

블랙홀 쌍성의 형성과 진화

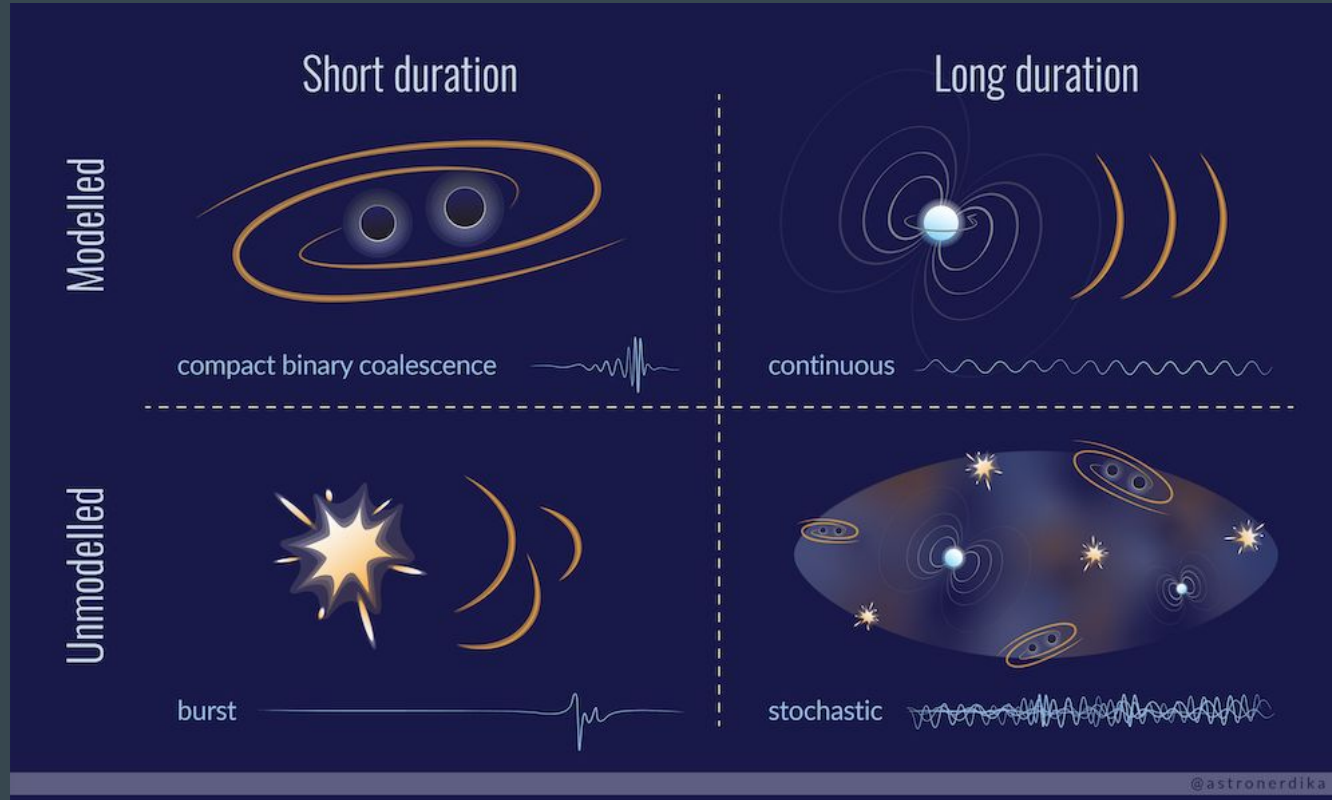
...

배영복 (중앙대)
2024 수치상대론 및 중력파여름학교
2024. 08. 01

Introduction

...

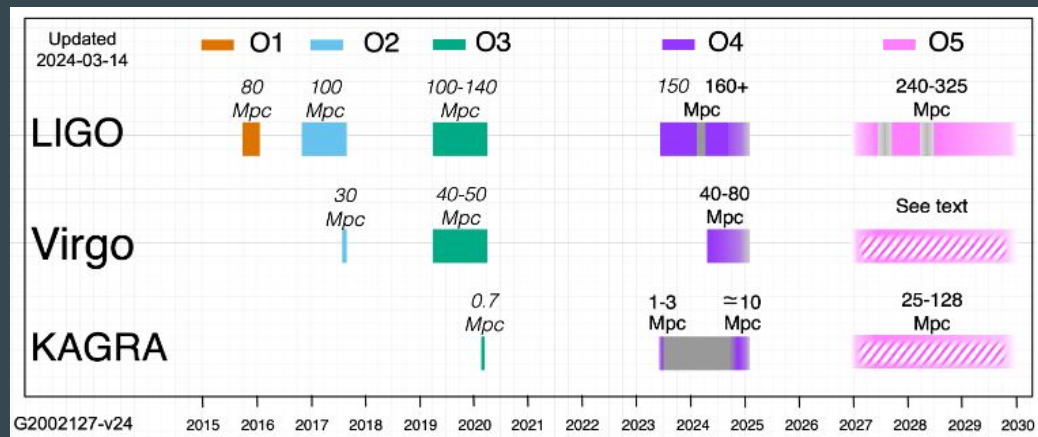
GW sources



Credit:
Shanika Galaudage

Observation of Gravitational Waves (GWs)

- GWTC-1 (Gravitational-Wave Transient Catalog)
 - O1 (Sep. 12, 2015 - Jan. 19, 2016)
 - First detection of GWs
 - O2 (Nov. 30, 2016 - Aug. 25, 2017)
 - First detection of a binary neutron star inspiral
 - 11 GW sources
- GWTC-2, GWTC-2.1
 - O3a (Apr. 01, 2019 - Oct. 01, 2019)
 - 44 GW sources
- GWTC-3
 - O3b (Nov. 01, 2019 - Mar. 27, 2020)
 - 35 GW sources
- GWTC-4 ?
 - O4a (May. 24, 2023 - Jan. 16, 2024)
 - O4b (Apr. 10, 2024 - Jun. 9, 2025)
 - Hundreds of GW sources?



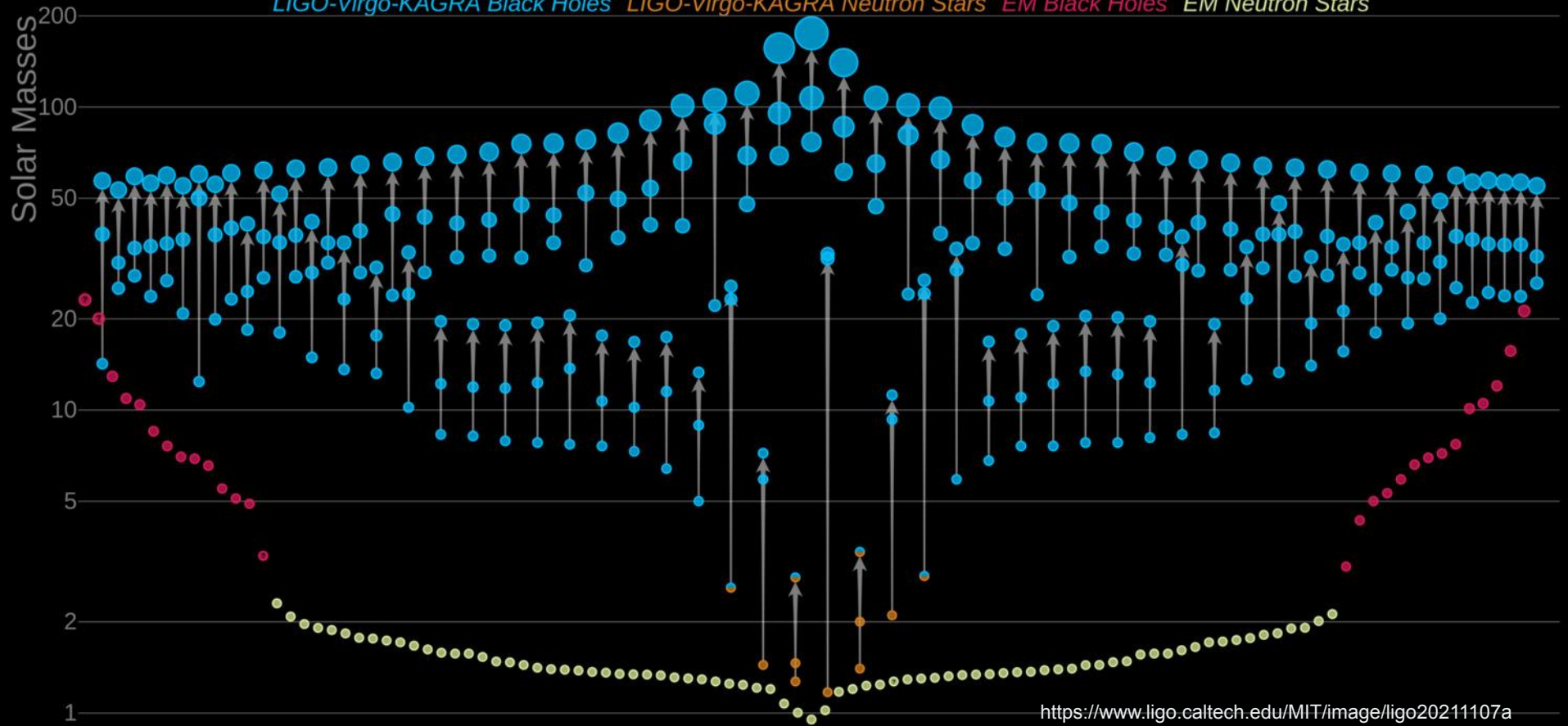
<https://observing.docs.ligo.org/plan/>

Name	Version	Release	GPS	Mass 1 (M_{\odot})	Mass 2 (M_{\odot})	Network SNR	Distance (Mpc)	χ_{eff}	Total Mass (M_{\odot})
GW200322_091133	v1	CWTC-3-confident	1268903511.3	+130 38 -22	+24.3 11.3 -6.0	+2.7 4.5 -3.0	+12500 3500 -2200	+0.54 0.27 -0.58	+132 50 -22
GW200316_215756	v1	CWTC-3-confident	1268431094.1	+10.2 13.1 -2.9	+2.0 7.8 -2.9	+0.4 10.3 -0.7	+480 1120 -440	+0.27 0.13 -0.10	+7.2 21.2 -2.0
GW200311_115853	v1	CWTC-3-confident	1267963151.3	+6.4 34.2 -3.8	+4.1 27.7 -5.9	+0.2 17.8 -0.2	+280 1170 -400	+0.16 -0.02 -0.20	+5.3 61.9 -4.2
GW200308_173609	v1	CWTC-3-confident	1267724187.7	+166 60 -29	+36 24 -13	+2.5 4.7 -2.9	+13900 7100 -4400	+0.58 0.16 -0.49	+169.0 92.0 -48.0
GW200306_093714	v1	CWTC-3-confident	1267522652.1	+17.1 28.3 -7.7	+6.5 14.8 -6.4	+0.4 7.8 -0.6	+1700 2100 -1100	+0.28 0.32 -0.46	+11.8 43.9 -7.5
GW200302_015811	v1	CWTC-3-confident	1267149509.5	+8.7 37.8 -8.5	+8.1 20.0 -5.7	+0.3 10.8 -0.4	+1020 1480 -700	+0.25 0.01 -0.26	+9.6 57.8 -6.9
GW200225_060421	v1	CWTC-3-confident	1266645879.3	+5.0 19.3 -3.0	+2.8 14.0 -3.5	+0.3 12.5 -0.4	+510 1150 -530	+0.17 -0.12 -0.28	+3.6 33.5 -3.0
GW200224_222234	v1	CWTC-3-confident	1266618172.4	+6.7 40.0 -4.5	+4.8 32.7 -7.2	+0.2 20.0 -0.2	+500 1710 -650	+0.15 0.10 -0.16	+7.2 72.3 -5.3
GW200220_124850	v1	CWTC-3-confident	1266238148.1	+14.1 38.9 -8.6	+9.2 27.9 -9.0	+0.3 8.5 -0.5	+2800 4000 -2200	+0.27 -0.07 -0.33	+17 67 -12
GW200220_061928	v1	CWTC-3-confident	1266214786.7	+40 87 -23	+26 61 -25	+0.4 7.2 -0.7	+4800 6000 -3100	+0.40 0.06 -0.38	+55 148 -33
GW200219_094415	v1	CWTC-3-confident	1266140673.1	+10.1 37.5 -6.9	+7.4 27.9 -8.4	+0.3 10.7 -0.5	+1700 3400 -1500	+0.23 -0.08 -0.29	+12.6 65.0 -8.2
GW200216_220804	v1	CWTC-3-confident	1265926102.8	+22 51 -13	+14 30 -16	+0.4 8.1 -0.5	+3000 3800 -2000	+0.34 0.10 -0.36	+20 81 -14
GW200210_092254	v1	CWTC-3-confident	1265361792.9	+7.5 24.1 -4.6	+0.47 2.83 -0.42	+0.5 8.4 -0.7	+430 940 -340	+0.22 0.02 -0.21	+7.1 27.0 -4.3
GW200209_085452	v1	CWTC-3-confident	1265273710.1	+10.5 35.6 -6.8	+7.8 27.1 -7.8	+0.4 9.6 -0.5	+1900 3400 -1800	+0.24 -0.12 -0.30	+13.9 62.6 -9.4

...
<https://gwosc.org/eventapi/html/GWTC/>

Masses in the Stellar Graveyard

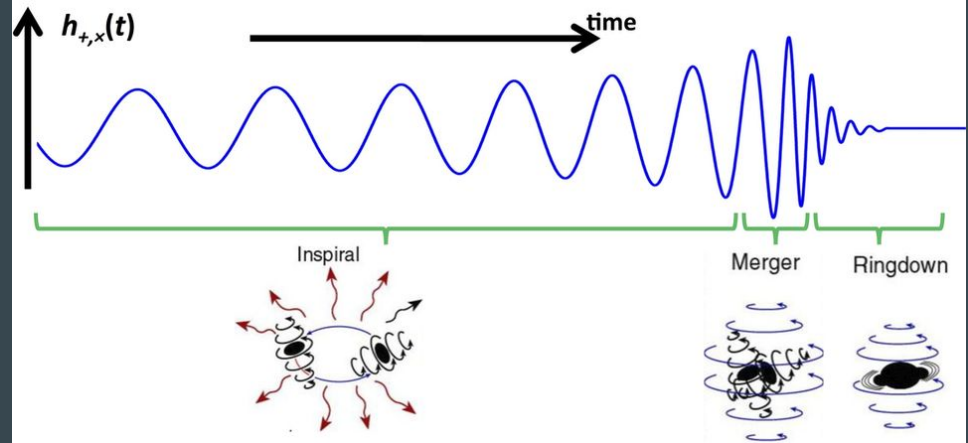
LIGO-Virgo-KAGRA Black Holes *LIGO-Virgo-KAGRA Neutron Stars* *EM Black Holes* *EM Neutron Stars*

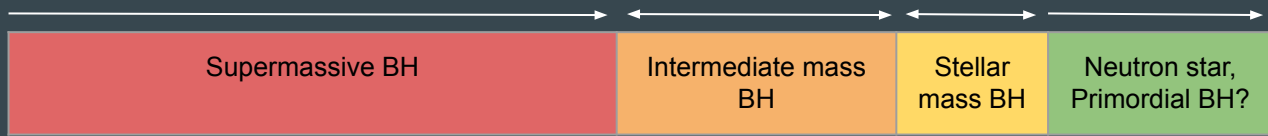
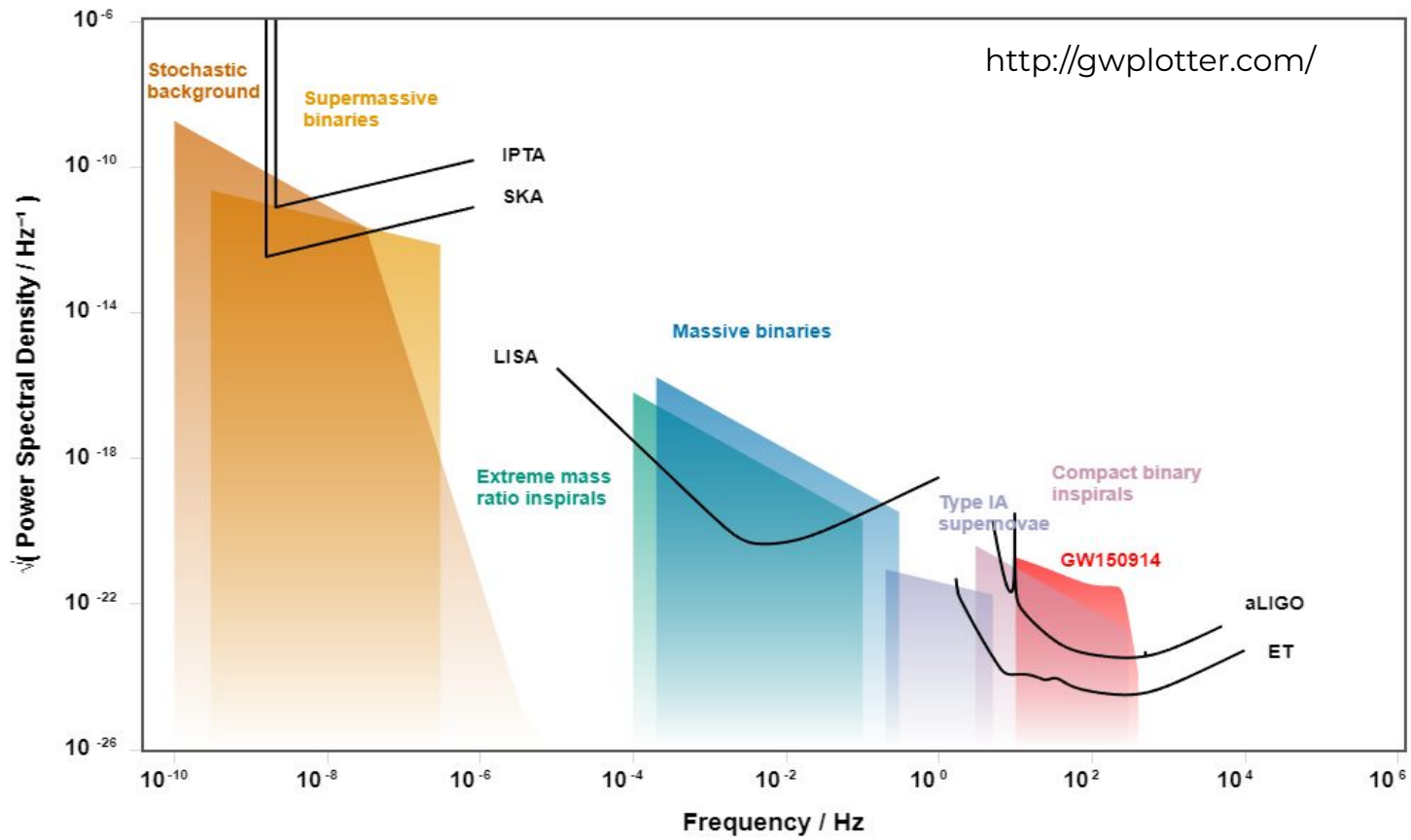


<https://www.ligo.caltech.edu/MIT/image/ligo20211107a>

Binary black holes (BBHs)

- More than 90% of GW sources ever detected
- Strong GW signal
- Detectable frequency for current interferometric GW detectors
- Predictable waveforms
- Coalescence
 - Inspiral - Merger - Ringdown



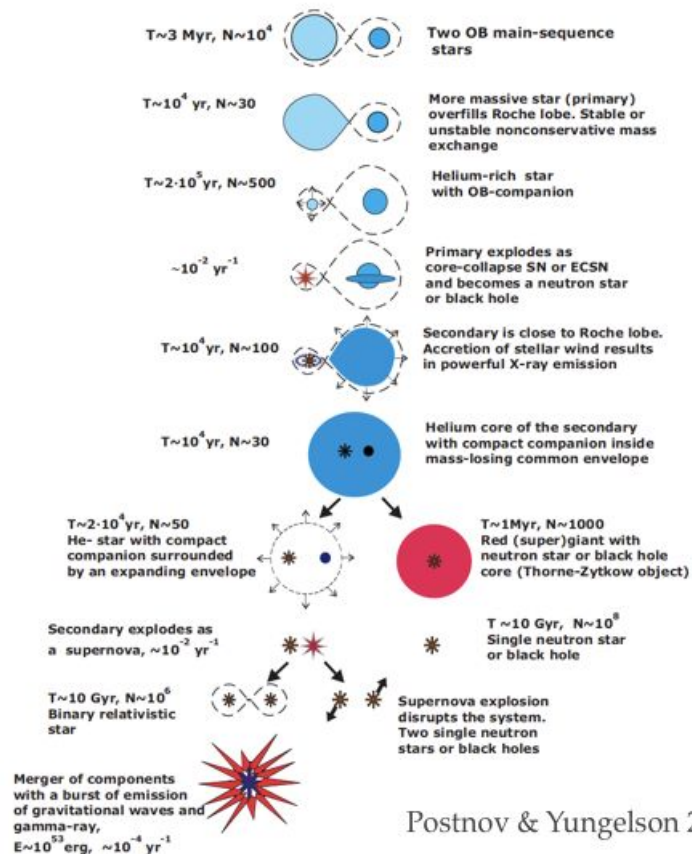


Formation

...

Formation of BBH

- Massive binary star \rightarrow Binary black hole



Postnov & Yungelson 2014

Figure 7: Evolutionary scenario for the formation of neutron stars or black holes in close binaries. T is the typical time scale of an evolutionary stage, N is the estimated number of objects in the given evolutionary stage.

Formation of BBH

- Dynamical evolution of star cluster
 - Self-gravitating system
 - Core collapse
 - Mass segregation
- Dynamical formation of BBH
 - Three-body process
 - Dynamical capture



M80 (NGC 6093)

[NASA, The Hubble Heritage Team, STScI, AURA - Great Images in NASA Description](#)

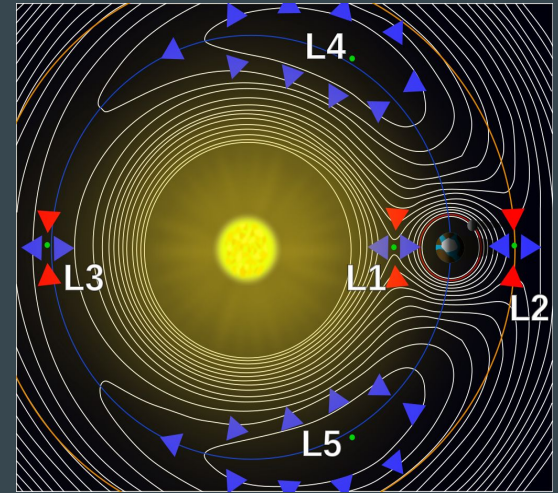


Nuclear star cluster of Milky Way

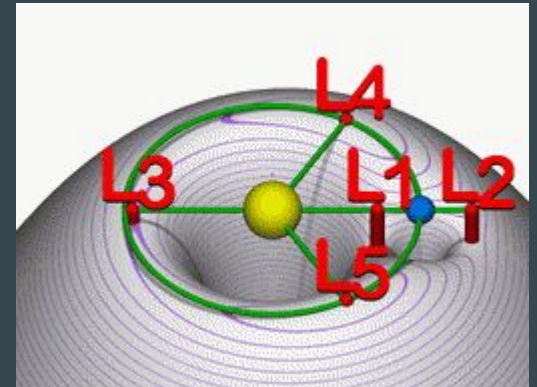
[Stefan Gillessen, Reinhard Genzel, Frank Eisenhauer
http://www.eso.org/public/outreach/press-rel/pr-2008/pr-46-08.html](http://www.eso.org/public/outreach/press-rel/pr-2008/pr-46-08.html)

Three-body problem

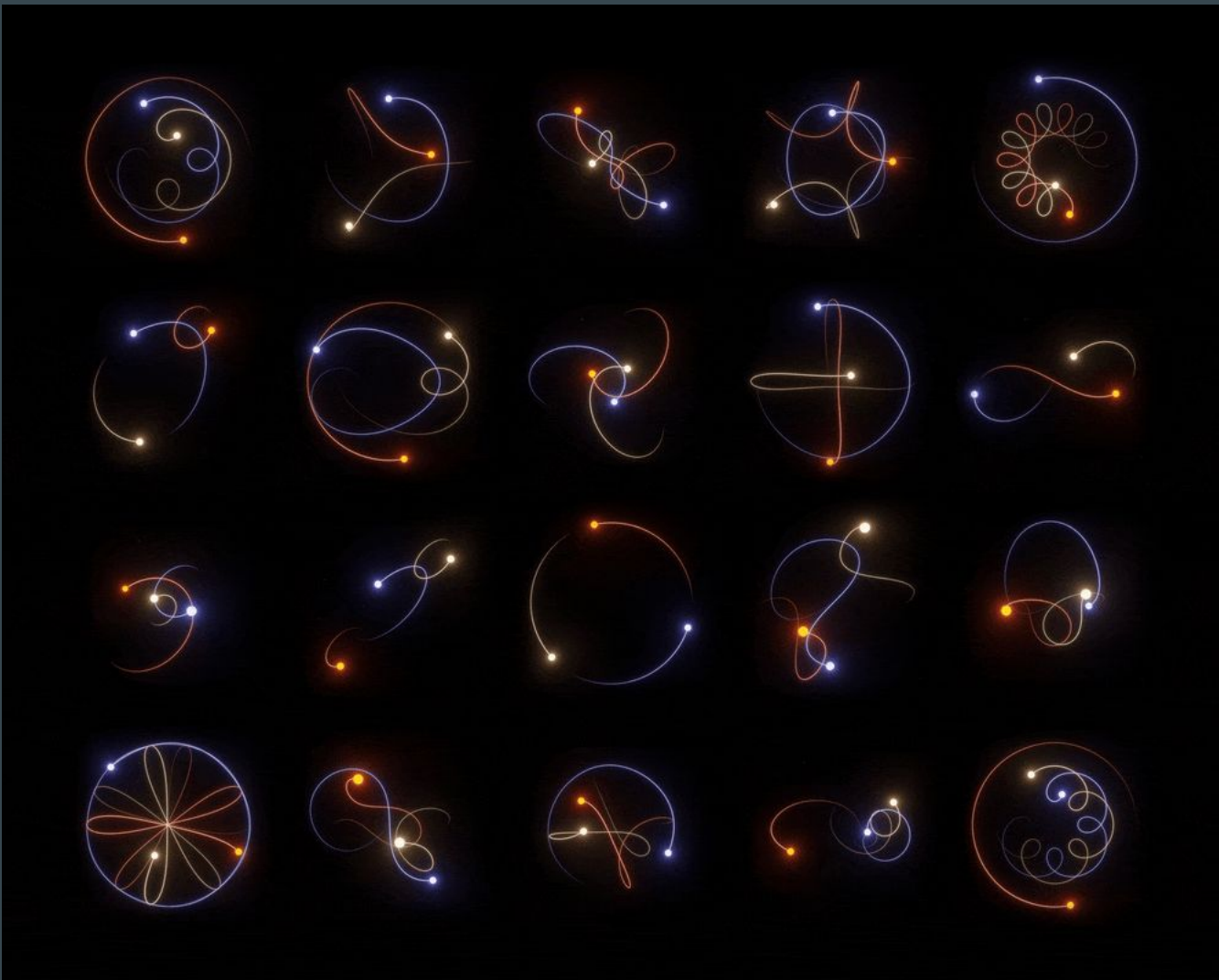
- No general closed-form solution exists, generally chaotic.
 - Series solution by Sundman (1912)
- Restricted three-body problem
 - one negligible mass under two massive bodies
 - Lagrange points
- Special case solutions
 - Euler's collinear solution, Figure-eight shape, ...
- Numerical methods are required in general.



https://en.wikipedia.org/wiki/Lagrange_point#/media/File:Lagrange_points2.svg



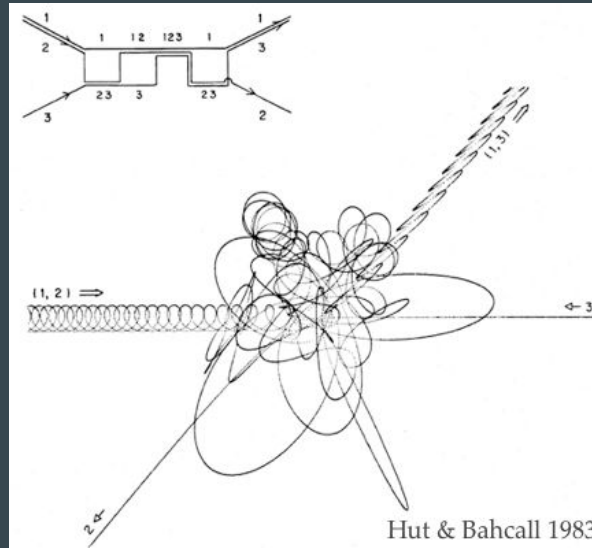
https://en.wikipedia.org/wiki/File:Lagrangian_points_eq_uipotential.gif



https://en.wikipedia.org/wiki/Three-body_problem#/media/File:5_4_800_36_downscaled.gif

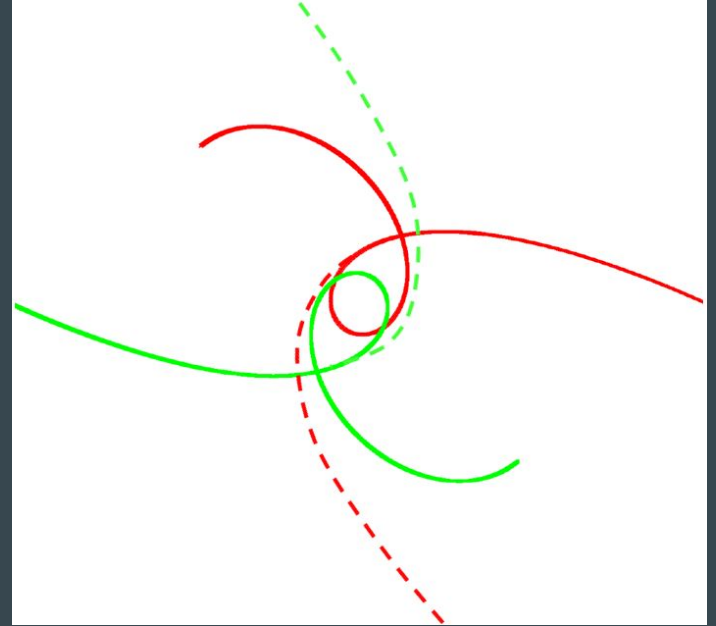
Three-body process

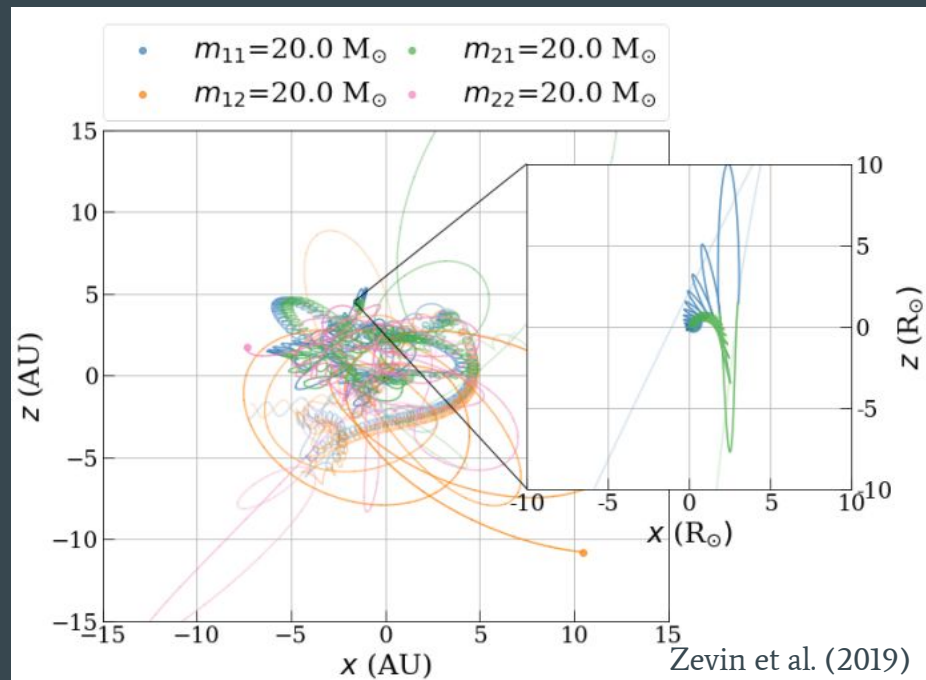
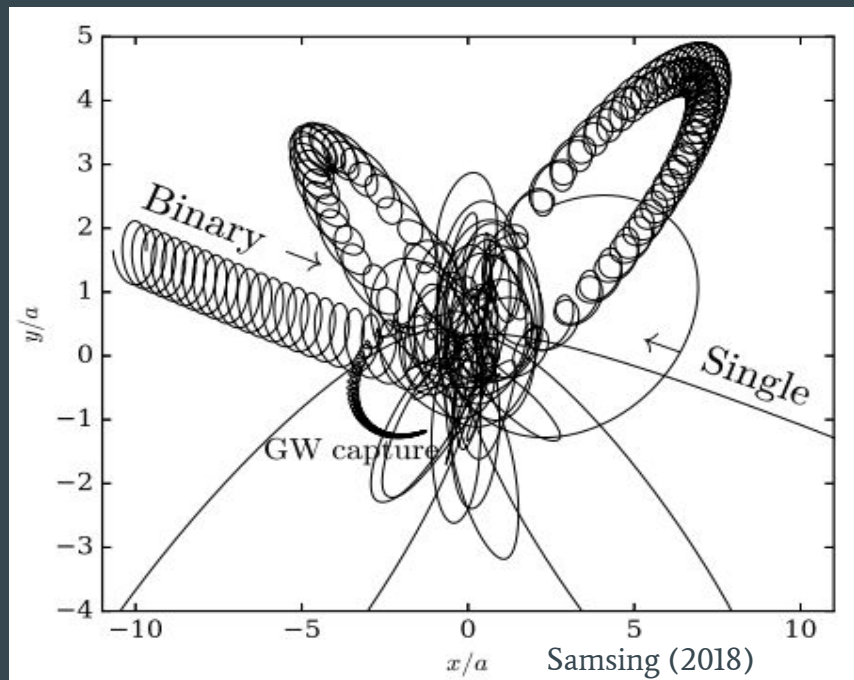
- Three-body process
 - Binary formation through the interactions of three or more bodies



Dynamical capture

- Orbital energy loss through GW emission
- Energy radiation $>$ orbital energy
- Hyperbolic \rightarrow Elliptic orbit





https://content.eid.ion.org/journals/0004-637X/87/1/91/revision1/apiaafcecf8_video.mp4?Expires=1723030060&Signature=8Mdkfu7WuBOikvTTixHxD2_D4yRWGt4z5VIFwBarrYimLuuMb-8mc550EEnLiBwK0u-3klNmcL41P385O75CPkaNd=faChMCPLJaxrb6GFAGZiailSuKzUFea-7FB5FWV9auL-36mubaDQUNo3KS0x0INB02_PVHHHOKS05SFDJJCcClO_sphxK-TIKX5k4yWmeIWuo416RL4IloivI84KtOmpxP3aa47eq-qrDnl_0CN5isMppOqOf-H6Qil982GFAYmCTpnybAnnNIVvrdnkZe8Zs-GbaouIUsoRM9bEv2L1LlpTDzODUG5bZrGoHoal-MpS-2M3nFrAUJohTPA_&Key-Pair-Id-KLI1D8TIY3N7T8

Evolution

...

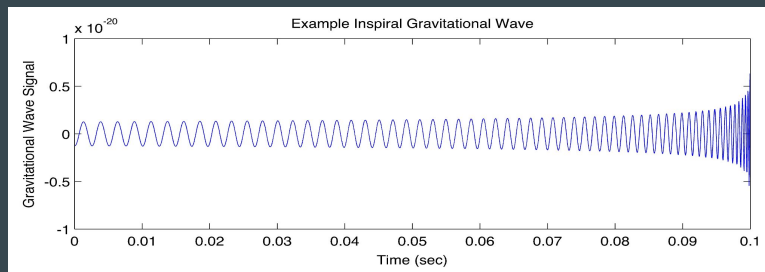
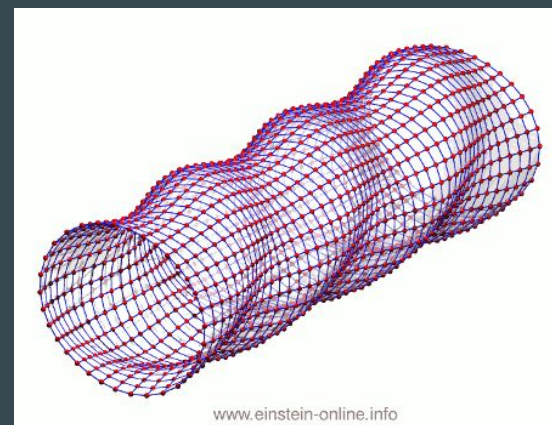
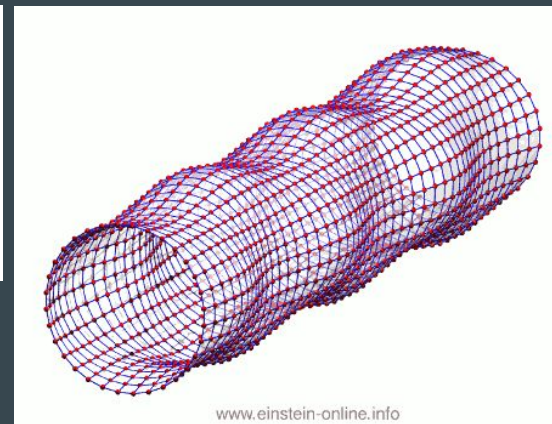
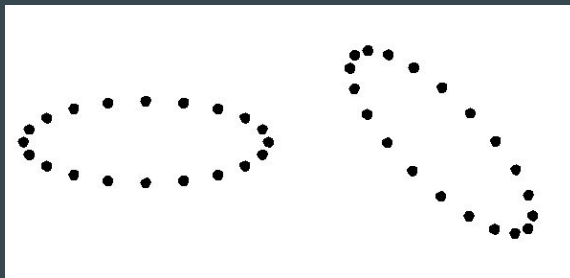
Inspiral

- Two polarization

$$h_+ = \frac{A}{r} (1 + \cos^2 i) \cos(2\pi ft) f^{2/3}$$

$$h_\times = \frac{2A}{r} \cos i \sin(2\pi ft) f^{2/3}$$

$$A = 2 \frac{G^{5/3}}{c^4} \pi^{2/3} M_c^{5/3}, \quad M_c \equiv \frac{(m_1 m_2)^{3/5}}{(m_1 + m_2)^{1/5}}$$

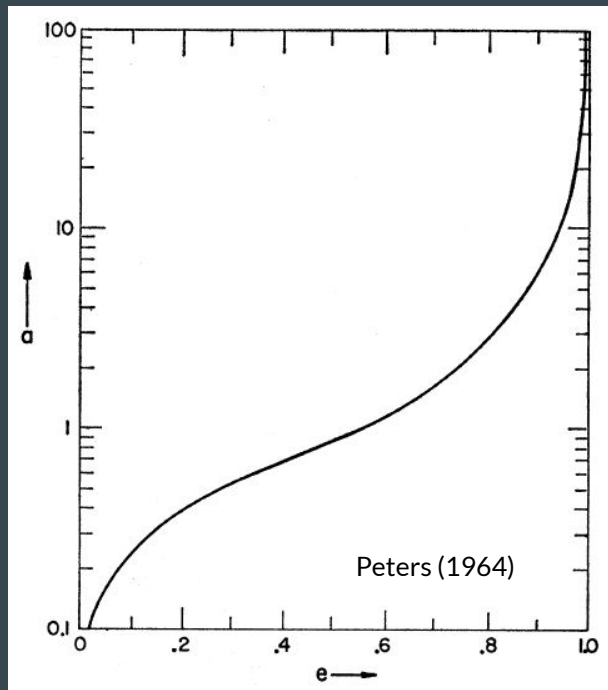
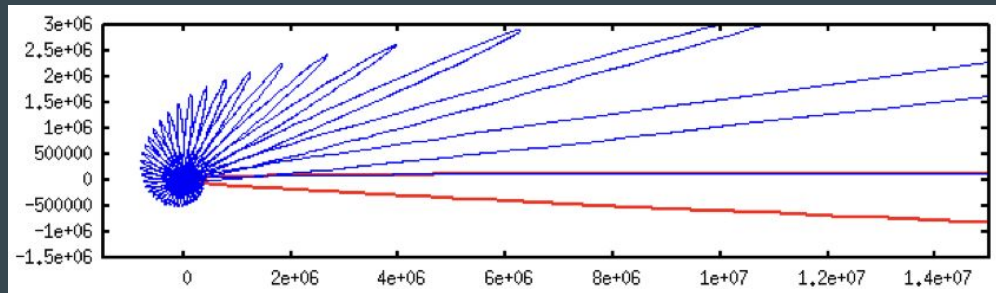


Inspiral

- Circularization

$$\left\langle \frac{da}{dt} \right\rangle = -\frac{64G^3 m_1 m_2 (m_1 + m_2)}{5 c^5 a^3 (1 - e^2)^{7/2}} \left(1 + \frac{73}{24} e^2 + \frac{37}{96} e^4 \right)$$

$$\left\langle \frac{de}{dt} \right\rangle = -\frac{304}{15} e \frac{G^3 m_1 m_2 (m_1 + m_2)}{c^5 a^4 (1 - e^2)^{5/2}} \left(1 + \frac{121}{304} e^2 \right)$$



Inspiral

- Innermost Stable Circular Orbit (ISCO)
- ISCO of test particle in Schwarzschild metric

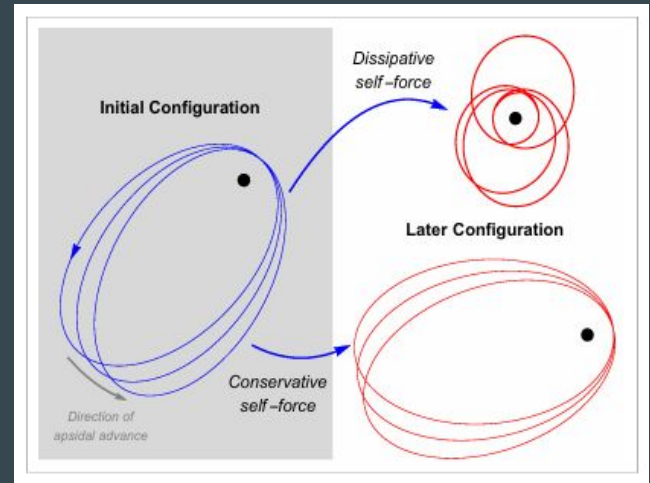
$$r_{ISCO} = \frac{6GM}{c^2}$$

- Highest GW frequency of inspiral phase

$$f_{ISCO,GW} = \frac{1}{\pi} \left(\frac{1}{6} \right)^{3/2} \frac{c^3}{G(m_1 + m_2)} \approx \frac{4396}{M/M_\odot} \text{Hz}$$

Inspiral

- Eccentricity



Osburn et al. (2016)

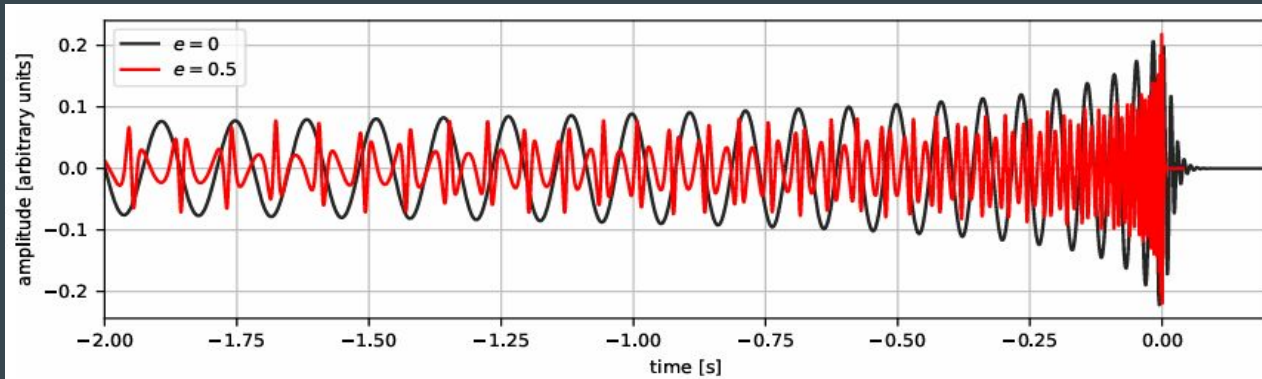
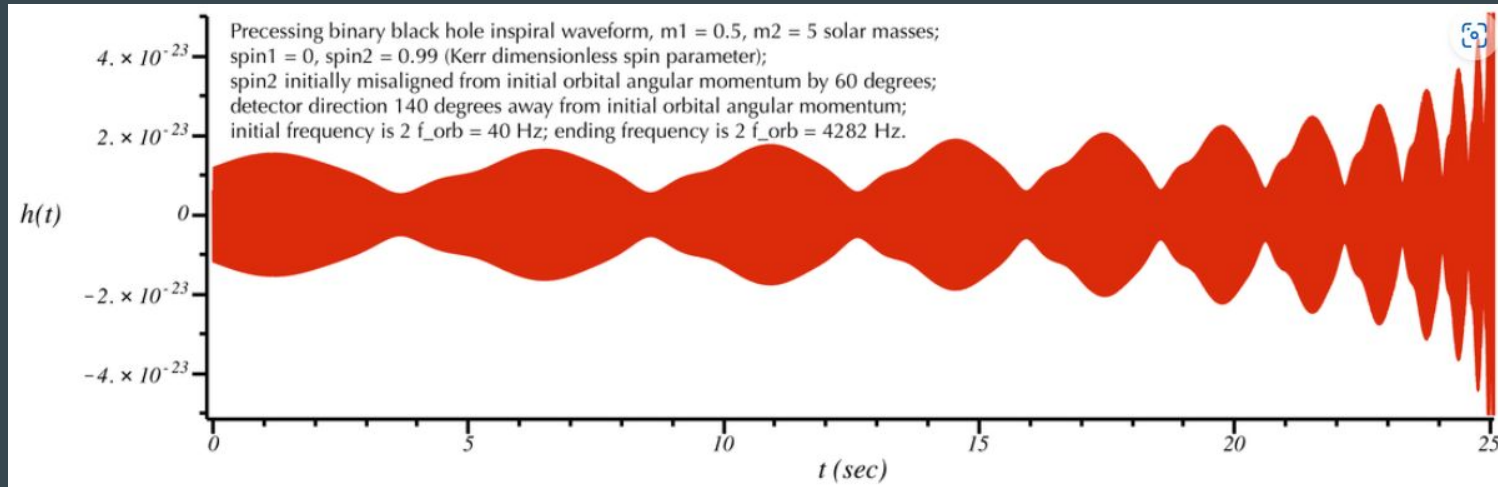


Figure 1. Examples of gravitational waveforms for a $10 M_{\odot} - 10 M_{\odot}$ BBH system with eccentricities 0 (black) and 0.5 (red).

Abbott et al. (2019)

Inspiral

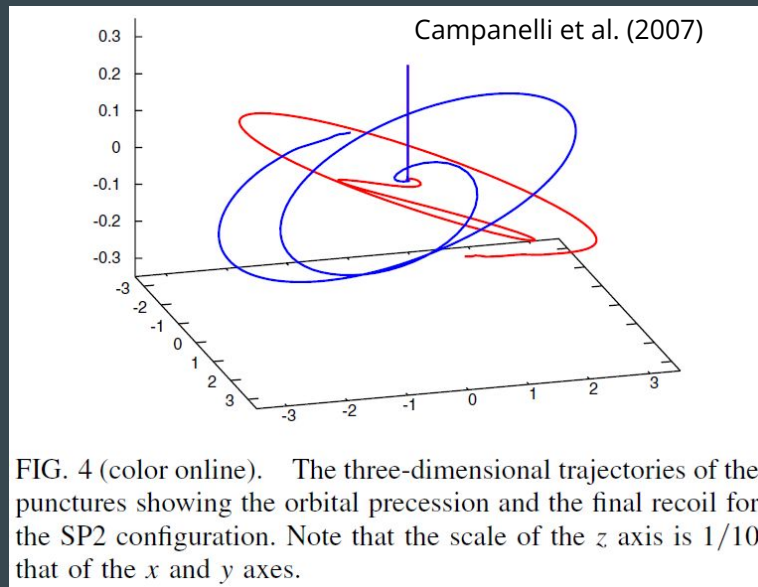
- Spin



<https://www.soundsofspacetime.org/spinning-binaries.html>

Merger

- GW emission peak
- Numerical relativity
- Recoil (Kick)
 - Asymmetric GW emission
 - Unequal mass, Spin
 - Up to $\sim 10,000$ km/s (Healy et al. 2009)



Ringdown

- Ringing of merged BH
 - Gradually settling into a stable Kerr BH
 - Damped oscillation after the merger
 - Higher GW frequency than inspiral
 - Astrophysical information - mass, spin
 - Quasi-normal mode (Berti et al. 2006, ...)
 - Quasi: damping by emitting GWs
- $$h(t) \sim A \exp[i(f_R + i f_I)t]$$
- Testing general relativity



Summary

- Binary black holes are the main targets of current GW detectors.
 - Formation
 - Evolution of stellar binary
 - Dynamical formation in star cluster
 - Coalescence
 - Inspiral-Merger-Ringdown
-