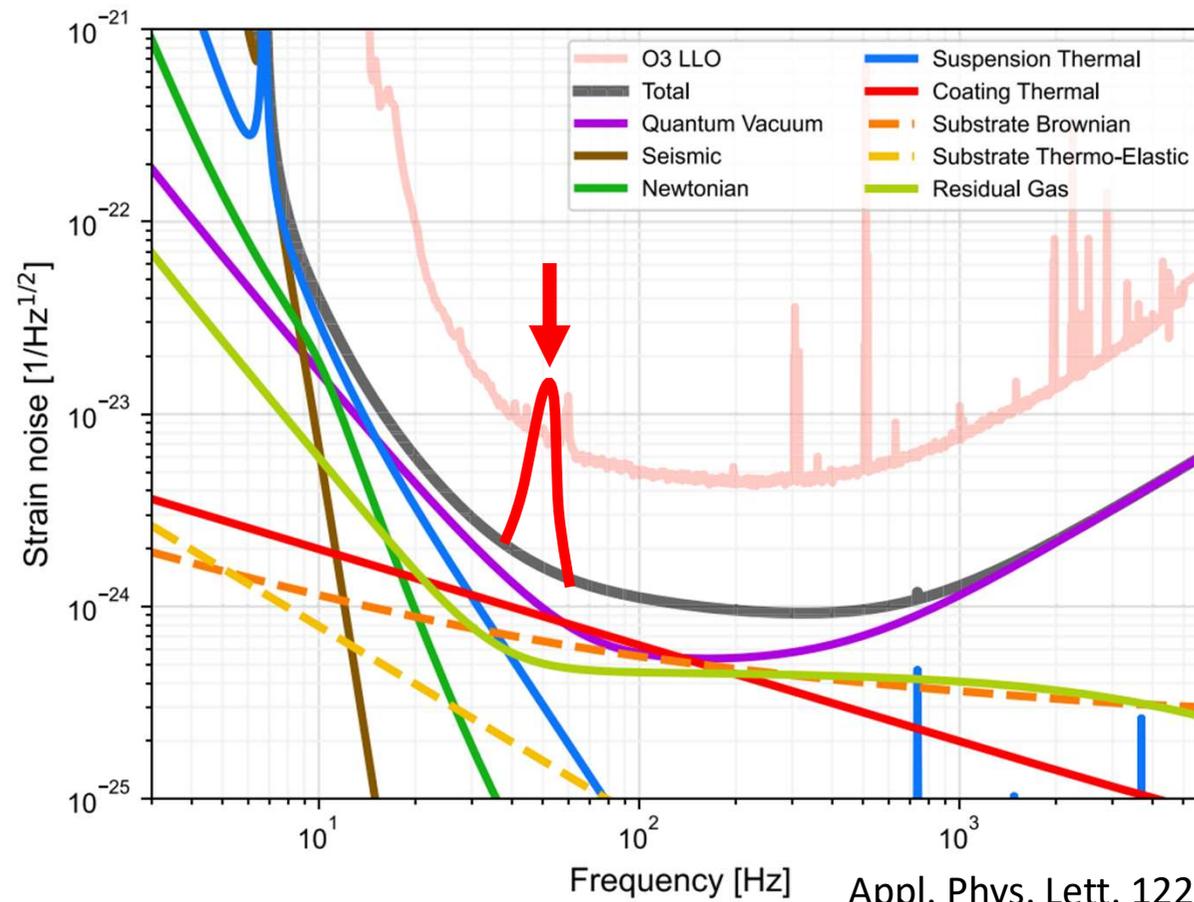
---

# Side band figure

---

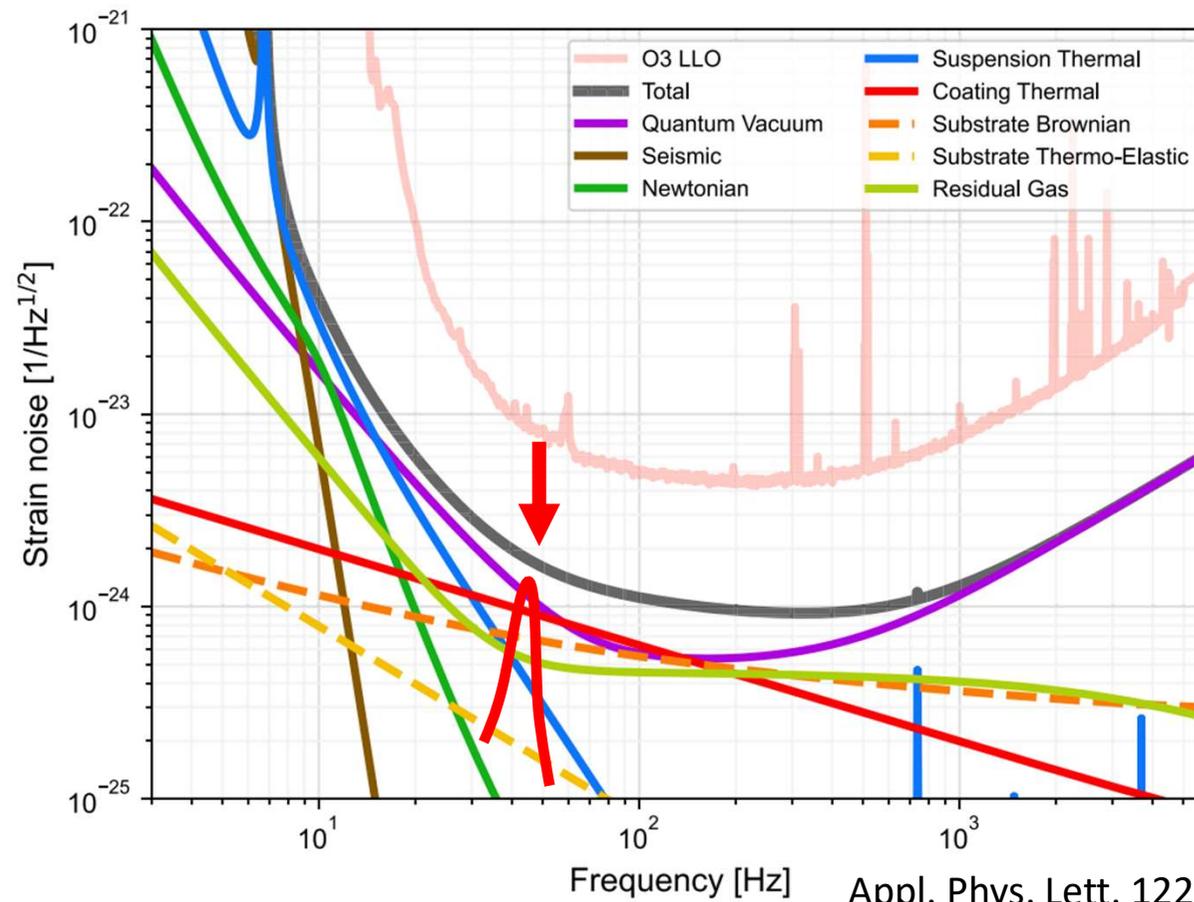


# LIGO sensitivity



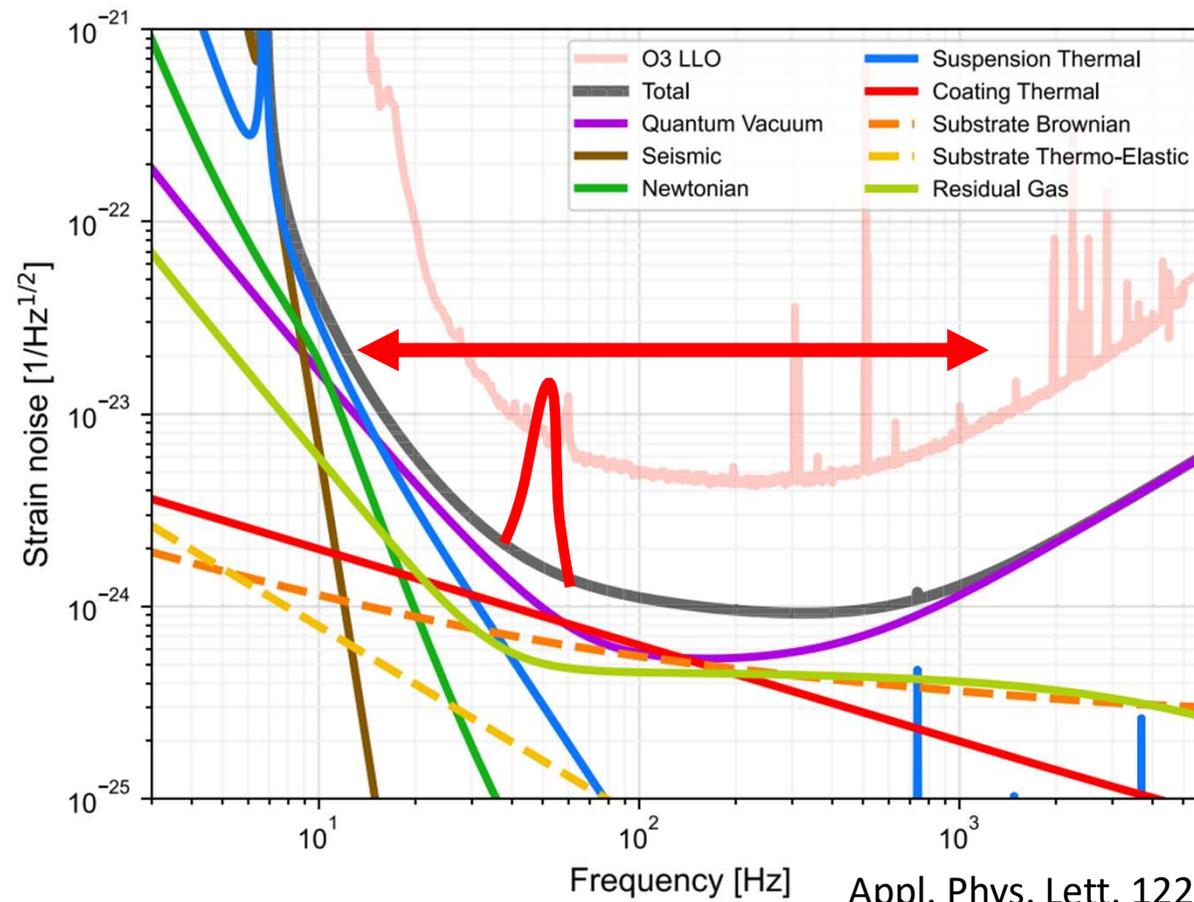
Appl. Phys. Lett. 122, 110502 (2023)

# LIGO sensitivity



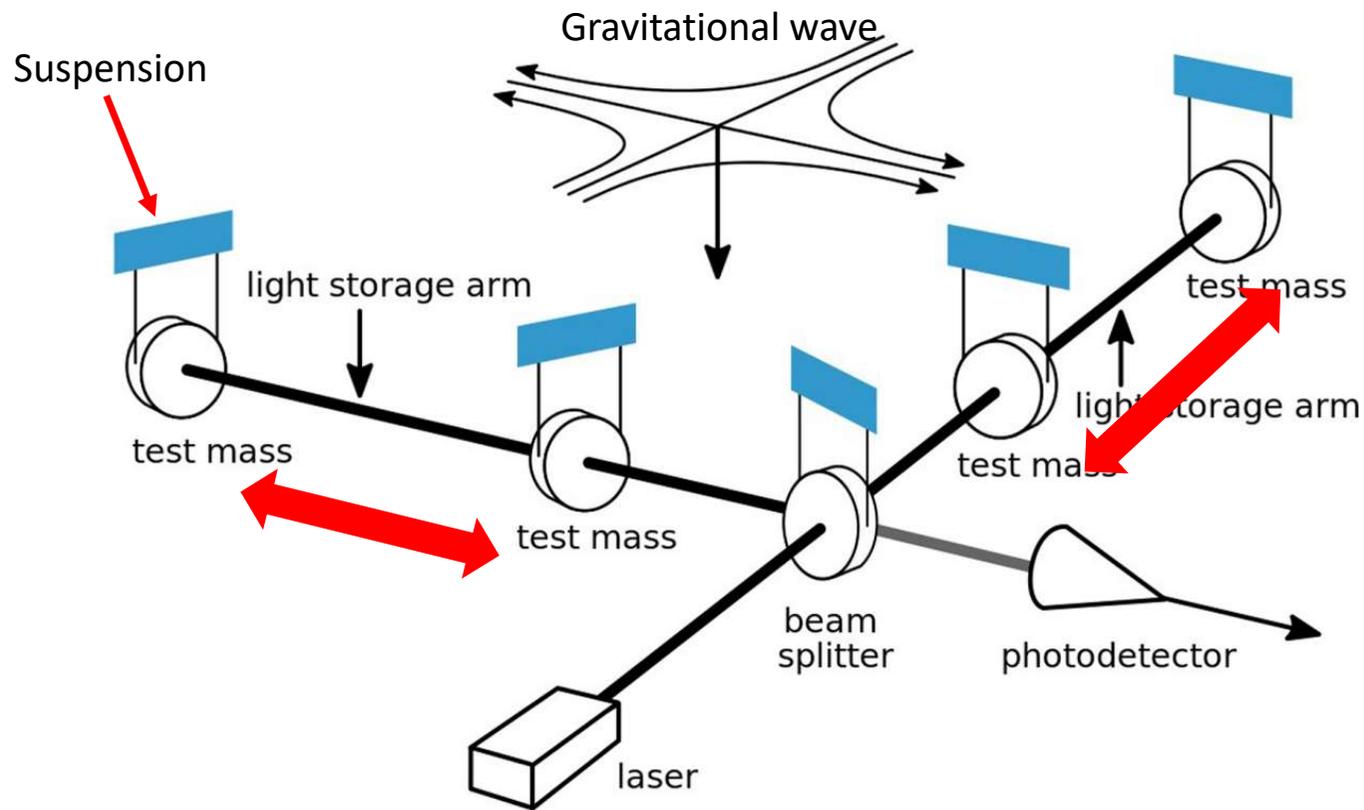
Appl. Phys. Lett. 122, 110502 (2023)

# LIGO sensitivity



Appl. Phys. Lett. 122, 110502 (2023)

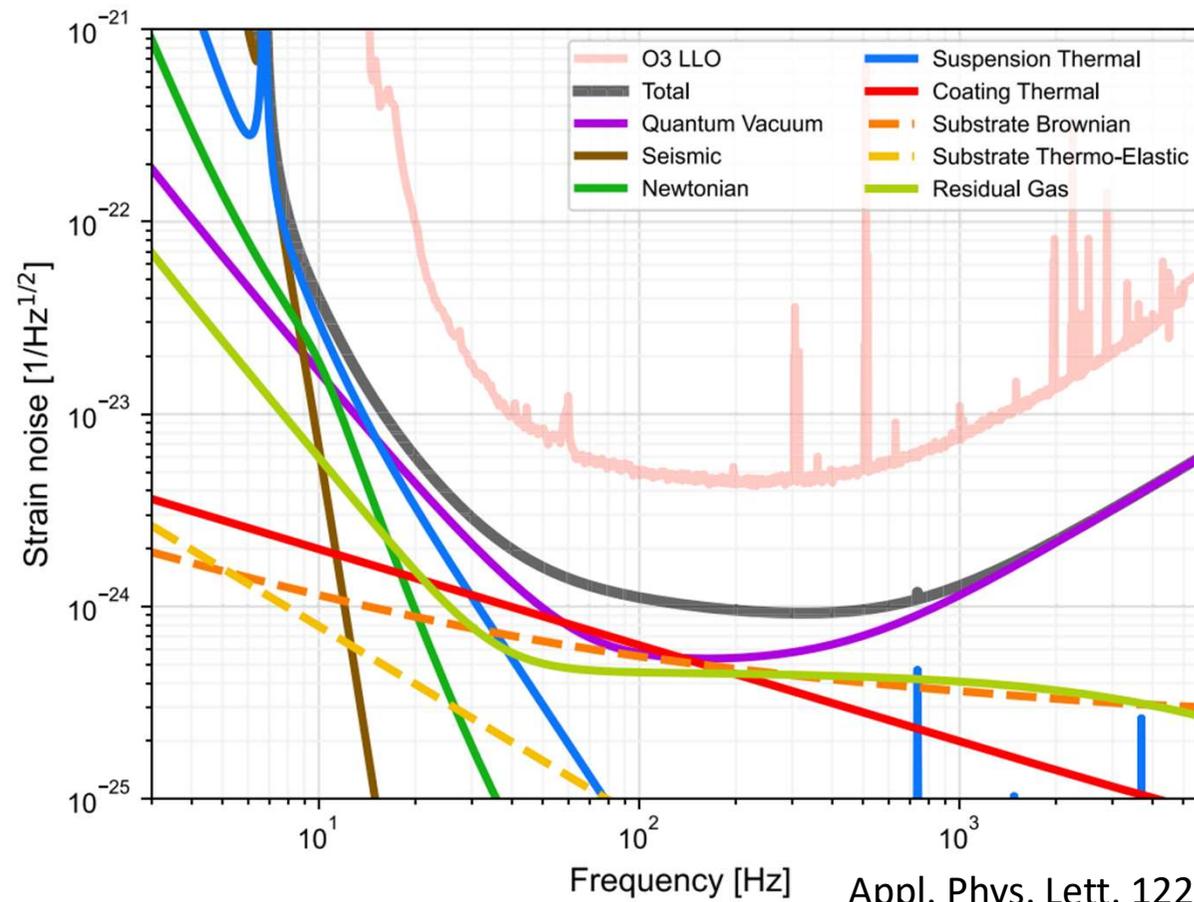
# Gravitational wave and GW detector



<https://www.ligo.caltech.edu/>

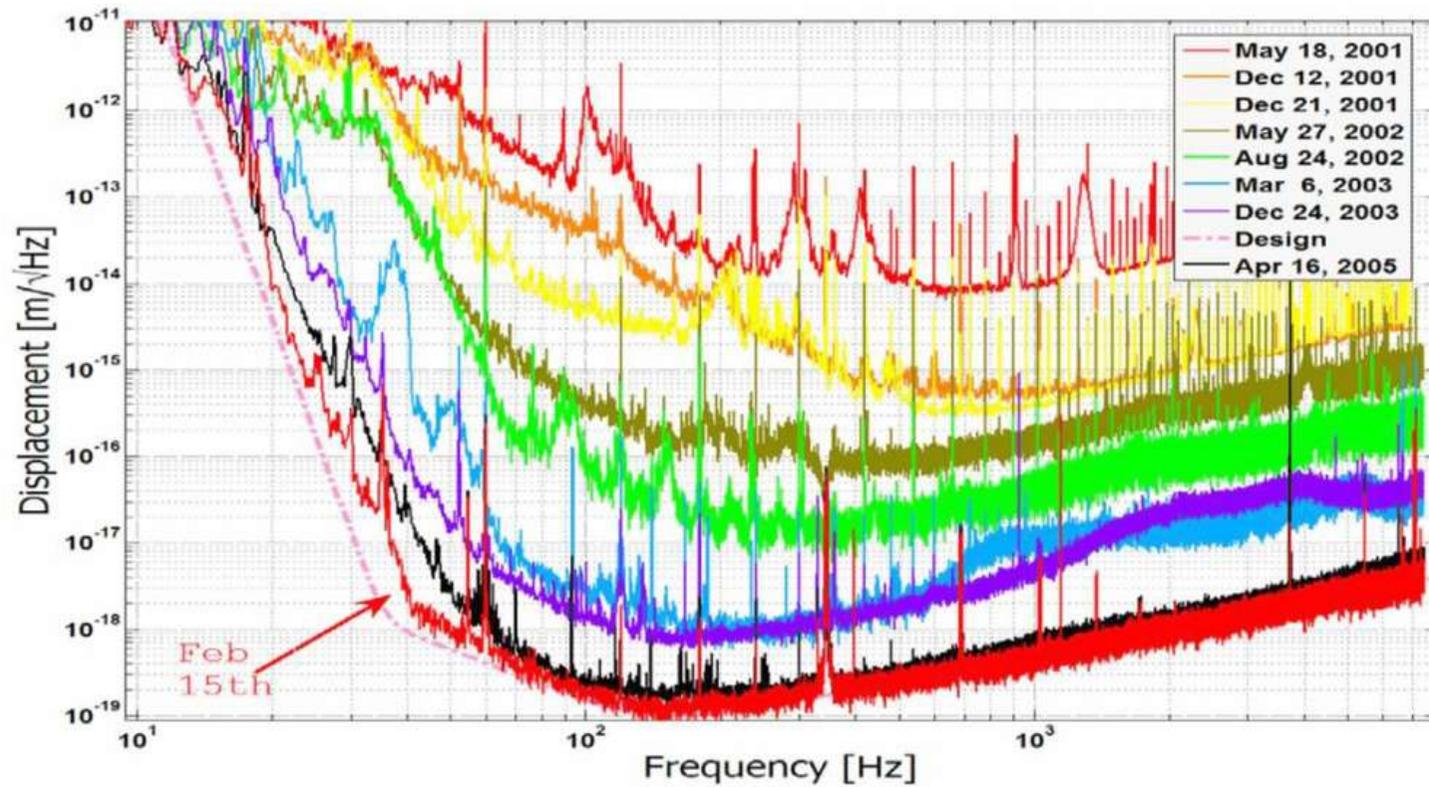
Swing out of gravitational wave frequency

# LIGO sensitivity

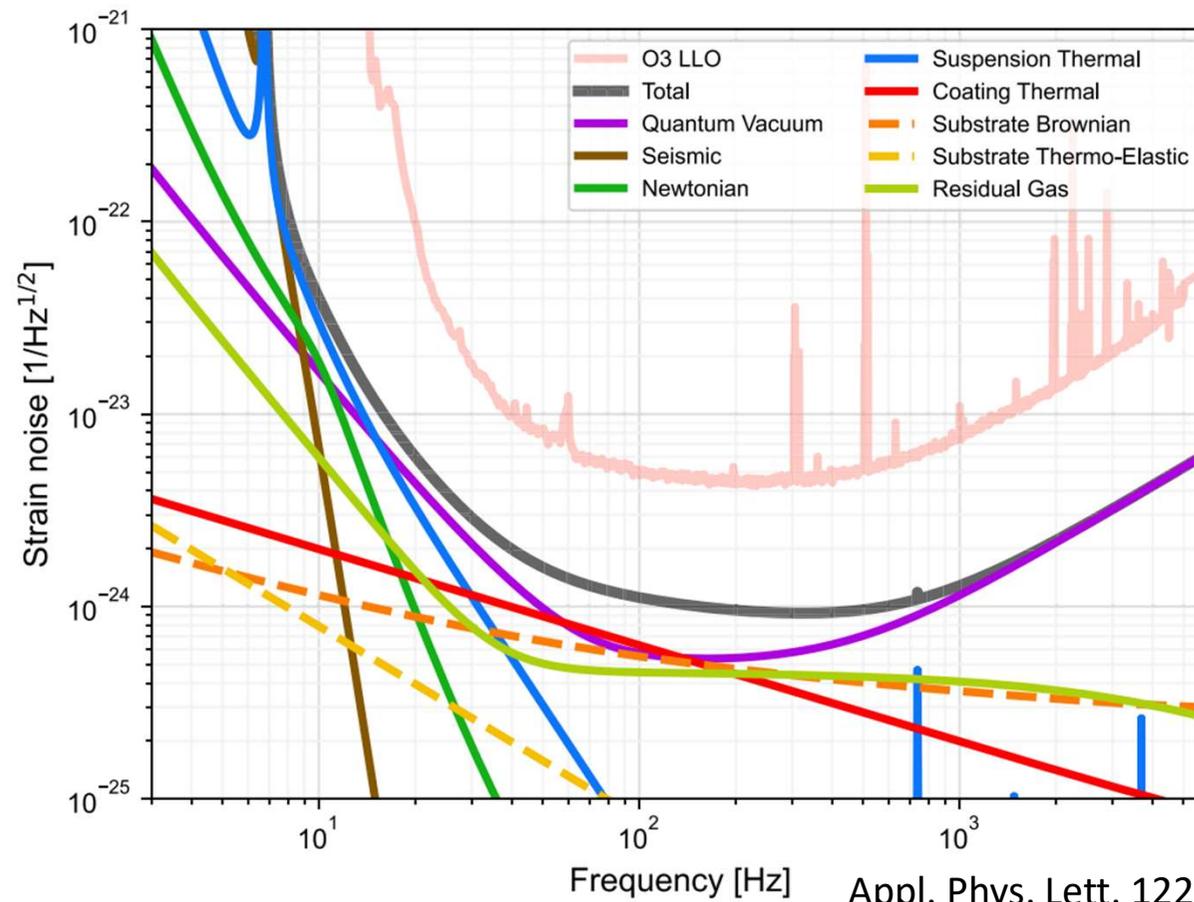


Appl. Phys. Lett. 122, 110502 (2023)

# Sensitivity during science run

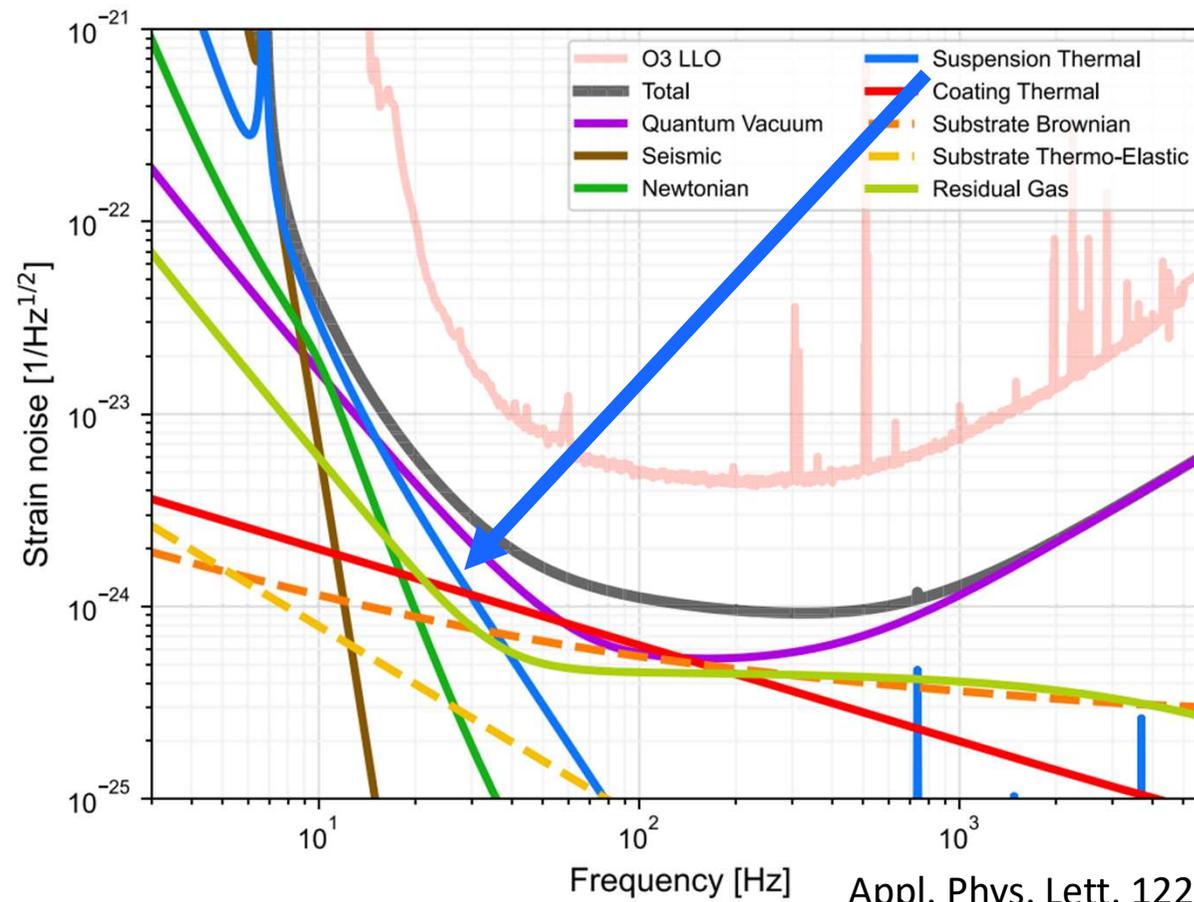


# LIGO sensitivity



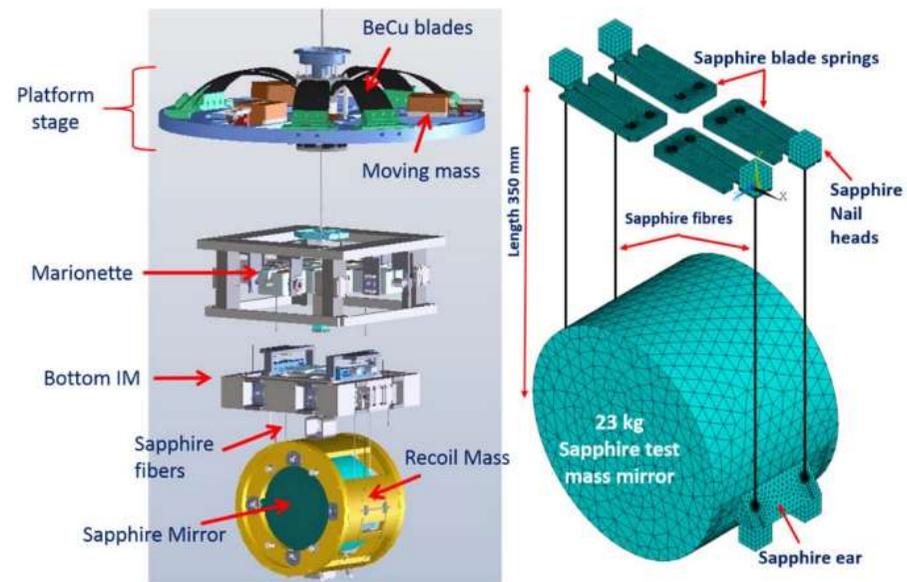
Appl. Phys. Lett. 122, 110502 (2023)

# LIGO sensitivity

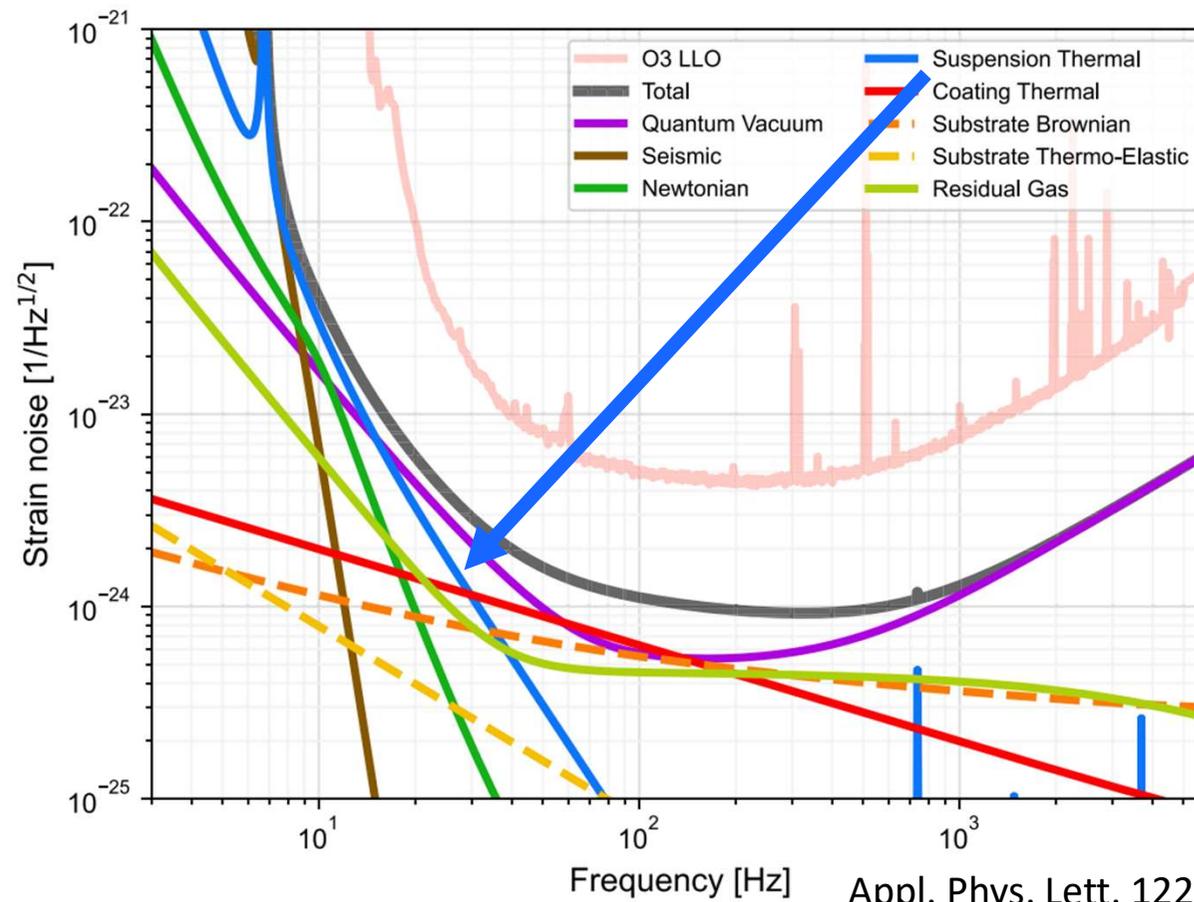


Appl. Phys. Lett. 122, 110502 (2023)

# Suspension

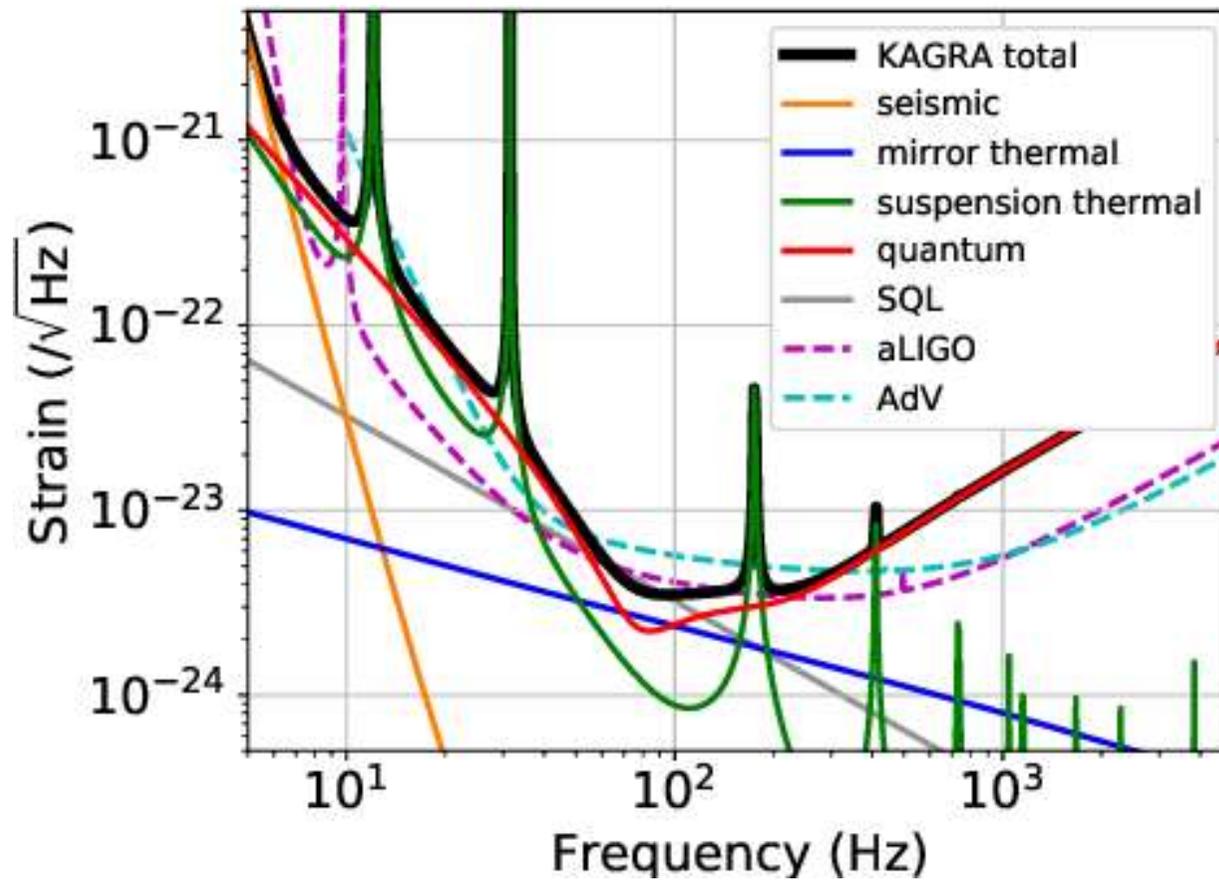


# LIGO sensitivity

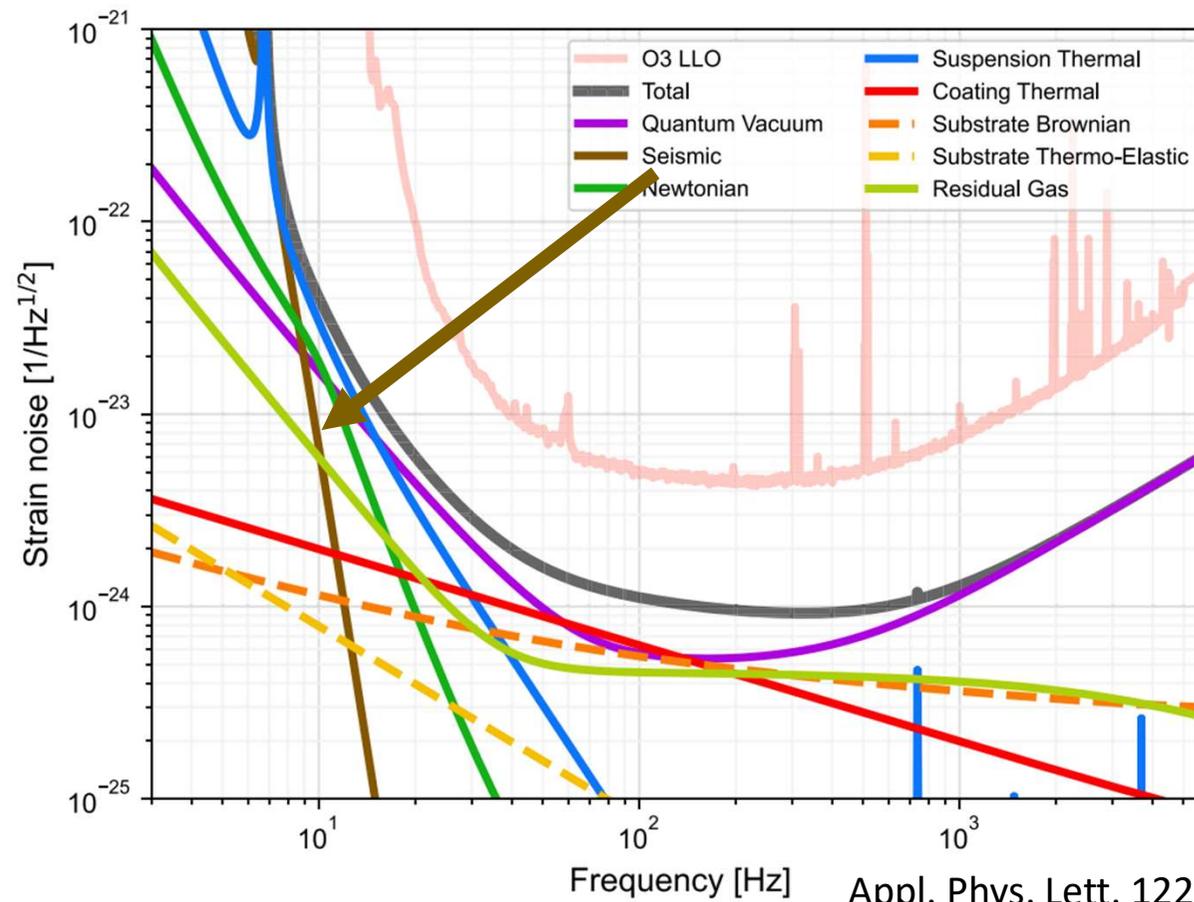


Appl. Phys. Lett. 122, 110502 (2023)

# Sensitivity curve of KAGRA

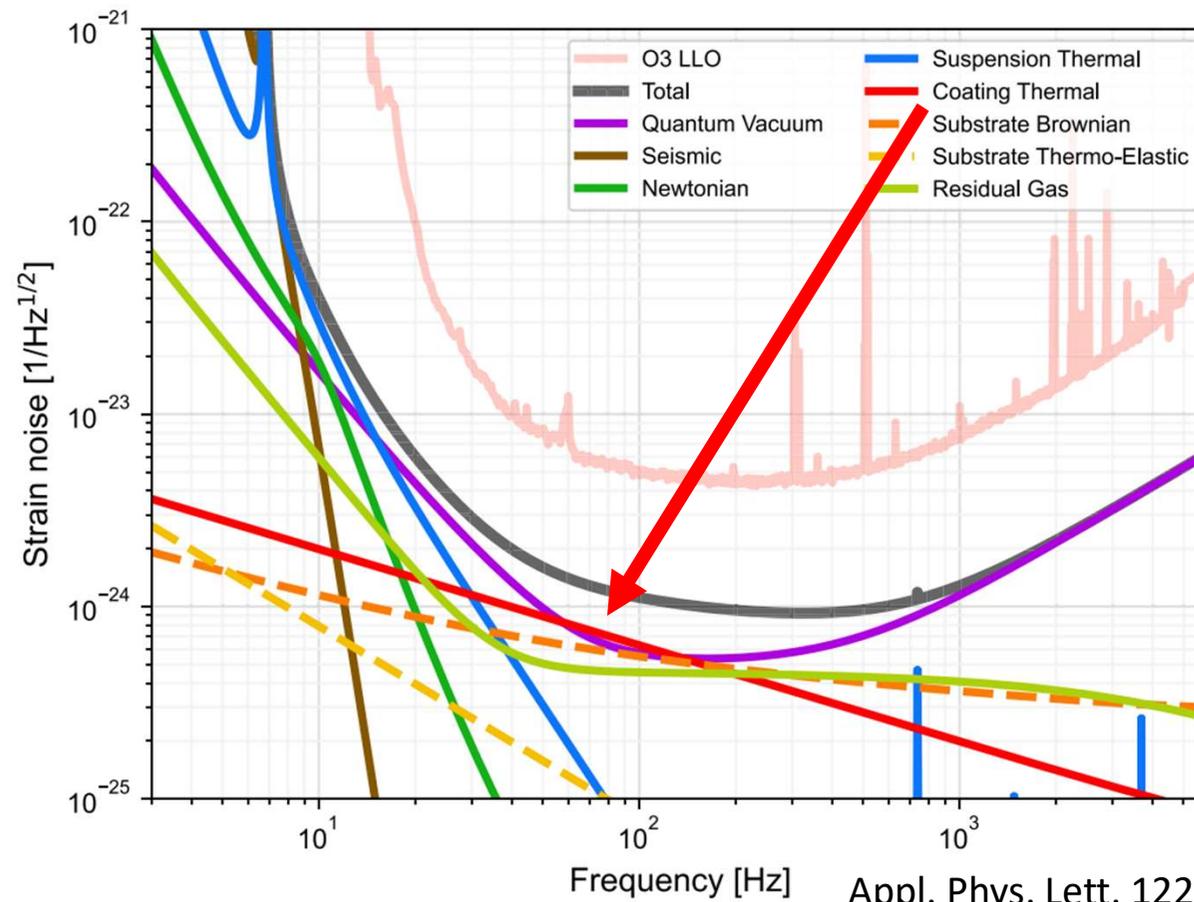


# LIGO sensitivity



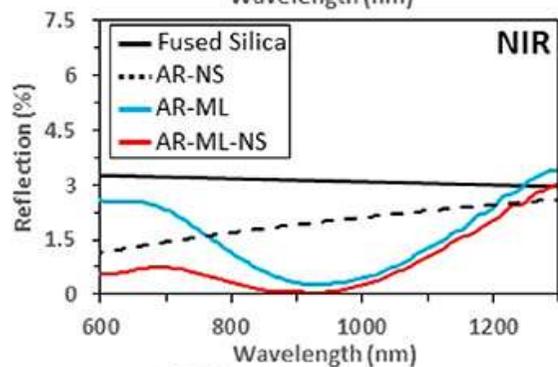
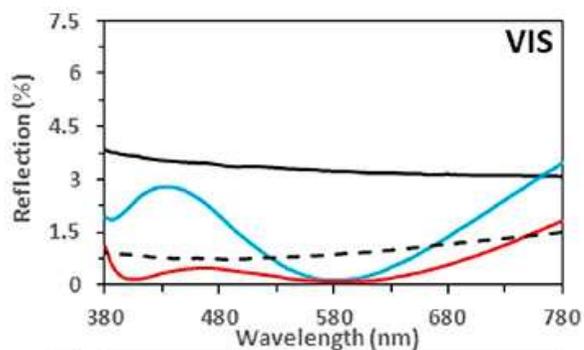
Appl. Phys. Lett. 122, 110502 (2023)

# LIGO sensitivity

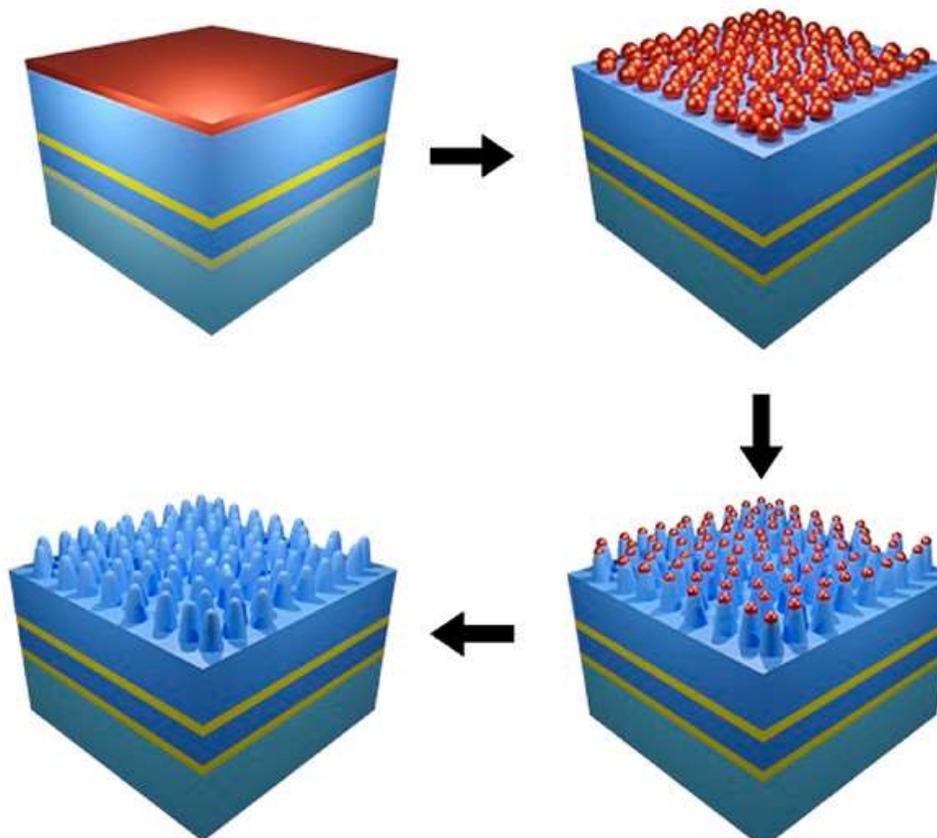


Appl. Phys. Lett. 122, 110502 (2023)

# Optical coating



CA > 150°

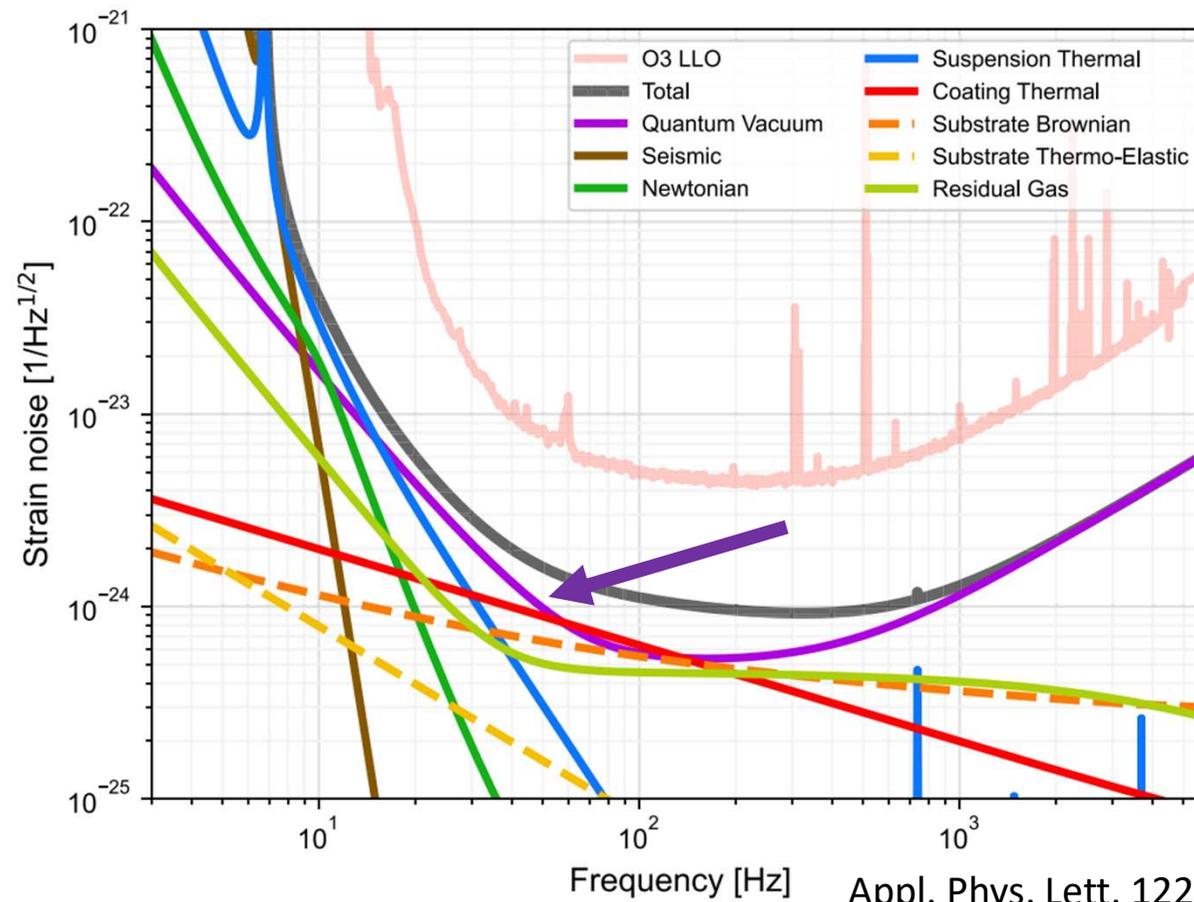


ACS Photonics 2021, 8, 3, 894–900

Publication Date: February 17, 2021

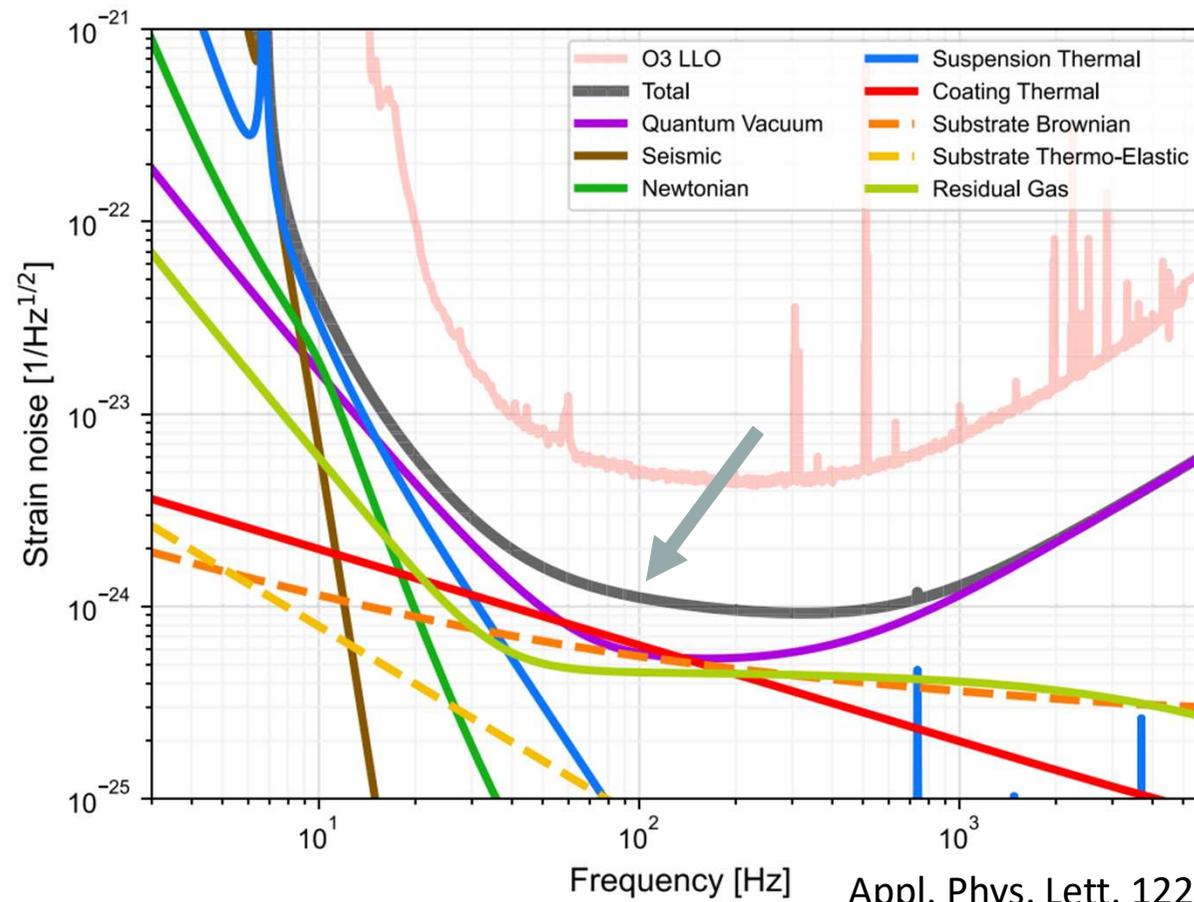
<https://doi.org/10.1021/acsp Photonics.0c01909>

# LIGO sensitivity



Appl. Phys. Lett. 122, 110502 (2023)

# LIGO sensitivity



Appl. Phys. Lett. 122, 110502 (2023)

### **3. Various techniques in gravitational wave detector**



# Vacuum tunnel

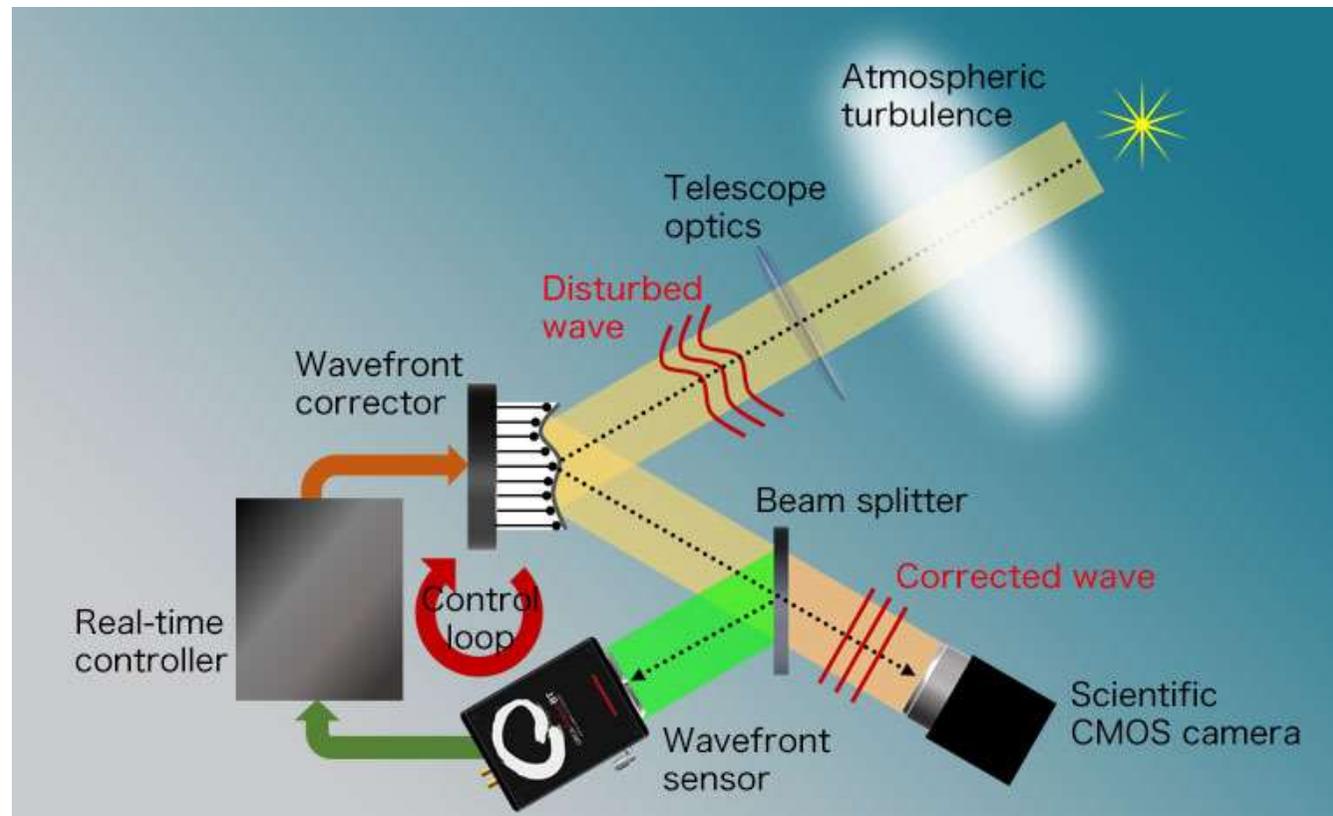
---



Air turbulence, scattering from air

---

# Atmospheric turbulence



# Vacuum tunnel

---

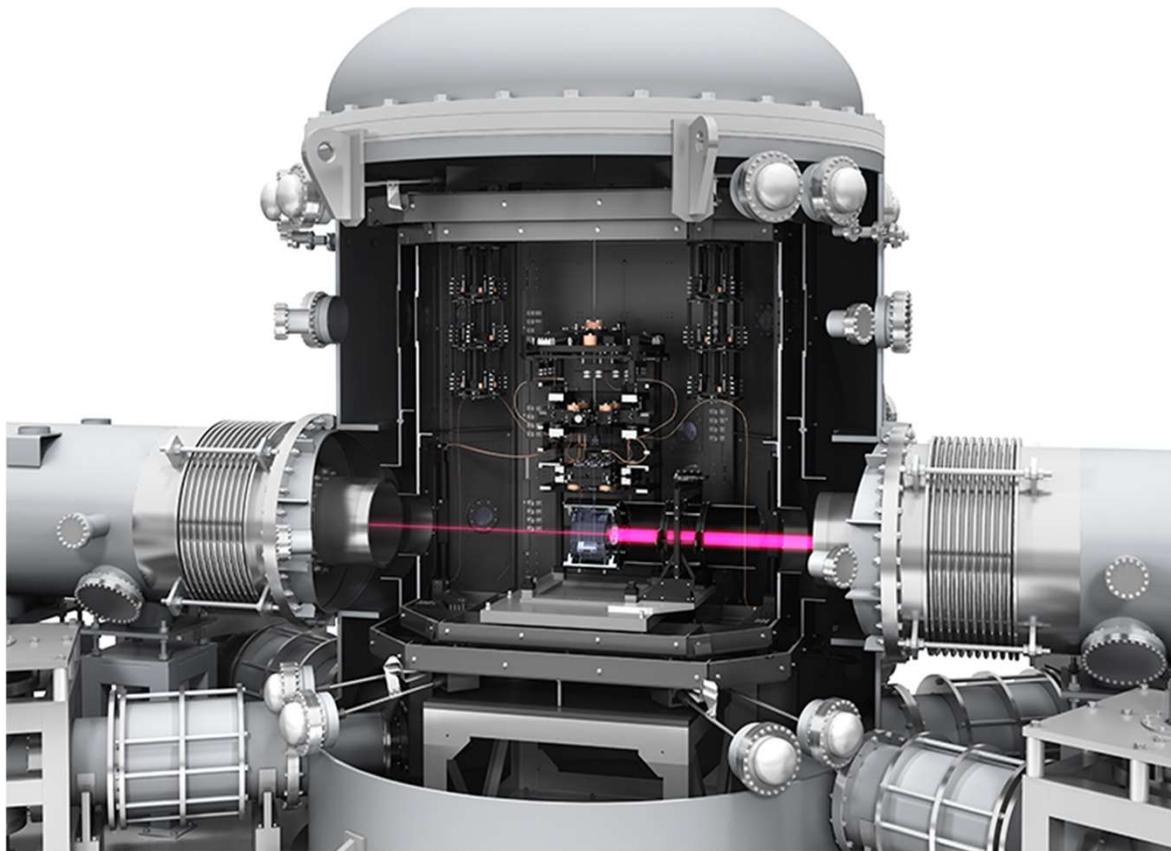


Air turbulence, scattering from air

---

# Test mass chamber

---

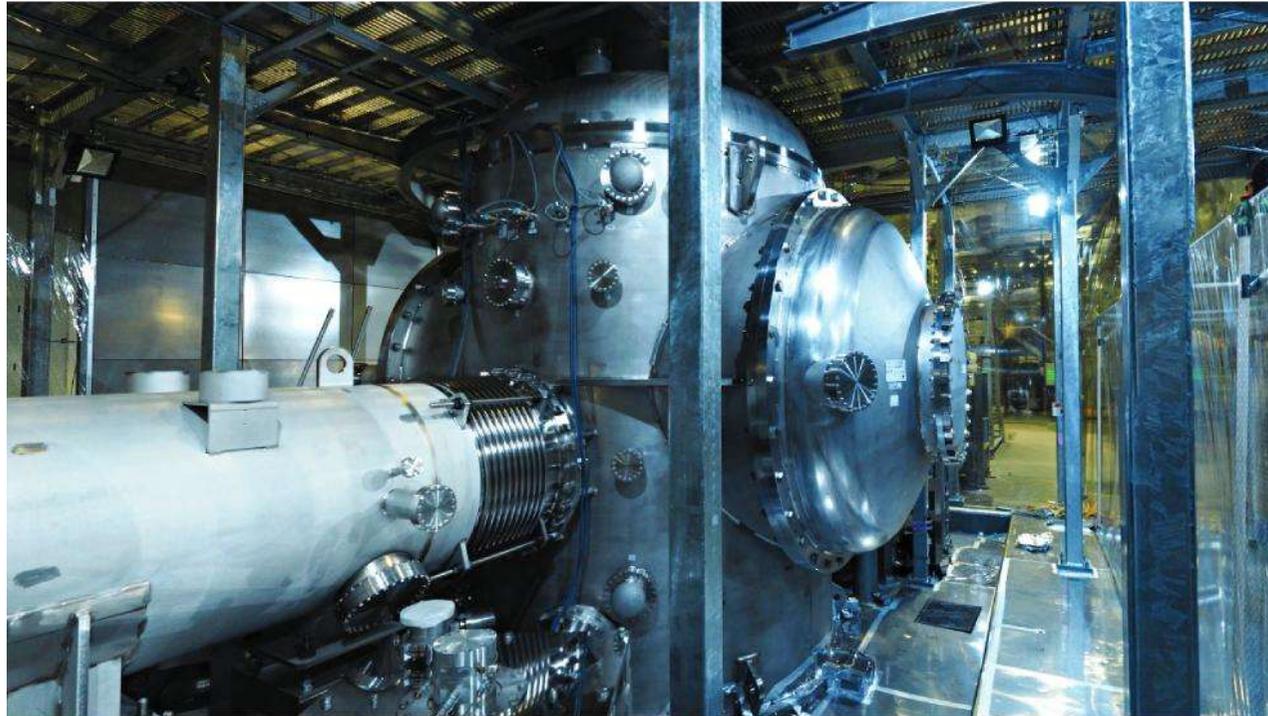


Rey.Hori

---

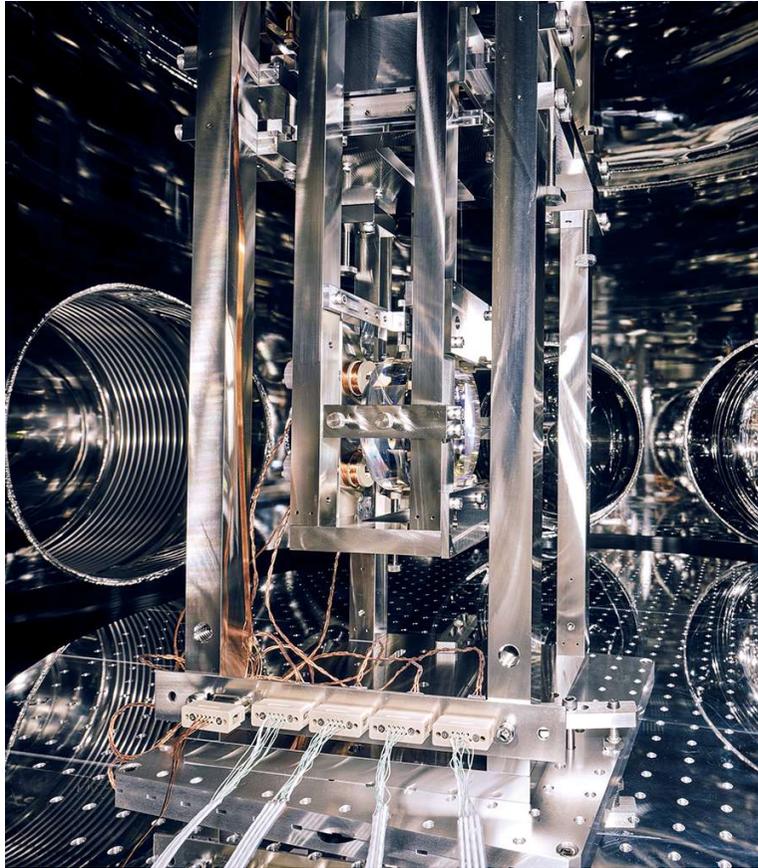
# KAGRA vacuum chamber

---



# KAGRA vacuum chamber

---

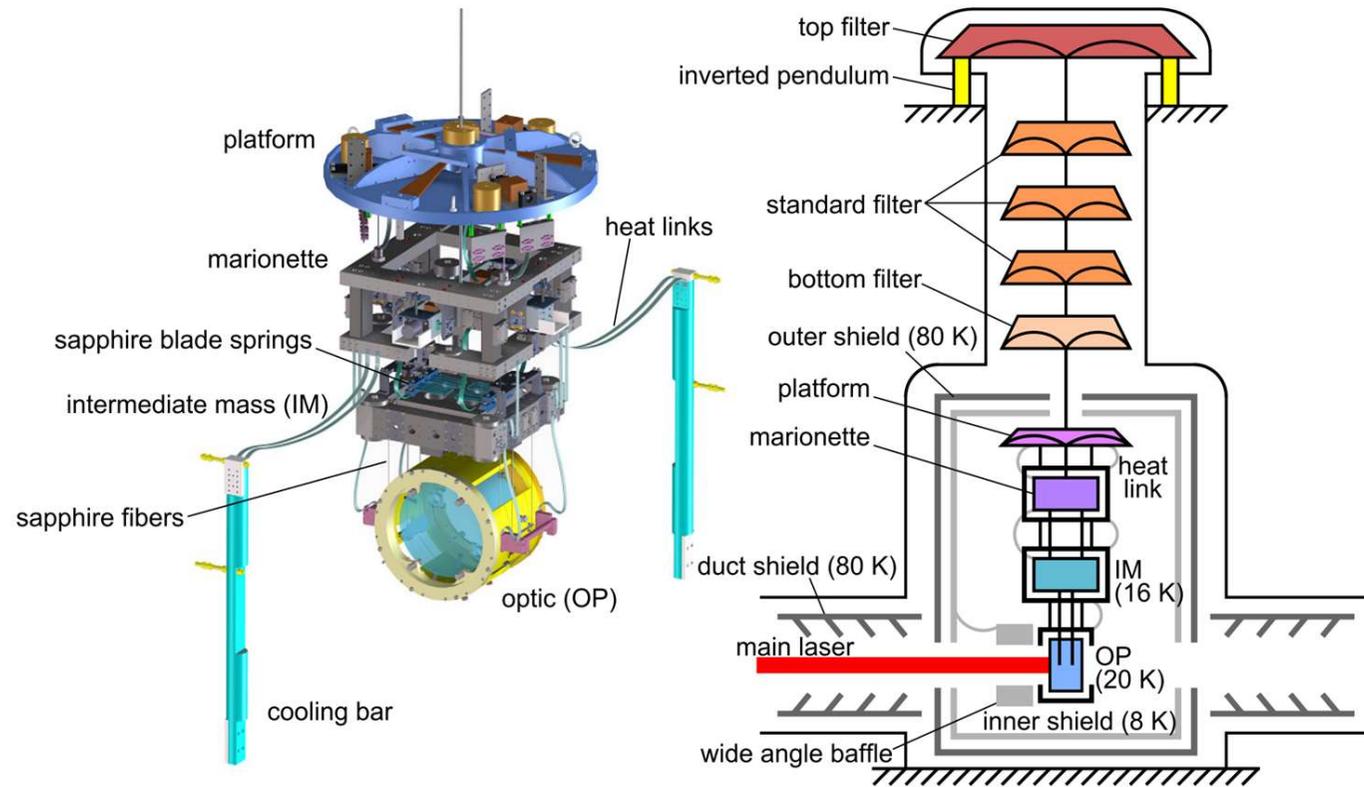


# Cryocooler of KAGRA

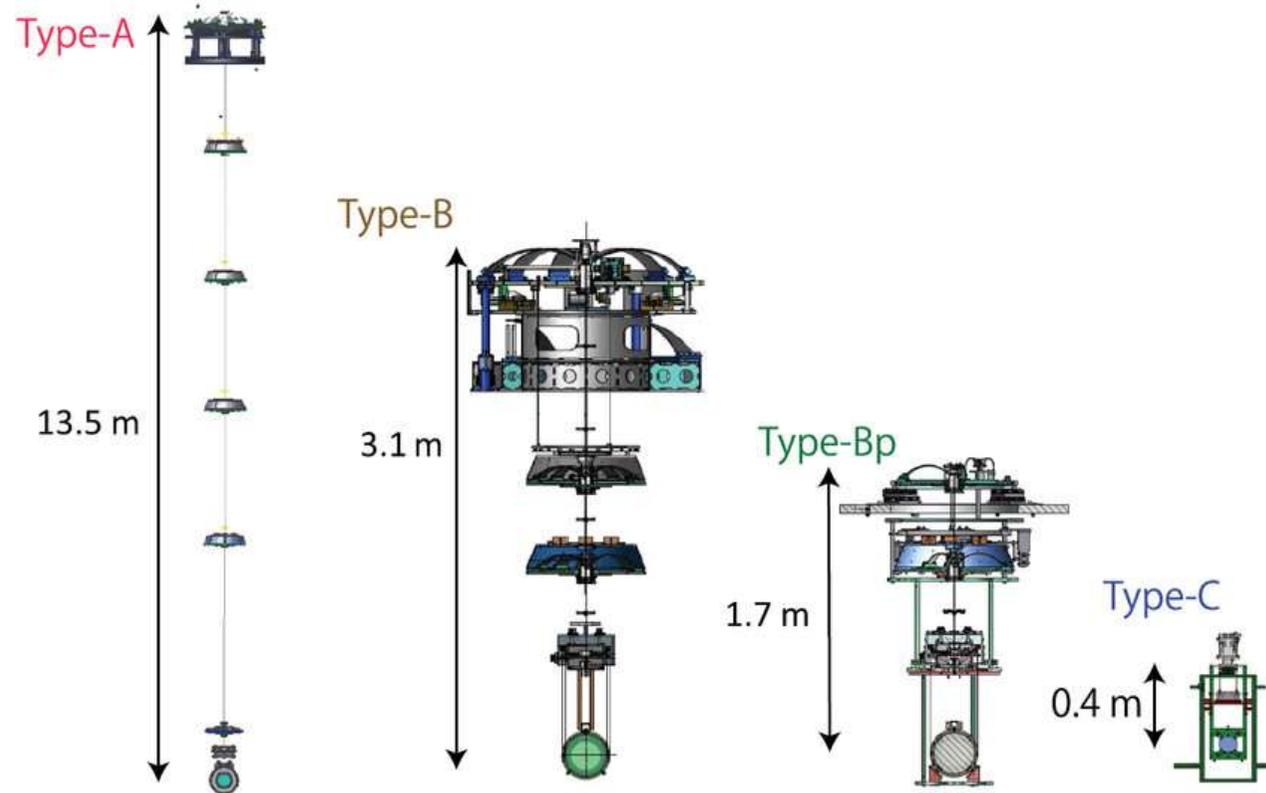
---



# KAGRA cryostat



# Vibration isolation



[Vibration isolation system with a compact damping system for power recycling mirrors of KAGRA](#)

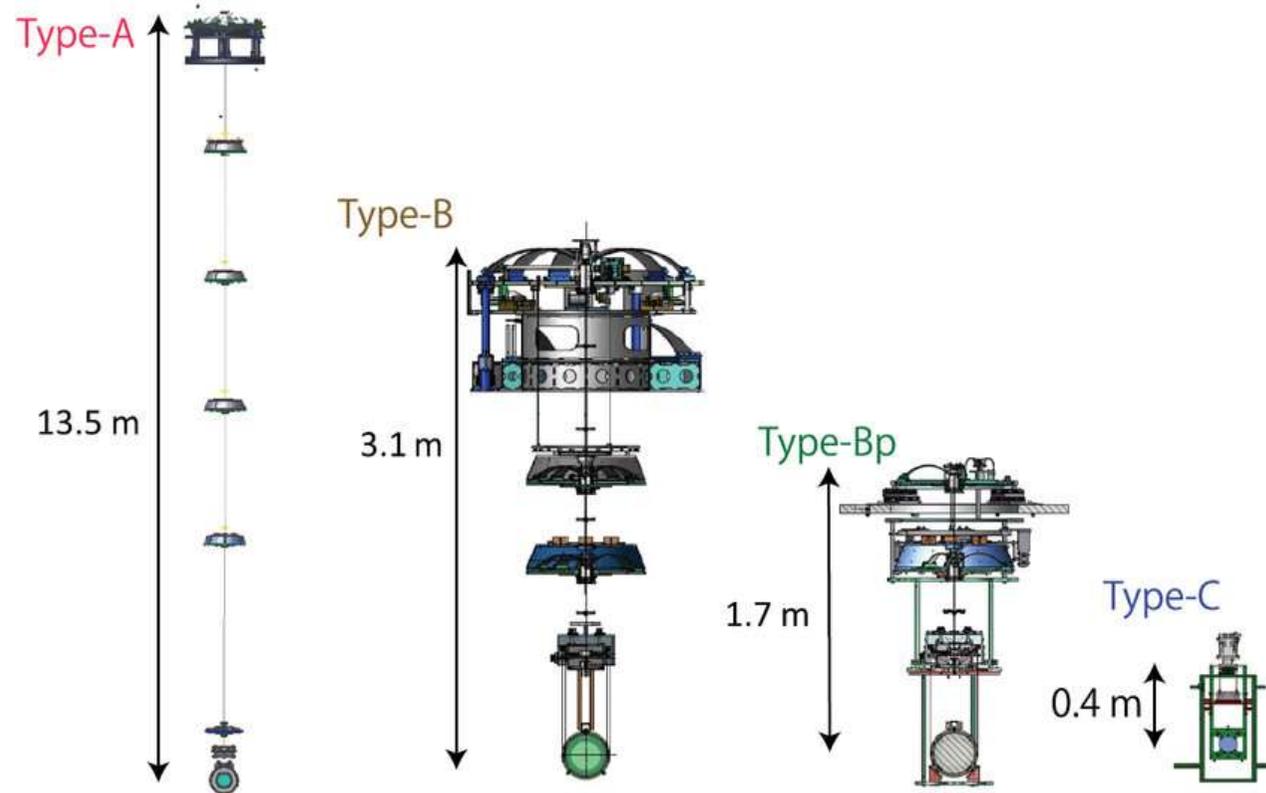
T.Akuts et al.,

# Vibration isolation

---



# Vibration isolation

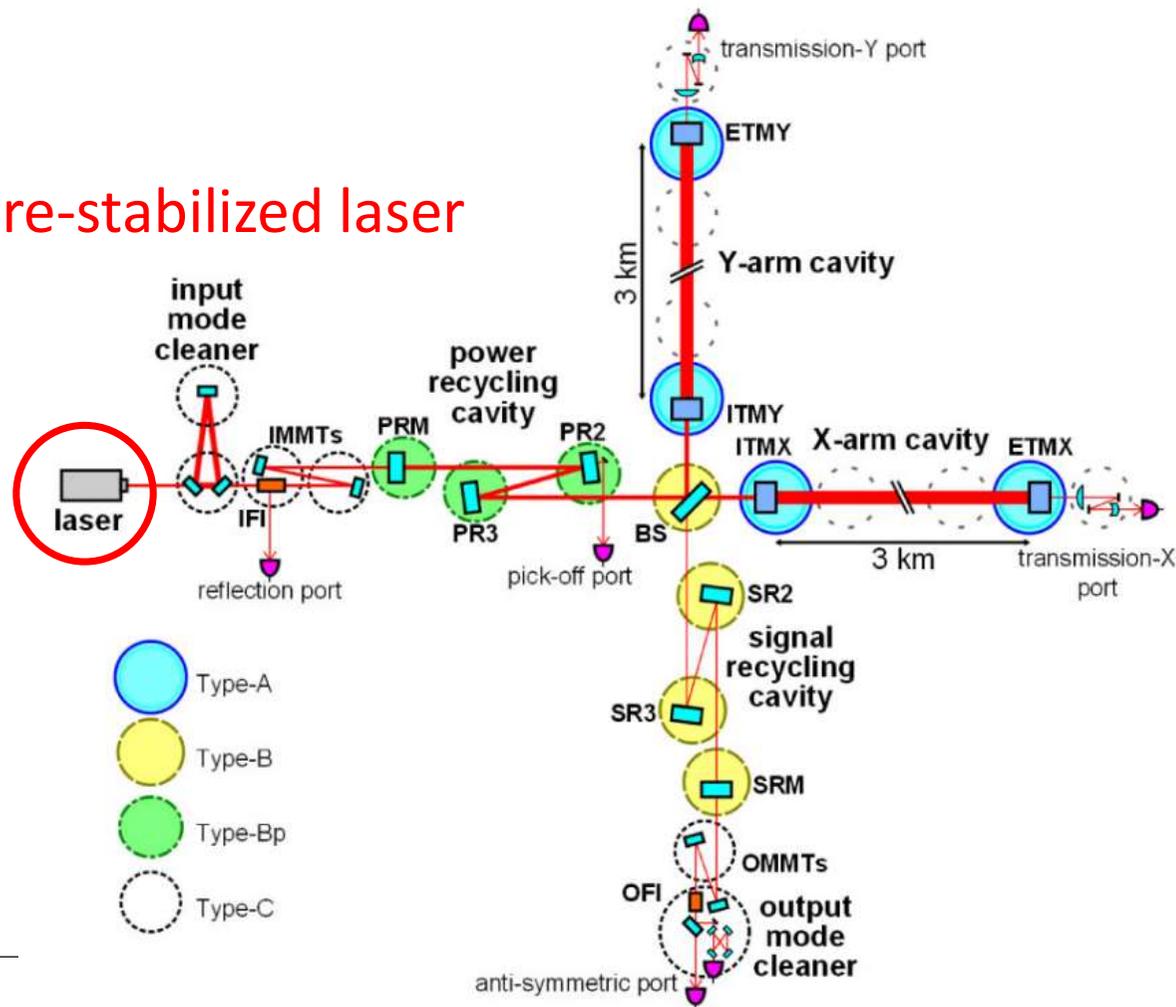


[Vibration isolation system with a compact damping system for power recycling mirrors of KAGRA](#)

T.Akuts et al.,

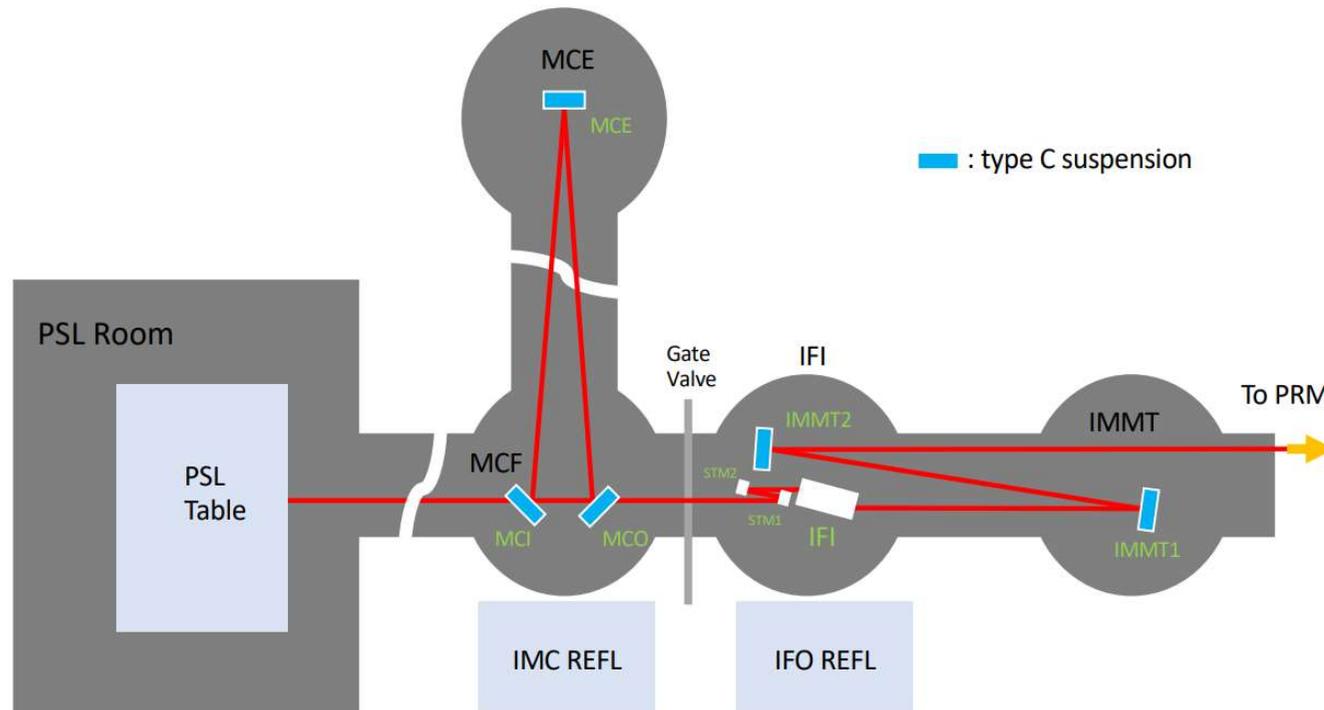
# KAGRA interferometer

Pre-stabilized laser



IOO : Input output optics  
MIF : Main interferometer  
MIR : Mirror  
MMT : Mode matching telescope  
OMC : Output mode cleaner

# IOO of KAGRA



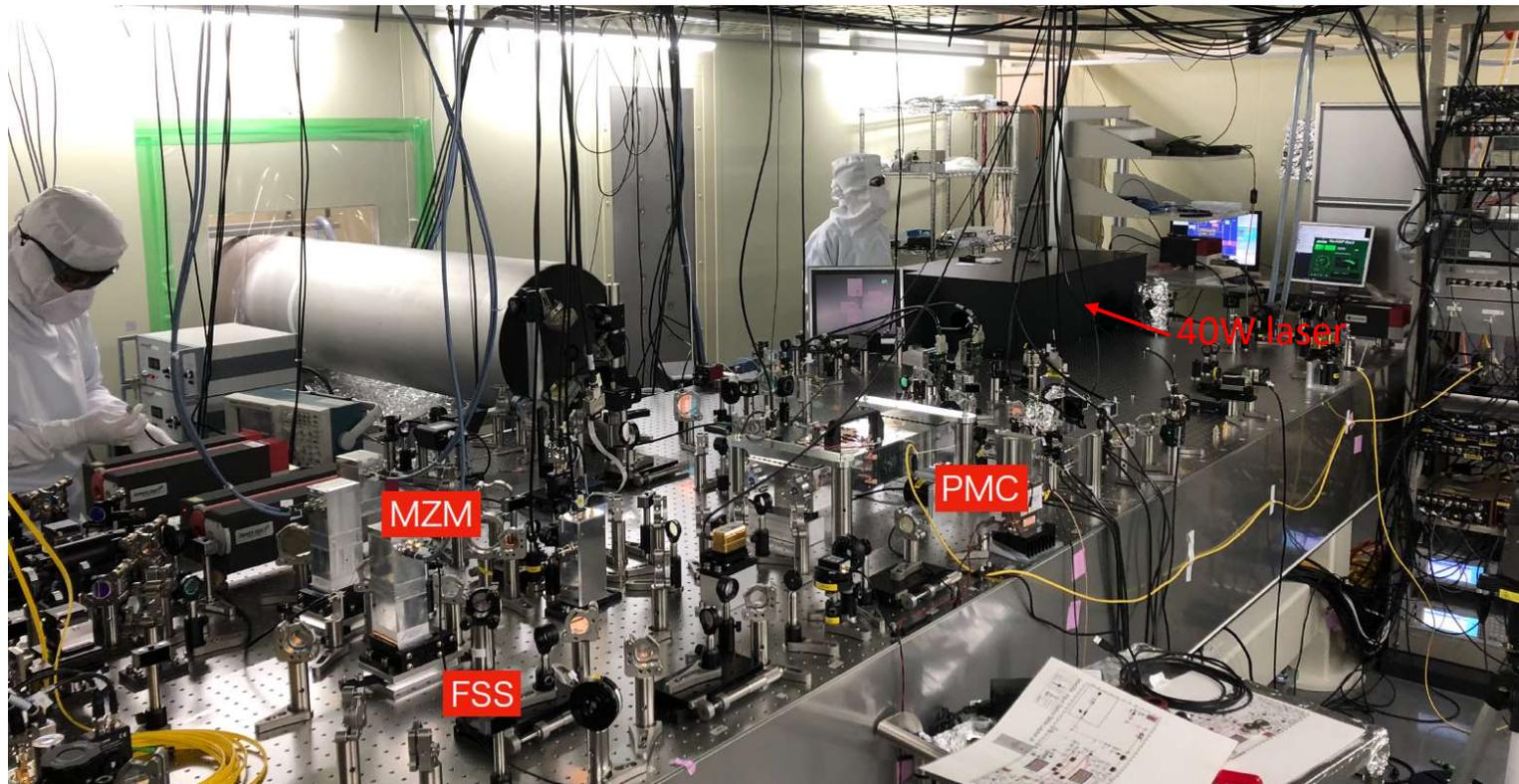
12/6/18

JGW-G1809351

Keiko Kokeyama<sub>1</sub>

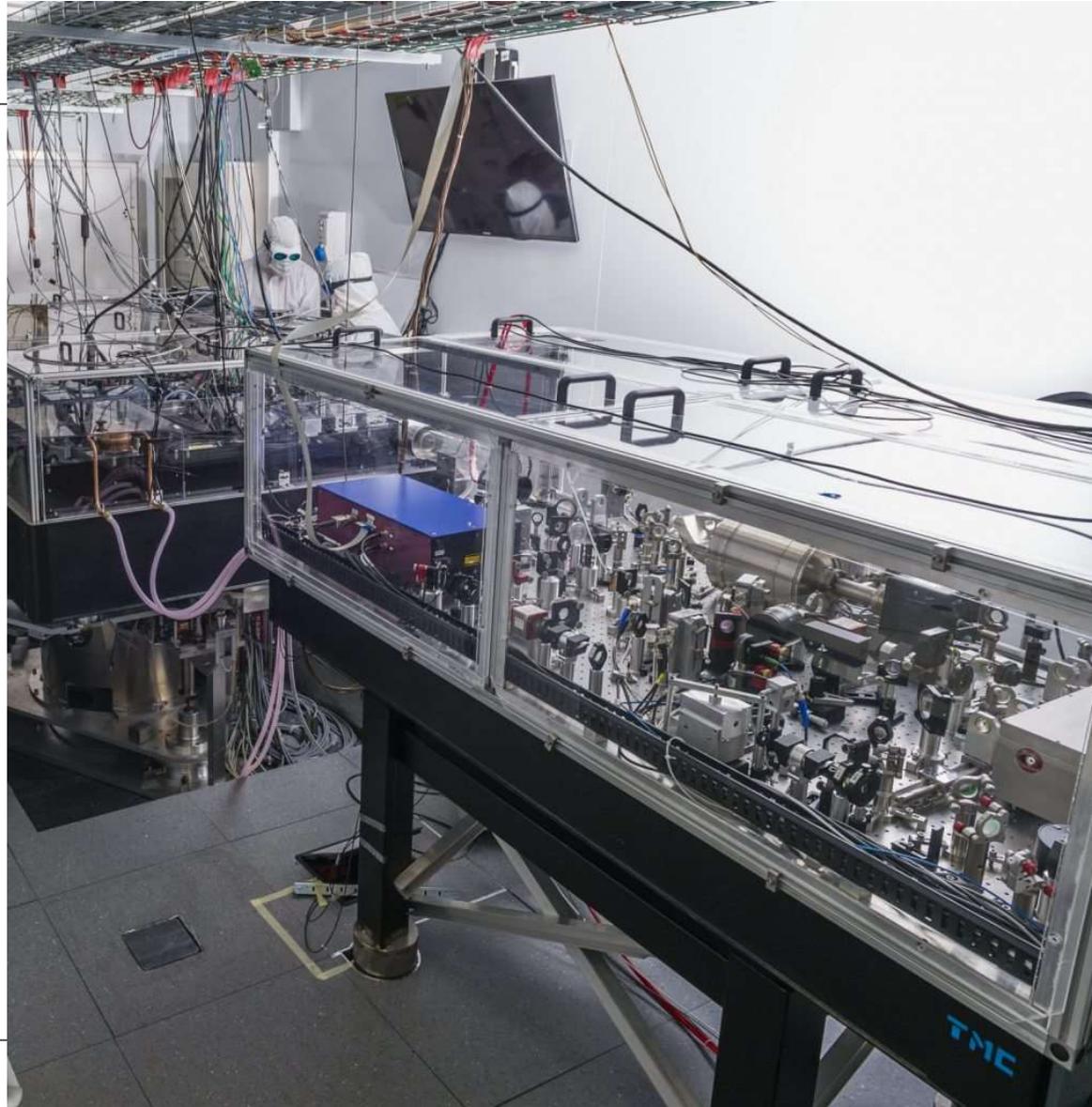
# PSL room of KAGRA

---



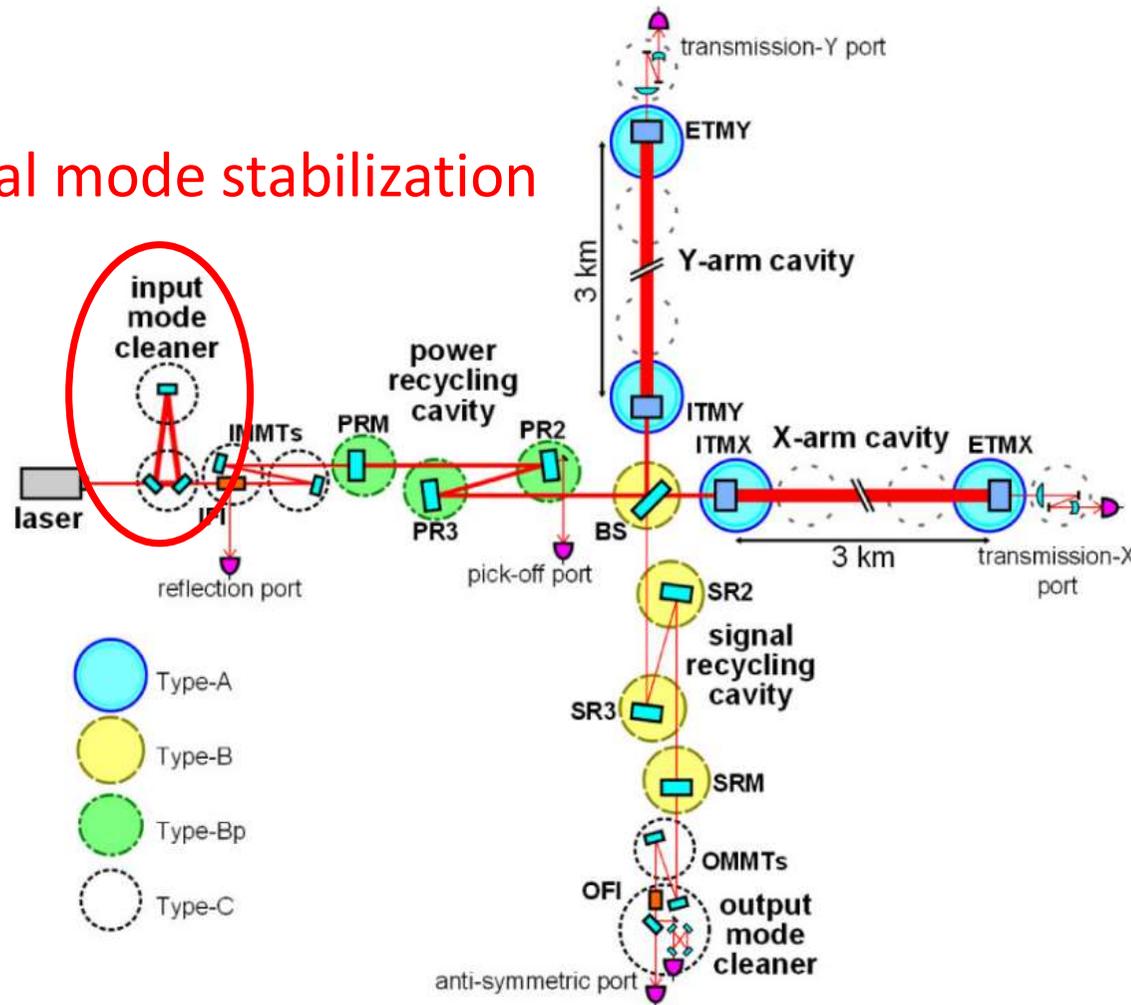
JGW-G1910363 – Masayuki Nakano

---



# KAGRA interferometer

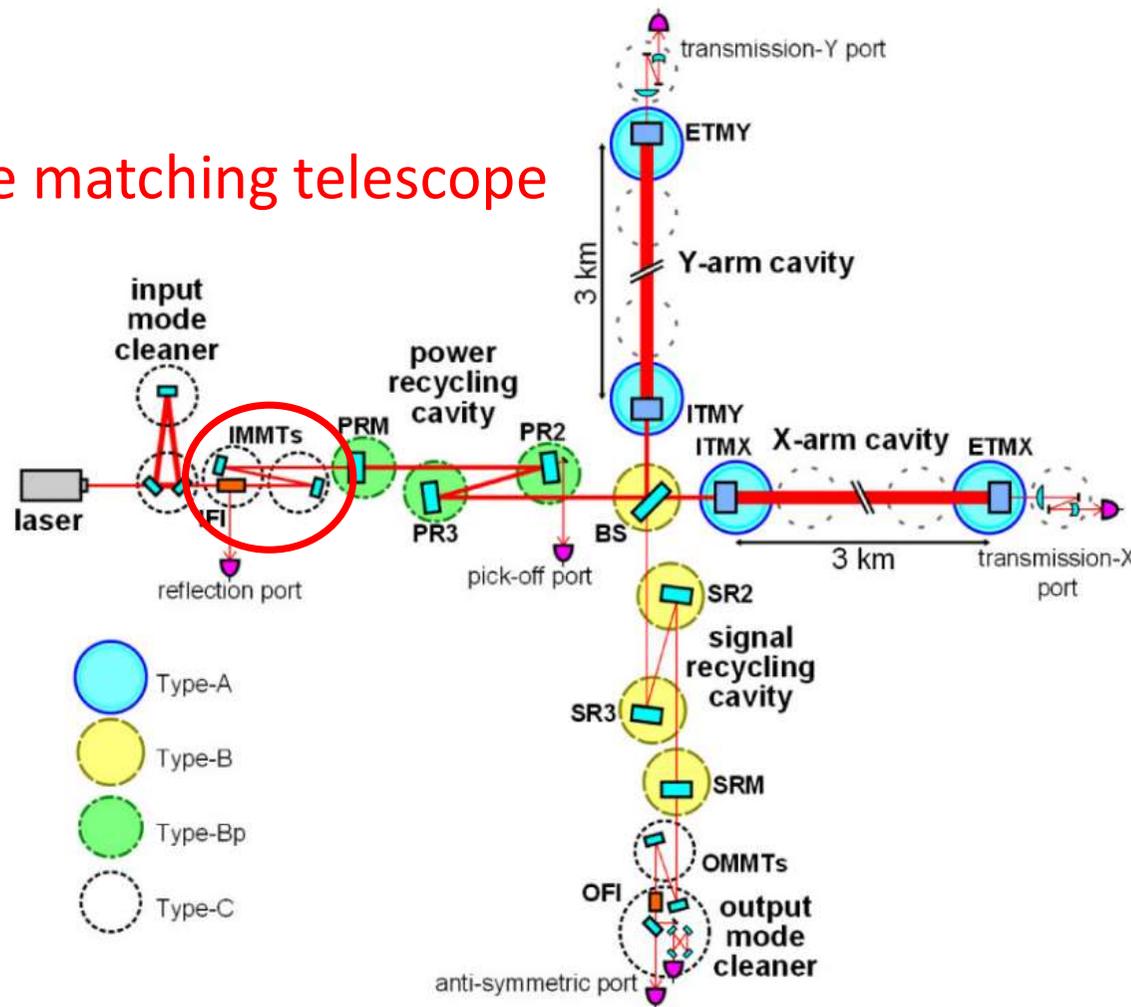
## Spatial mode stabilization



IOO : Input output optics  
MIF : Main interferometer  
MIR : Mirror  
MMT : Mode matching telescope  
OMC : Output mode cleaner

# KAGRA interferometer

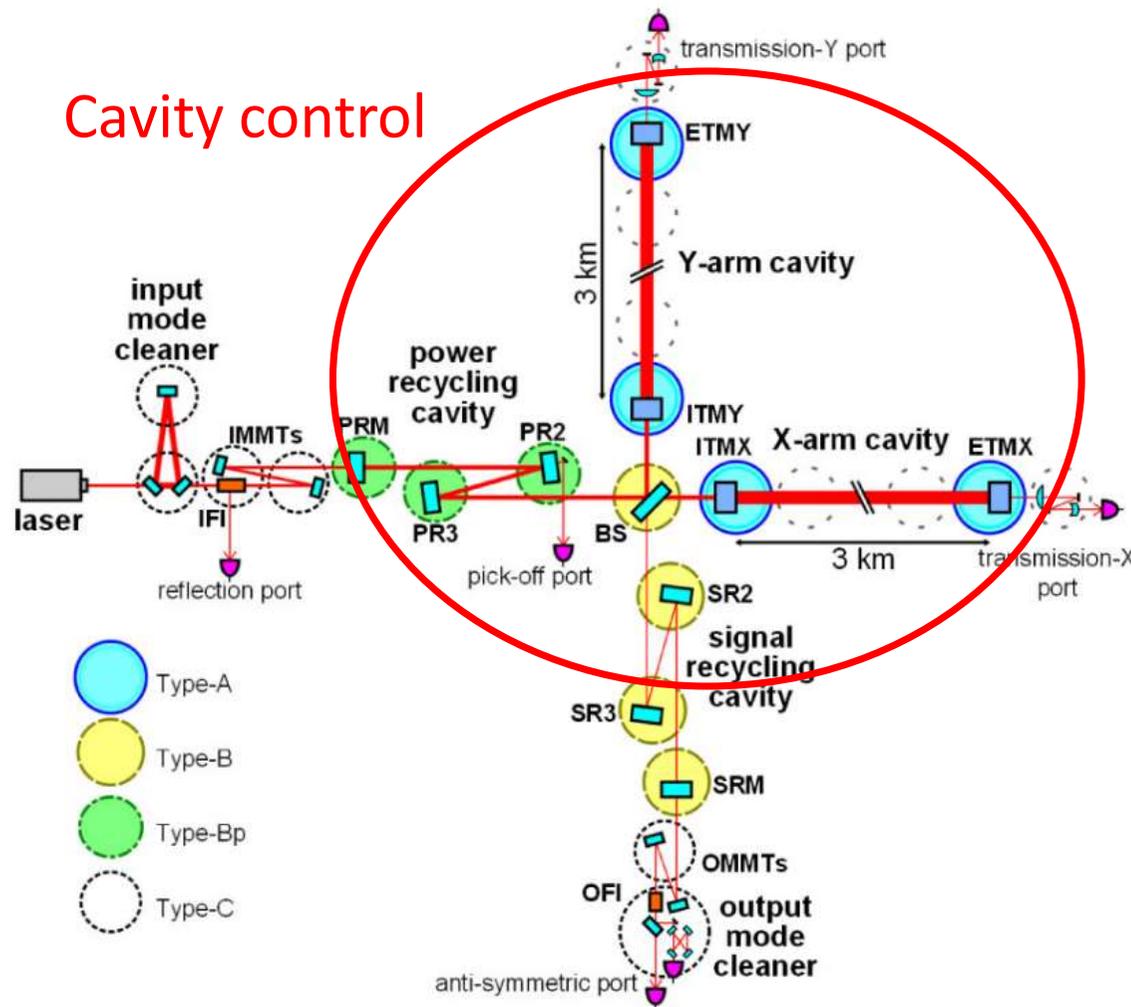
Mode matching telescope



IOO : Input output optics  
MIF : Main interferometer  
MIR : Mirror  
MMT : Mode matching telescope  
OMC : Output mode cleaner

# KAGRA interferometer

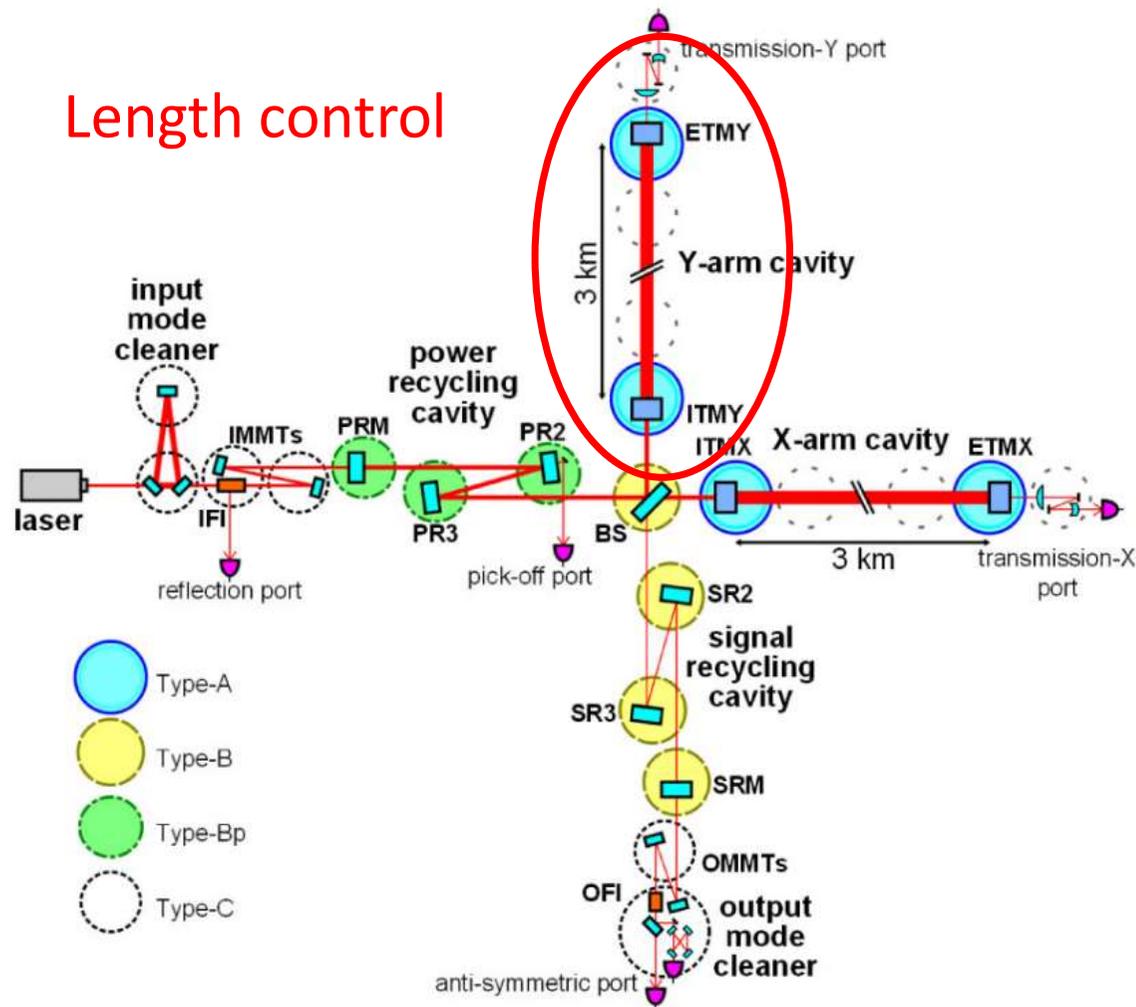
## Cavity control



IOO : Input output optics  
MIF : Main interferometer  
MIR : Mirror  
MMT : Mode matching telescope  
OMC : Output mode cleaner

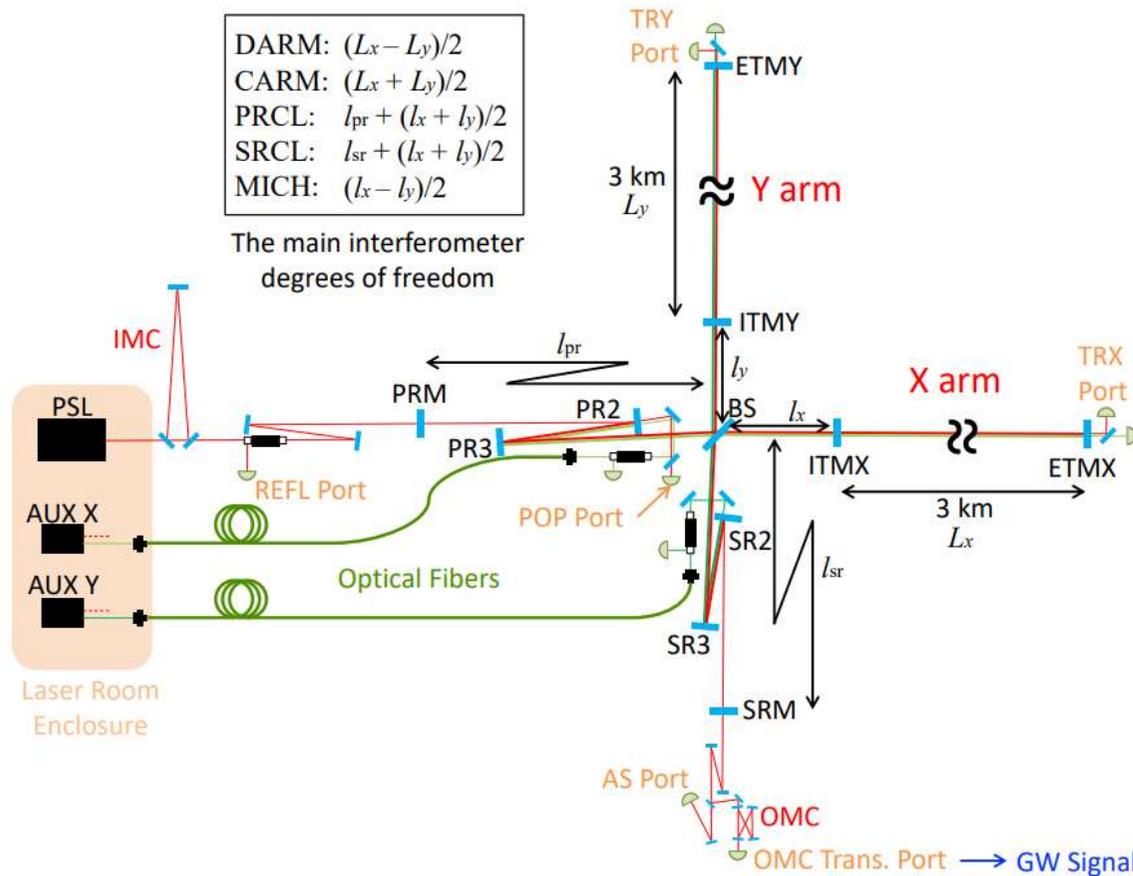
# KAGRA interferometer

Length control



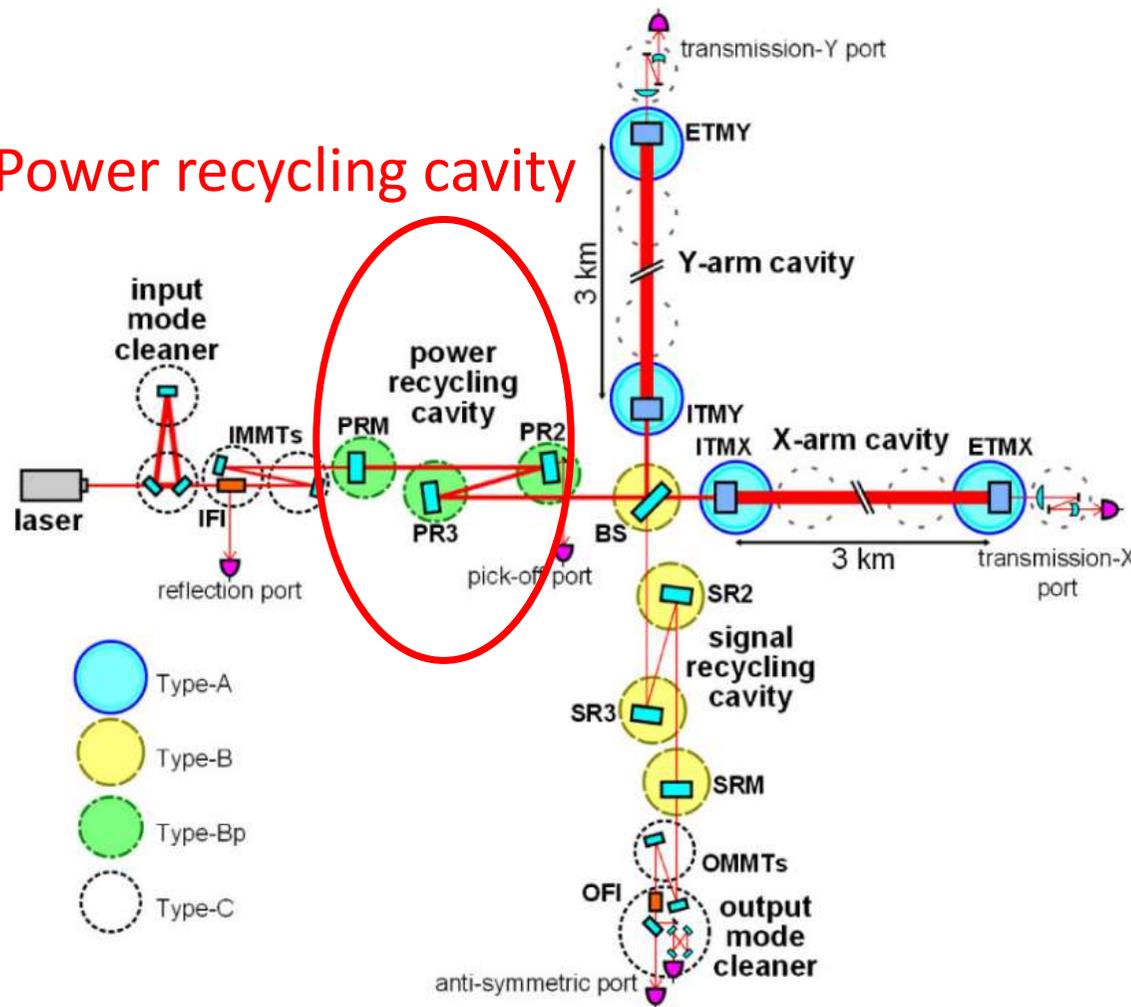
IOO : Input output optics  
MIF : Main interferometer  
MIR : Mirror  
MMT : Mode matching telescope  
OMC : Output mode cleaner

# Arm length stabilization of KAGRA



# KAGRA interferometer

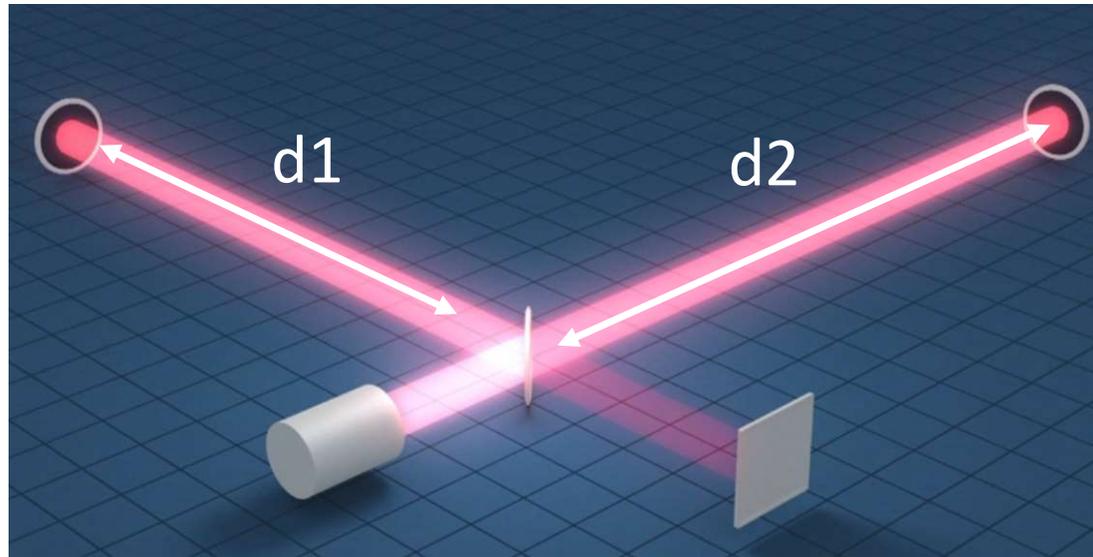
Power recycling cavity



IOO : Input output optics  
MIF : Main interferometer  
MIR : Mirror  
MMT : Mode matching telescope  
OMC : Output mode cleaner

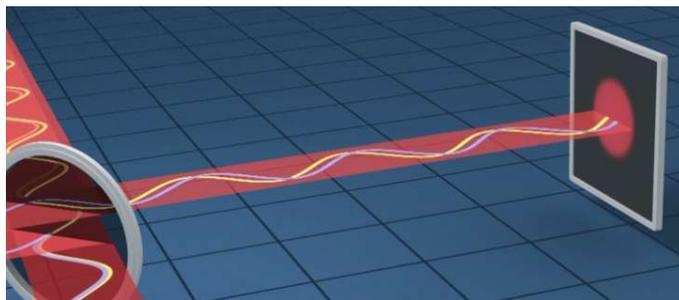
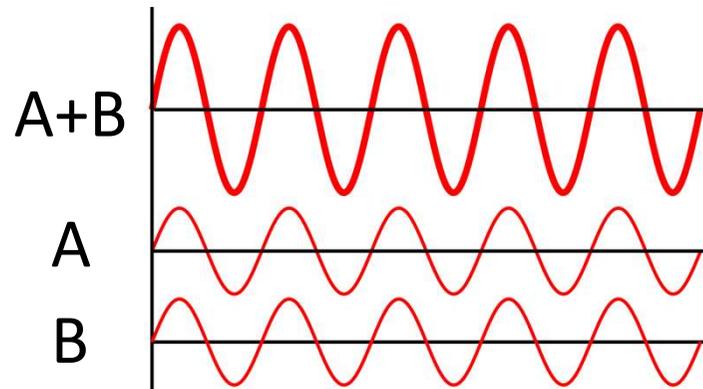
# Power recycling cavity

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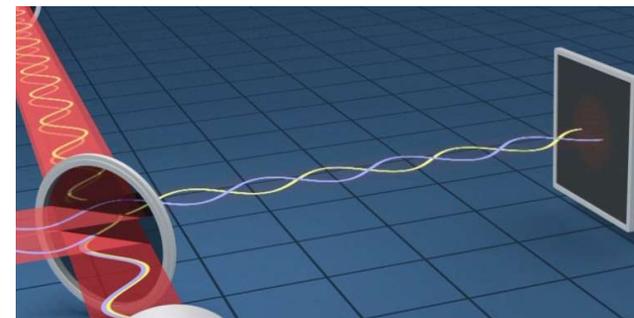
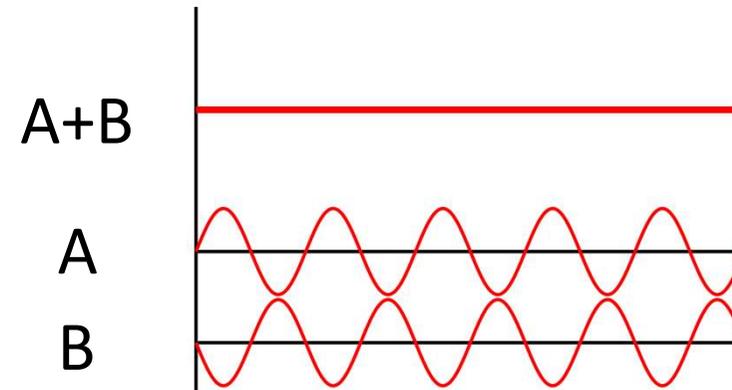


# Power recycling cavity

---



Constructive

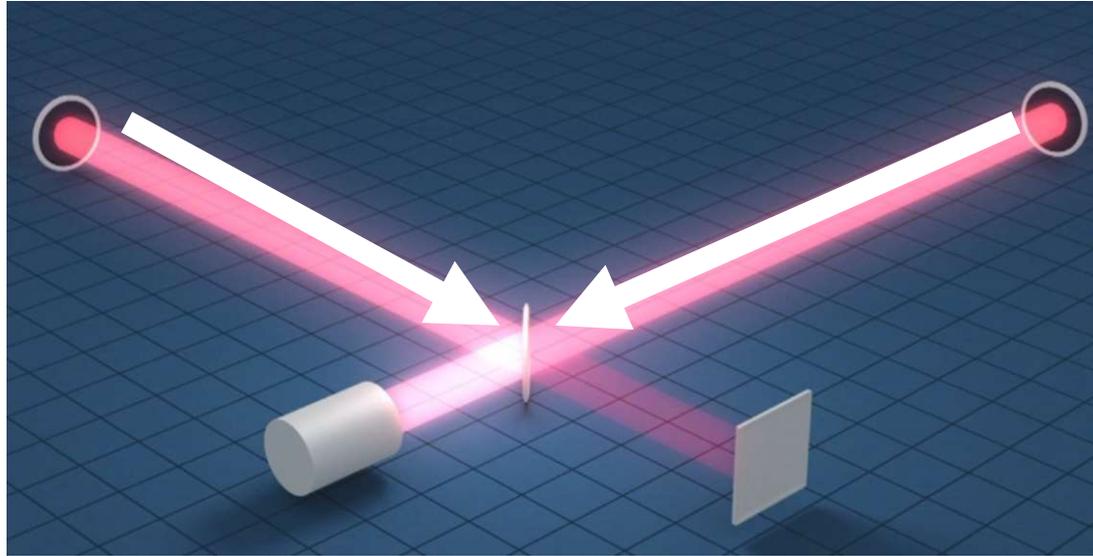


Destructive

---

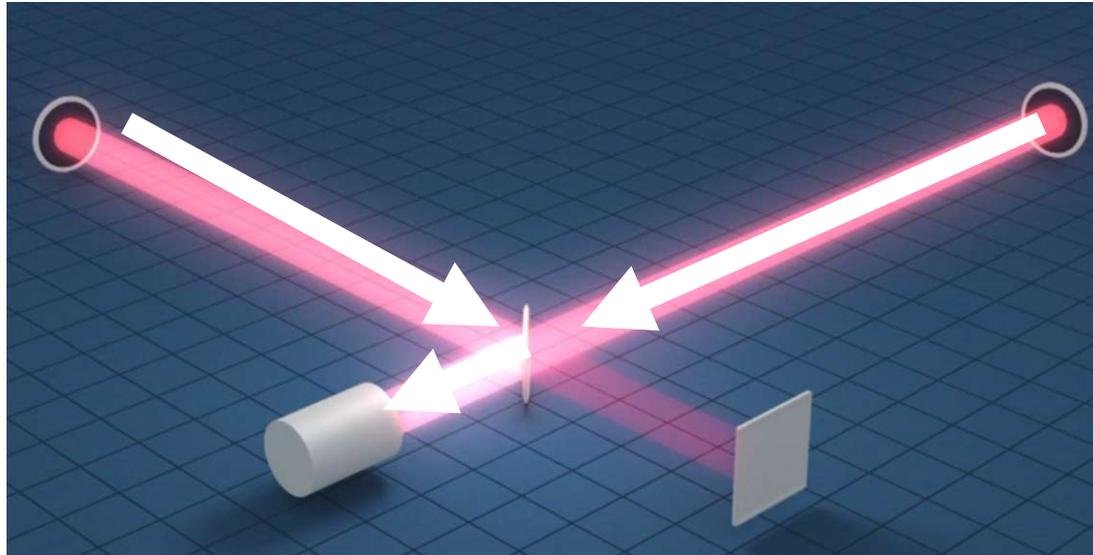
# Power recycling cavity

---



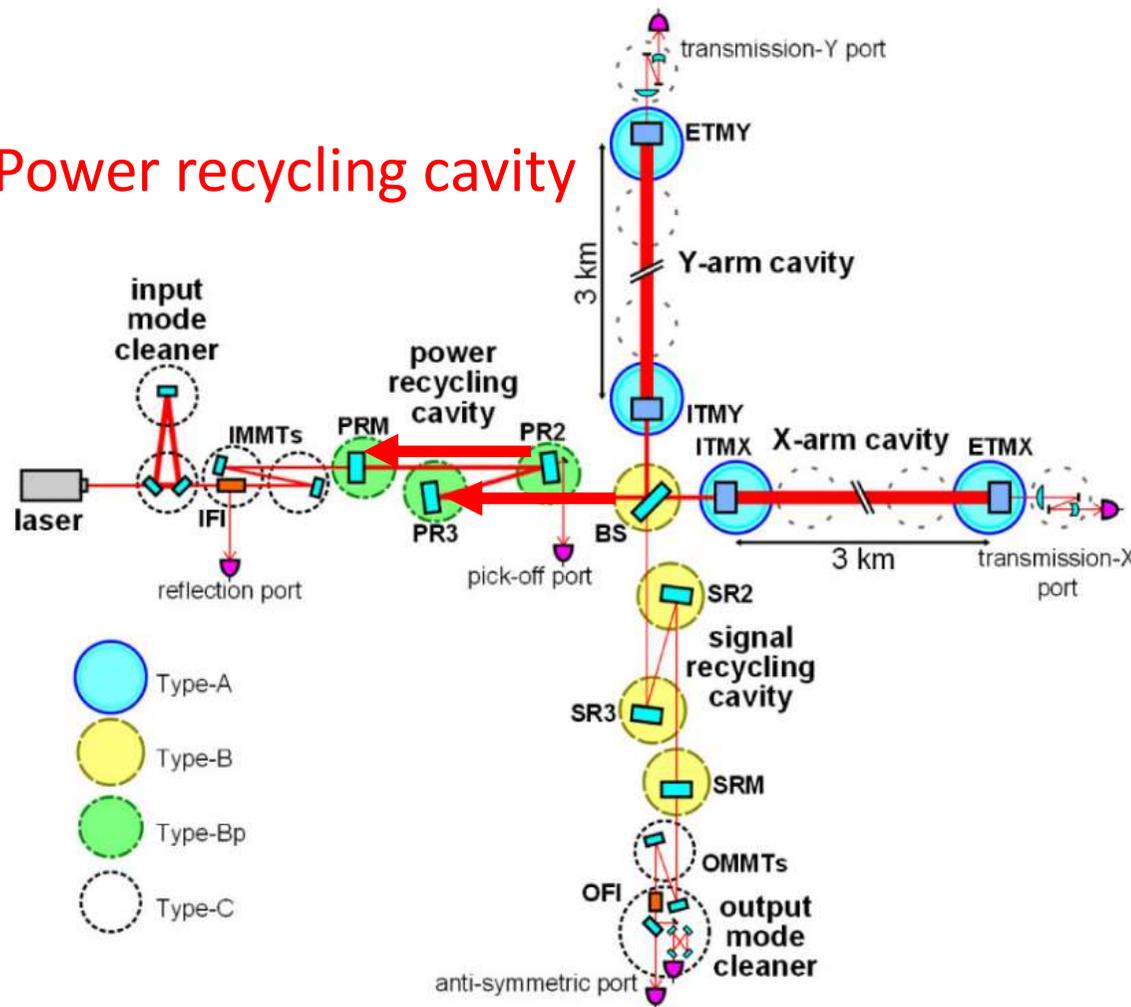
# Power recycling cavity

---



# KAGRA interferometer

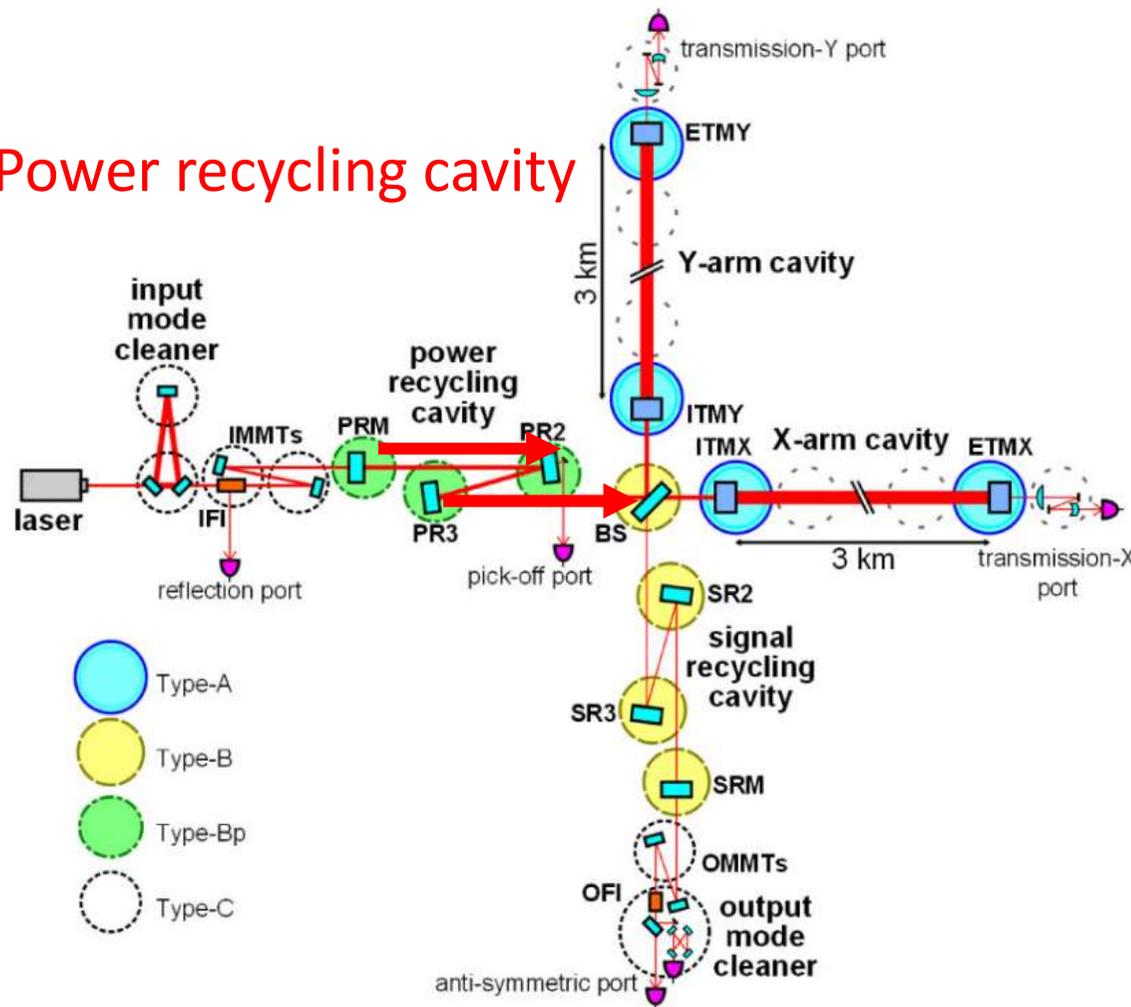
Power recycling cavity



IOO : Input output optics  
MIF : Main interferometer  
MIR : Mirror  
MMT : Mode matching telescope  
OMC : Output mode cleaner

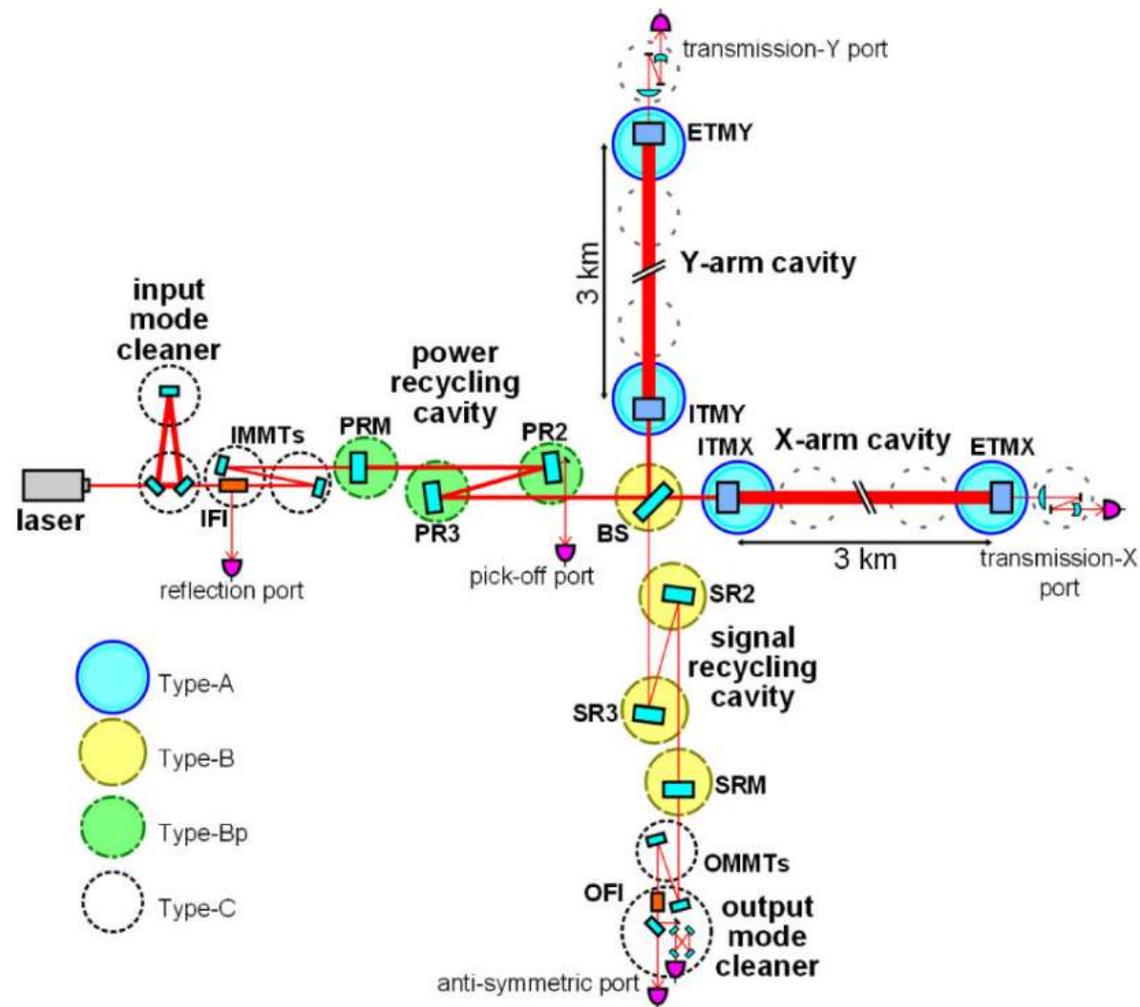
# KAGRA interferometer

Power recycling cavity



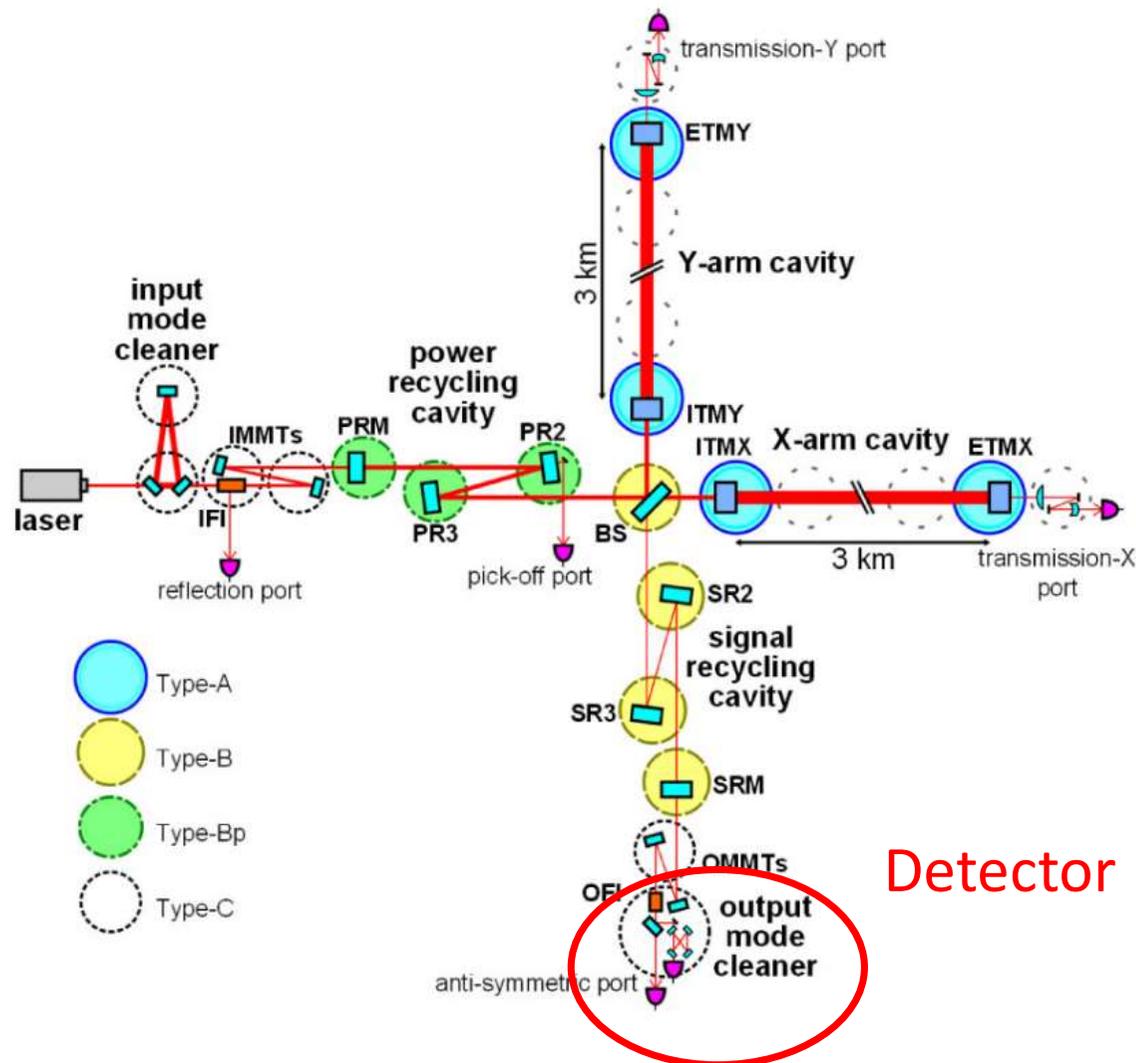
IOO : Input output optics  
MIF : Main interferometer  
MIR : Mirror  
MMT : Mode matching telescope  
OMC : Output mode cleaner

# KAGRA interferometer

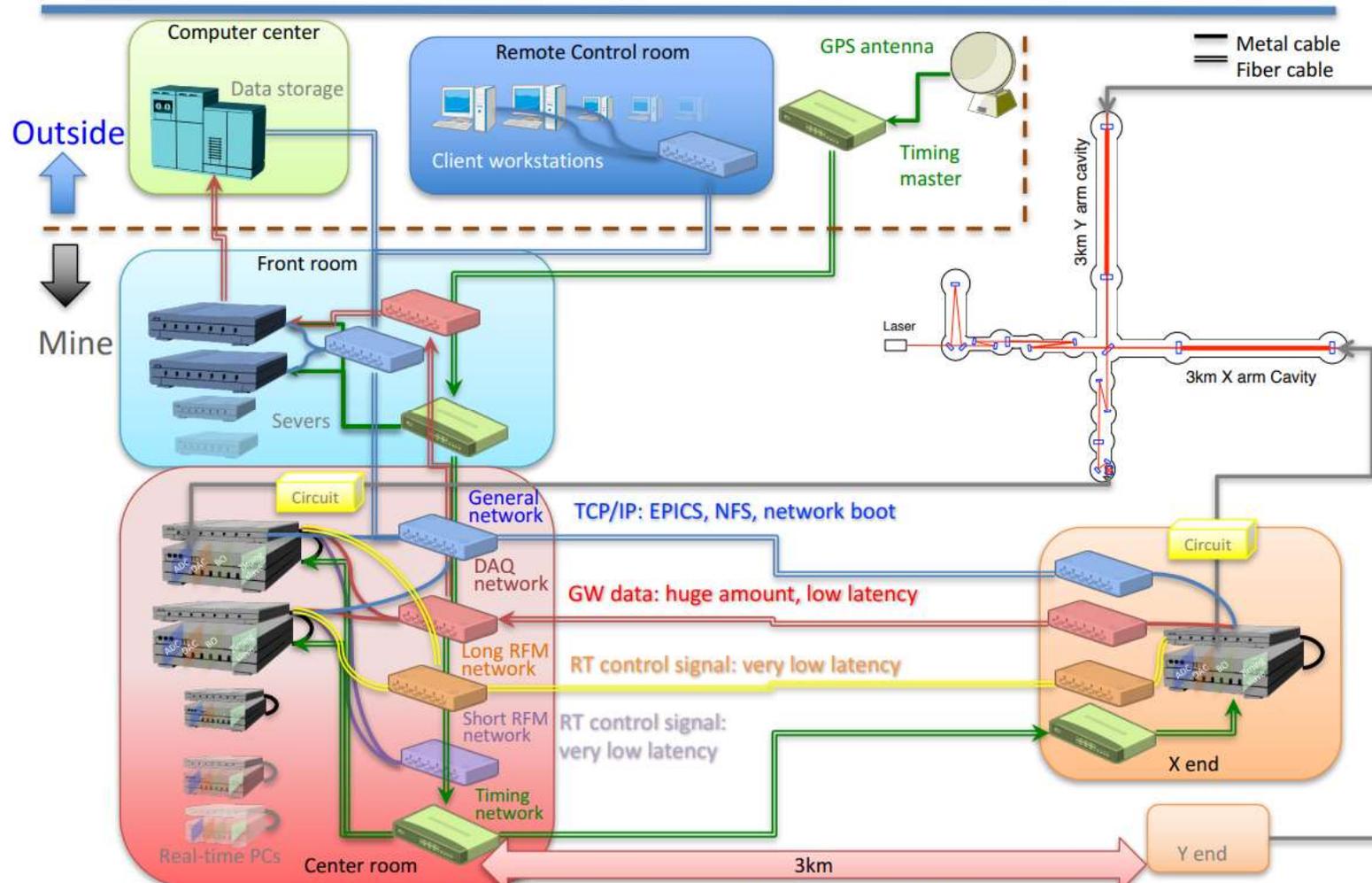


IOO : Input output optics  
MIF : Main interferometer  
MIR : Mirror  
MMT : Mode matching telescope  
OMC : Output mode cleaner

# KAGRA interferometer



IOO : Input output optics  
MIF : Main interferometer  
MIR : Mirror  
MMT : Mode matching telescope  
OMC : Output mode cleaner



# Sensors in gravitational wave detector

